

Verify that each of the following is an identity:

$$1. \quad 1 + \frac{1}{\cos \theta} \stackrel{?}{=} \frac{\tan^2 \theta}{\sec \theta - 1}$$

$$2. \quad \csc \theta \cdot \sec \theta \stackrel{?}{=} \cot \theta + \tan \theta$$

$$3. \quad \frac{\tan^2 \theta}{1 - \cos^2 \theta} \stackrel{?}{=} \frac{\sec \theta}{\cos \theta}$$

$$4. \quad (1 + \sin \theta)(1 - \sin \theta) \stackrel{?}{=} \frac{1}{\sec^2 \theta}$$

$$5. \frac{\cos^2 \theta}{1 - \sin \theta} = 1 + \sin \theta$$

$$6. \sin^2 \theta (\csc^2 \theta + \sec^2 \theta) = \sec^2 \theta$$

$$7. \sin \theta + \cos^2 \theta = \frac{1 + \tan \theta}{\sec \theta}$$

$$8. \frac{\sin \theta}{1 - \cos \theta} + \frac{1 - \cos^2 \theta}{\sin \theta} = 2 \csc \theta$$

