

Modified and Animated By Chris Headlee
Nov 2011

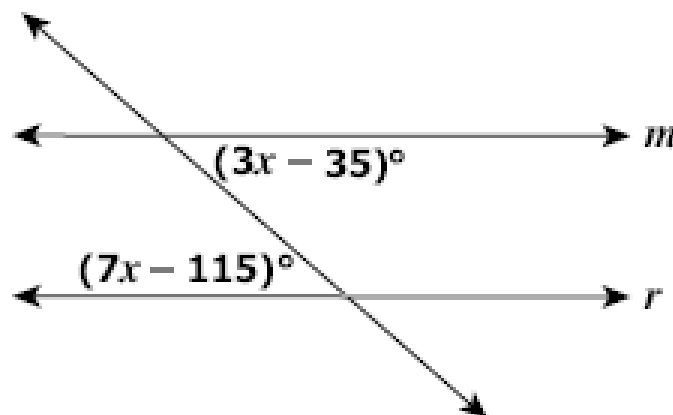
CHAPTER 3 SOL PROBLEMS

SSM: Super Second-grader Methods

SOL Problems; not Dynamic Variable Problems

2 Lines m and r are cut by a transversal.

Alternate Interior



SSM:

- both angle acute \rightarrow EQUAL
- plug in answers to see which make them equal

What value of x will show that line m is parallel to line r ?

- ☒ F 20
- ☐ G 24
- ☐ H 25
- ☐ J 33

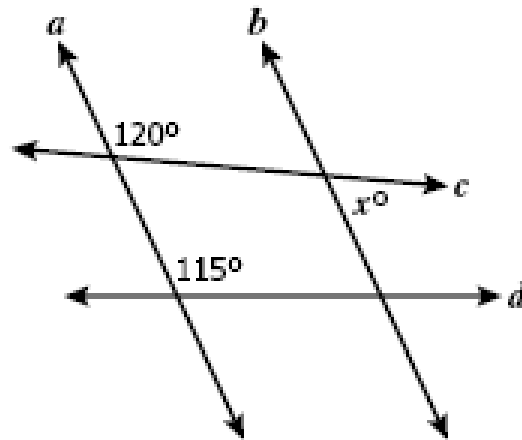
Alternate Interior angles are equal!

$$7x - 115 = 3x - 35$$

$$4x - 115 = -35$$

$$4x = 80$$

$$x = 20$$



If lines a and b are parallel, what is the value of x ?

- A 120
- B 115
- C 65
- D 60

SSM:

- x is acute
ELIMINATE A and B
- Magic Number is 180
- $x + \text{what} = 180$

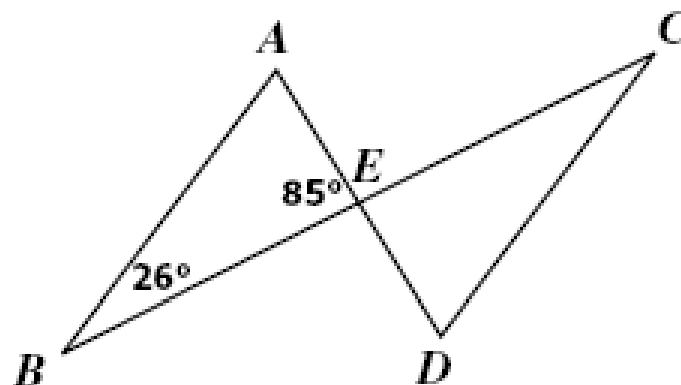
Angles must be formed by one transversal (line c)

x and 120 go together for a and b being parallel

$$x + 120 = 180$$

$$x = 60$$

5 For what measure of $\angle D$ is $\overline{AB} \parallel \overline{DC}$ in this figure?



- A 26°
- B 59°
- C 69°**
- D 95°

SSM:

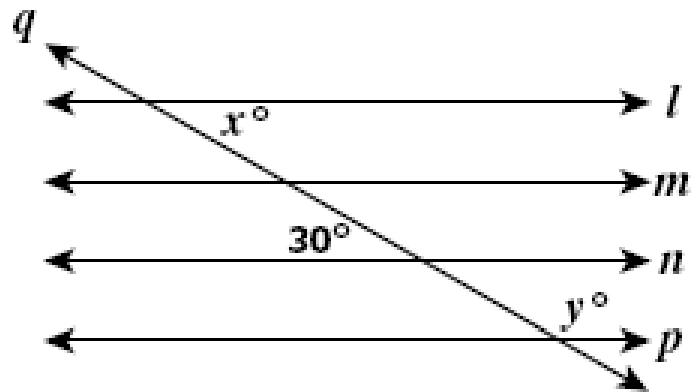
- Eliminate D ($\angle D$ is acute)
- $\angle D > \angle B$, eliminate A

angle A and D are alternate interior angles and must be the same

$$26 + 85 + m\angle A = 180$$

$$m\angle A = 180 - (26 + 85) = 180 - 111 = 69$$

7 In the figure shown, line q is a transversal of parallel lines l , m , n , and p . Lines and Angles



What are the values of x and y ?

- A $x = 30, y = 30$
- B $x = 30, y = 150$**
- C $x = 150, y = 30$
- D $x = 150, y = 150$

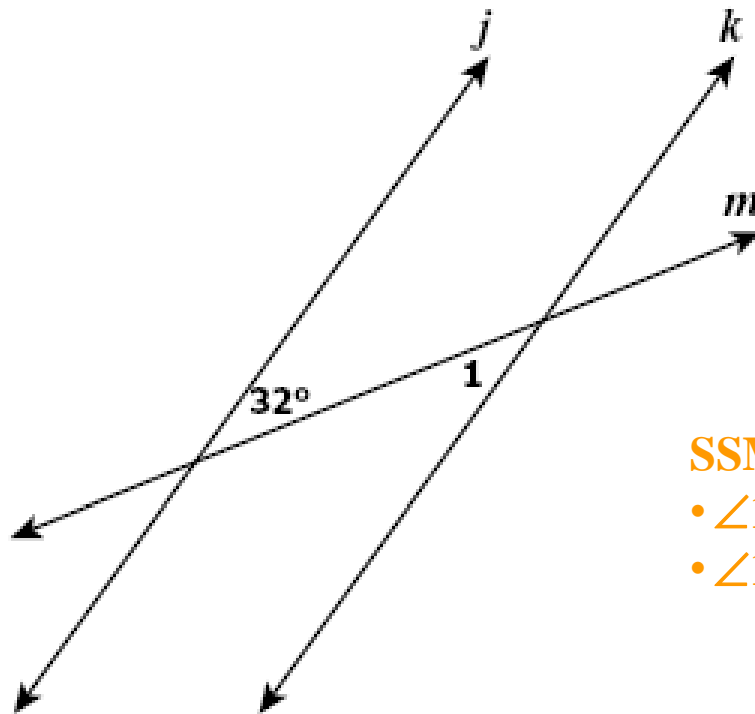
SSM:

- x is acute; eliminate C and D
- y is obtuse; eliminate A and C
- B is only answer left!

x and 30 have to be equal (alternate interior angles between l and n)

y and the vertical angle to 30 are consecutive interior angles; so $30 + y = 180$
and y must be 150

8 In the figure shown, parallel lines j and k are cut by transversal m .



SSM:

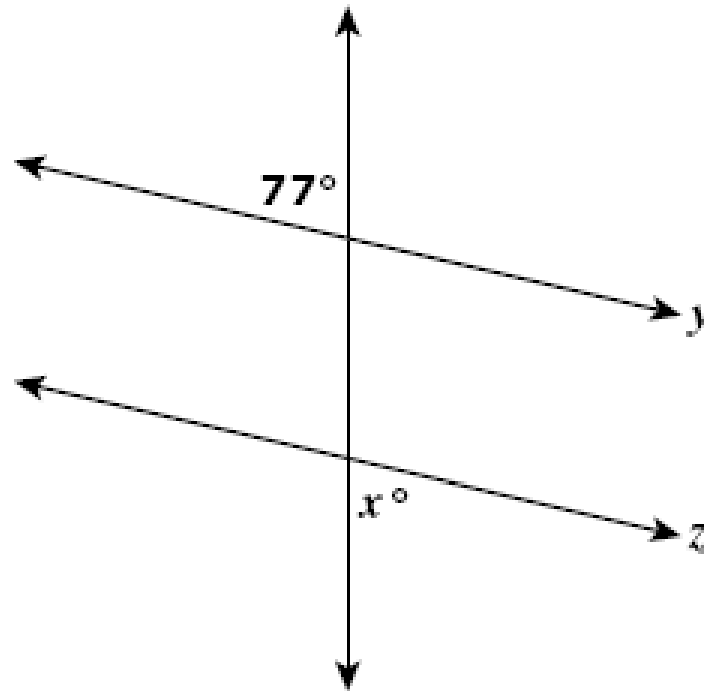
- $\angle 1$ is acute; eliminate H and J
- $\angle 1$ looks same as 32

What is $m\angle 1$?

- F** 32°
- G** 58°
- H** 122°
- J** 148°

**32 and $\angle 1$ are alternate interior angles
and so are equal**

9 Lines y and z are cut by a transversal.



SSM:

- x is acute; eliminate C and D
- x is large acute; eliminate A

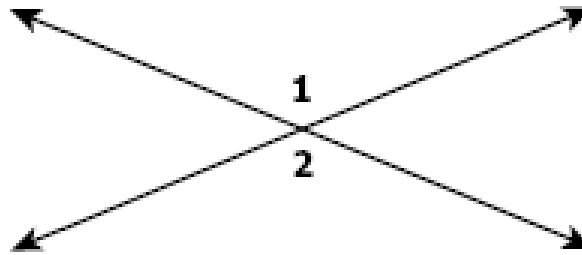
For what value of x is $y \parallel z$?

- A 13
- B 77**
- C 103
- D 154

Parallel lines:

Alternate exterior angles are equal

10 In this figure, $m\angle 1 = (15x - 5)^\circ$ and $m\angle 2 = (10x + 35)^\circ$.



What is $m\angle 1$?

- F 31°
- G 65°
- H 85°
- J 115°**

SSM:

• $\angle 1$ is obtuse; only answer J works

Vertical angles are equal

$$15x - 5 = 10x + 35$$

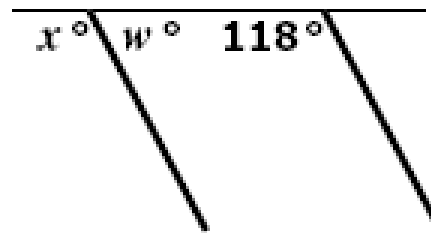
$$5x - 5 = 35$$

$$5x = 40$$

$$x = 8$$

Substitute: $m\angle 1 = 15(8) - 5 = 115$

- 11 This figure represents line segments painted on a parking lot to create parking spaces.



Which equation can be used to show that these line segments are parallel?

- A $118 - w = x$
- B $118 - x = w$
- C $x + 118 = 180$
- D** $w + 118 = 180$

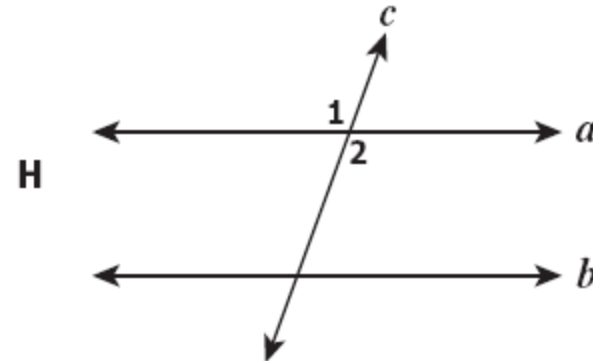
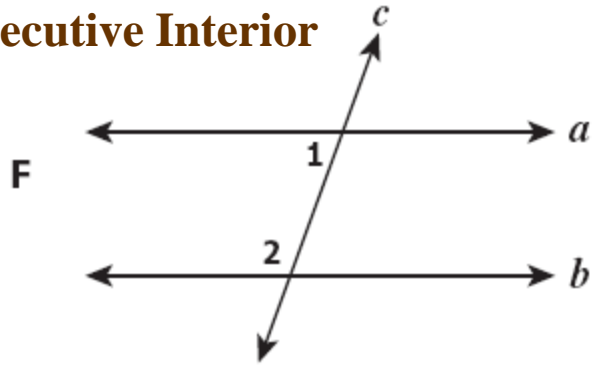
SSM:

- Our eyes tell us that x is obtuse and w is acute
- acute + obtuse = 180 in parallel lines

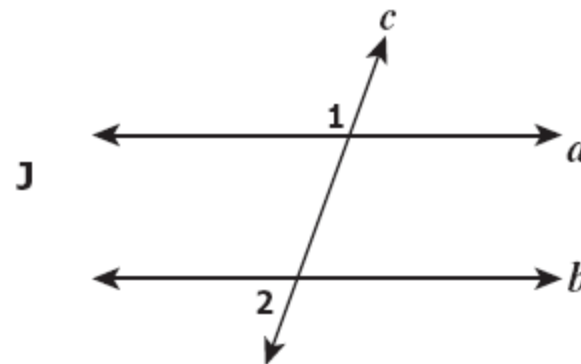
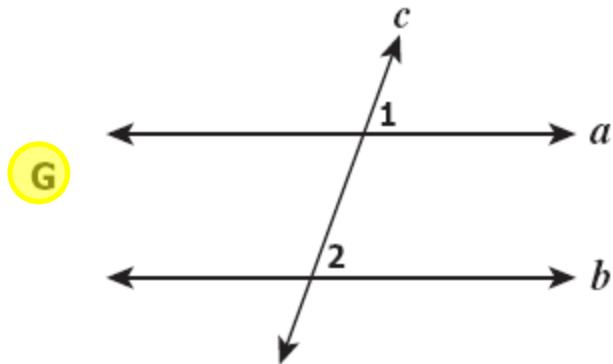
consecutive interior angles are supplementary;
 $w + 118 = 180$

2 In each of the following figures, transversal c cuts lines a and b . In which figure are $\angle 1$ and $\angle 2$ corresponding angles?

Consecutive Interior



Vertical



No name

Corresponding Angles:
 same side of the transversal
 same relationship to other line

SSM:

- Must be same size
- Two different lines involved

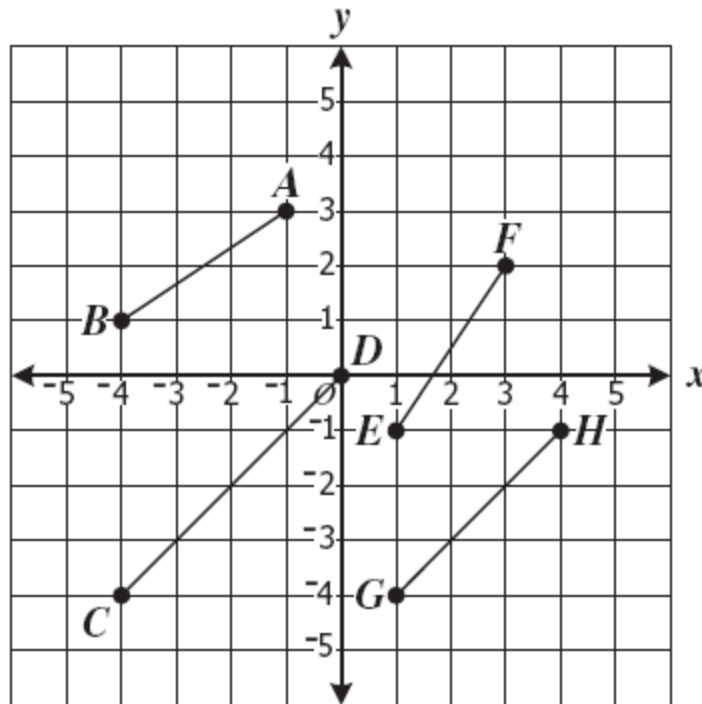
4

$$m_{AB} = 2/3$$

$$m_{CD} = 1$$

$$m_{EF} = 3/2$$

$$m_{AB} = 1$$



SSM:

- Use straight-edge tool to continue lines as far as possible
- Parallel never can cross
EF and AB cross CD
EF crosses GH

Which two segments in the drawing above are most likely parallel?

F \overline{CD} and \overline{GH}

G \overline{CD} and \overline{AB}

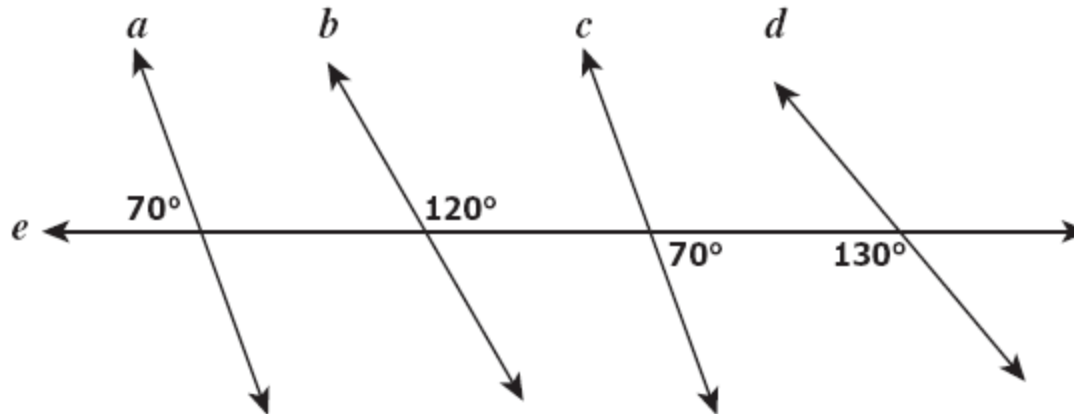
H \overline{AB} and \overline{EF}

J \overline{EF} and \overline{GH}

Parallel: same slopes

calculate slopes: $m = \Delta y / \Delta x$

7 In this figure, transversal e intersects lines a , b , c , and d .



Which lines *must* be parallel?

- A** a and c
- B** b and c
- C** b and d
- D** a and d

SSM:

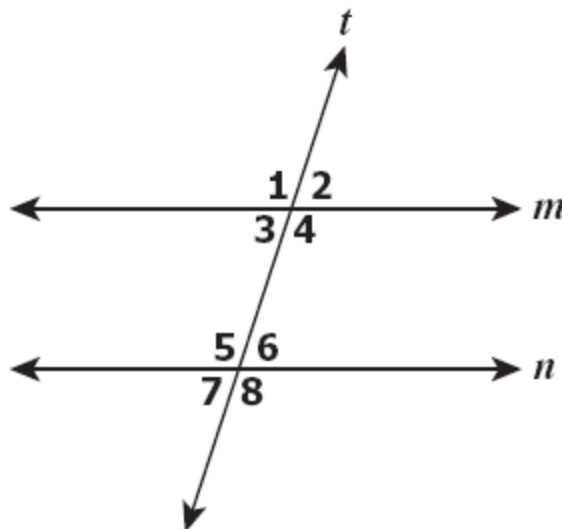
- Use straight-edge tool to continue lines as far as possible
- Parallel never can cross
 b crosses a and c
 d crosses all of them

If lines are parallel, then all acute angles are equal
 and all obtuse angles are equal

Form linear pair combos with given angles

Pick which has same pairs of angles

9 In this figure, line t is a transversal of lines m and n .



SSM:

- Angles must deal with both lines m and n :
angles 1 and 4 deal with m
angles 2 and 7 deal with both
angle 5 is obtuse \rightarrow c is false
angles 6 and 8 deal with n

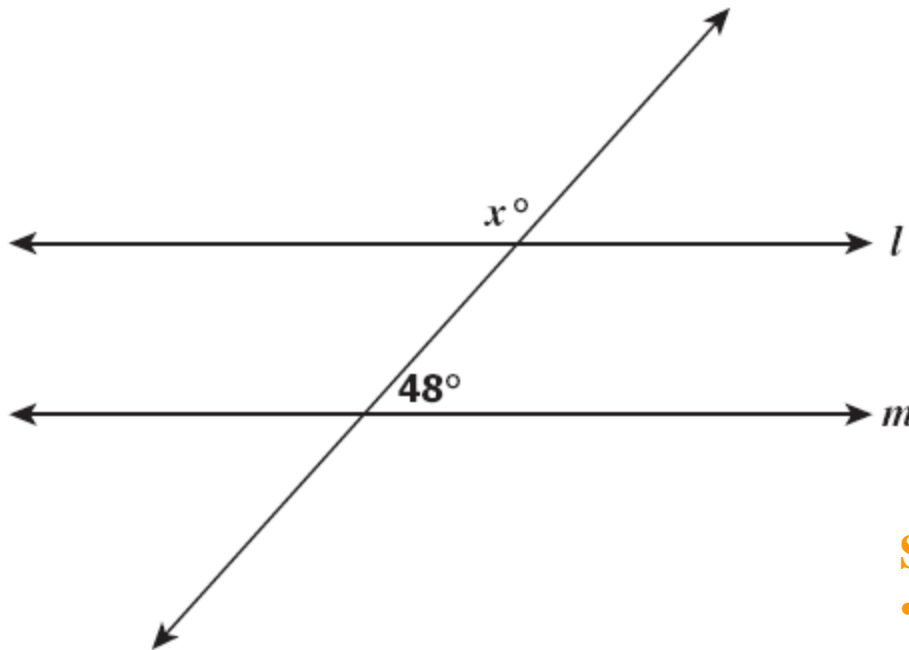
Which of the following statements determines that lines m and n are parallel?

- A $\angle 1 \cong \angle 4$
- B** $\angle 2 \cong \angle 7$
- C $\angle 3$ and $\angle 5$ are complementary
- D $\angle 6$ and $\angle 8$ are supplementary

Parallel lines:

Alternate exterior angles are equal

10 For what value of x is line l parallel to line m in this figure?



SSM:

- x is obtuse (answers F & G are wrong)
- 180 is a magic number

- F 42
G 48
H 132
J 138

Vertical angles are equal

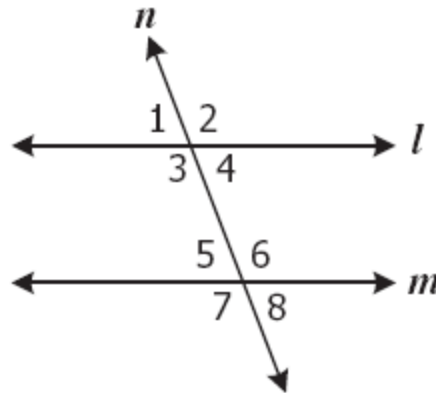
Consecutive interior angles are supplementary

$$48 + x = 180$$

$$x = 180 - 48$$

$$x = 132$$

1 Lines l and m are cut by transversal n .



SSM:

- pair of angles must involve both lines
- only one answer, A, works

Which statement would prove $l \parallel m$?

- A** $m\angle 2 = m\angle 6$
- B** $m\angle 2 = m\angle 3$
- C** $m\angle 7 + m\angle 8 = 180^\circ$
- D** $m\angle 3 + m\angle 5 = 90^\circ$

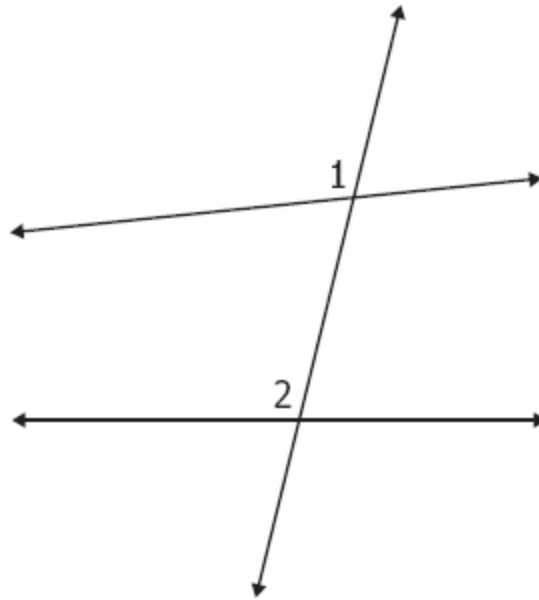
Angles 2 and 6 are corresponding

Angles 2 and 3 are vertical angles (always =)

Angles 7 and 8 are a linear pair (always supplementary)

Angle 3 is obtuse so answer D is wrong

- 3 In this figure, two lines are cut by a transversal. Which type of angles are $\angle 1$ and $\angle 2$?



SSM:

- Eliminate answers

A (vertical angle)

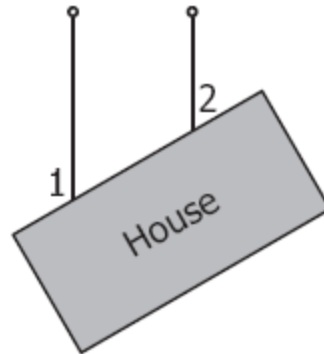
C (both on same side)

D (no such special name)

- A Vertical angles
- B Corresponding angles**
- C Alternate interior angles
- D Same-side interior angles

**Angle 1 and Angle 2 are same side of transversal
and one is interior (2) and one is exterior (1) → Corresponding angles**

- 4 Sally is using strings to mark parallel rows for a vegetable garden behind her house.



SSM:

- Angle 2 is medium acute
eliminate answers F and J

If the measure of $\angle 1$ is 115° , what should be the measure of $\angle 2$?

- F 25°
G 65°
H 75°
J 115°

Angle 2 is an acute angle

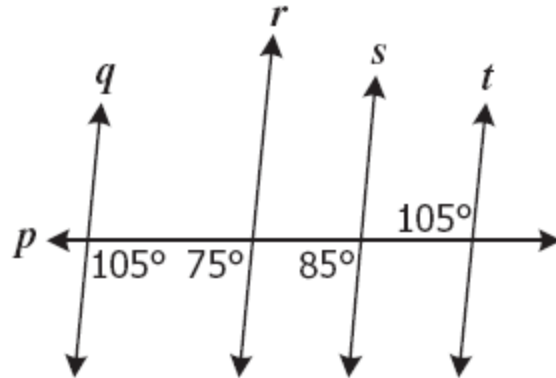
Angle 1 is an obtuse angle

Acute angle and obtuse angle = 180 (magic number!)

$$115 + x = 180$$

$$x = 65$$

5 Line p is a transversal.



SSM:

- Use straight-edge tool to continue lines as far as possible
- Parallel never can cross s eventually will cross either r or t

For lines q , r , s , and t , which is *not* parallel to the other three?

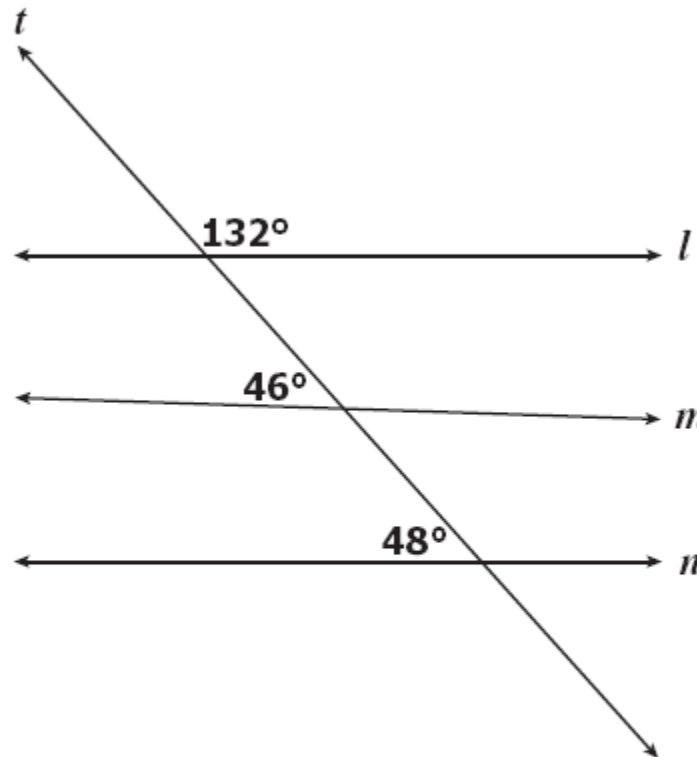
- A q
- B r
- C s**
- D t

If lines are parallel, then all acute angles are equal
and all obtuse angles are equal

Form linear pair combos with given angles

Pick which does not have same pairs of angles

- 6 Lines l , m , and n are intersected by transversal t . The measures of some of the angles that are formed are shown.



SSM:

- Use straight-edge tool to continue lines as far as possible
- Parallel never can cross m eventually will cross both l and n

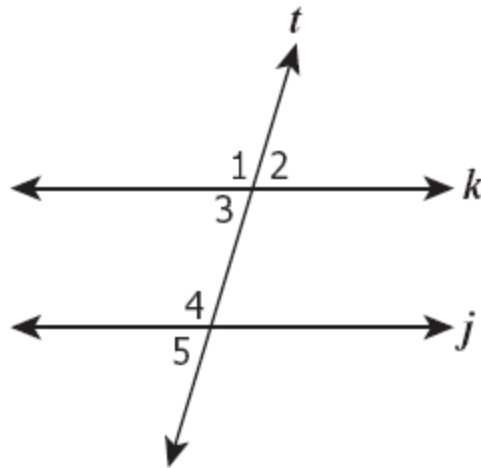
Which of the following statements about lines l , m , and n *must* be true?

- F** $l \parallel m \parallel n$
G $l \parallel m$ only
H $l \parallel n$ only
J $m \parallel n$ only

If lines are parallel, then all acute angles are equal
 and all obtuse angles are equal

Form linear pair combos with given angles
 Pick which has same pairs of angles

7 Transversal t intersects lines k and j as shown.



SSM:

- Must be same size (if \cong)
- Supplementary if one of each
- Two different lines involved

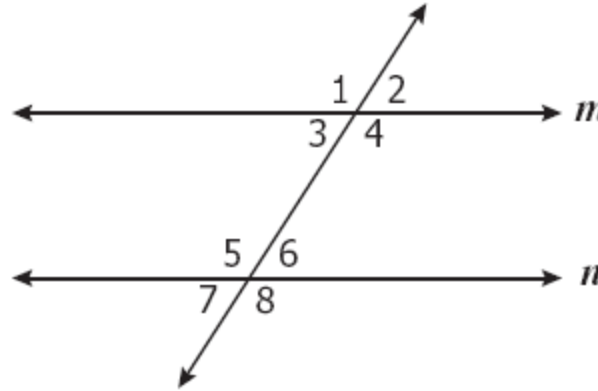
Which of the following relationships makes $j \parallel k$?

- A $\angle 2 \cong \angle 3$
- B $\angle 1 \cong \angle 3$
- C $\angle 4$ and $\angle 5$ are supplementary
- D** $\angle 3$ and $\angle 4$ are supplementary

Eliminate answers:

- A. vertical angles
- B. linear pair
- C. linear pair
- D. consecutive interior angles (supplementary)

11

**SSM:**

- Must be same size (if \cong)
- Two different lines involved

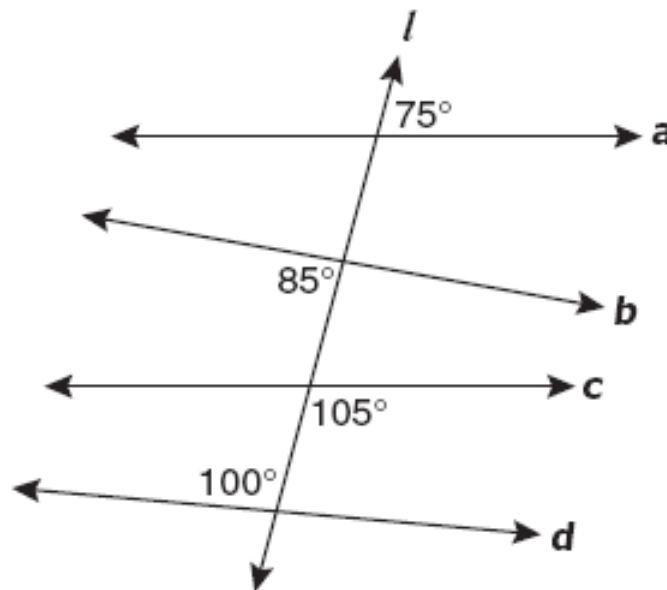
Which statement would *not* prove line m parallel to line n ?

- A** $\angle 7 \cong \angle 6$
- B** $\angle 1 \cong \angle 5$
- C** $\angle 4 \cong \angle 5$
- D** $\angle 3 \cong \angle 6$

Eliminate answers:

- A. vertical angles** (only one line affected)
- B. corresponding angles**
- C. alternate interior angles**
- D. alternate interior angles**

1 Transversal l cuts lines a , b , c , and d .



SSM:

- pair of angles must involve both lines
- only one answer, A, works

Which two lines are parallel?

- A** a and c
- B** a and d
- C** b and c
- D** b and d

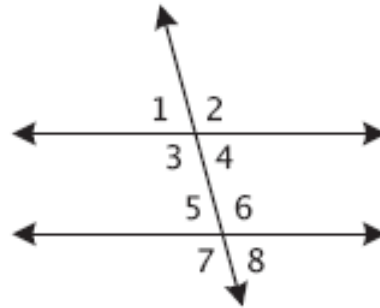
Angles 2 and 6 are corresponding

Angles 2 and 3 are vertical angles (always =)

Angles 7 and 8 are a linear pair (always supplementary)

Angle 3 is obtuse so answer D is wrong

2



In the figure above, $\angle 2$ and $\angle 6$ are a pair of —

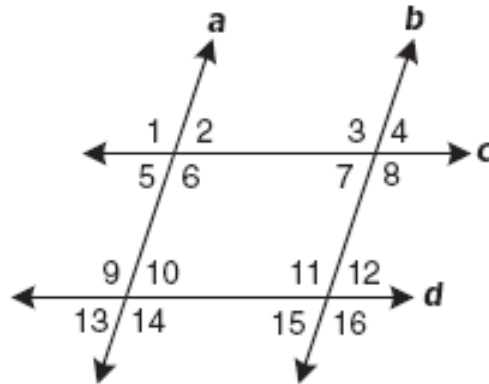
- F consecutive interior angles
- G alternate interior angles
- H vertical angles
- J** corresponding angles

SSM:

- pair of angles involve both lines (eliminates H)
- same side of transversal (eliminates G)
- both obtuse (eliminates F)
- only one answer, J, works

**Angles 2 and 6 are corresponding
same side of the transversal and same side (above) the other line**

4 In this drawing, $a \parallel b$ and $c \parallel d$.



SSM:

- angle 1 is obtuse
- angle 12 is acute

Which angle is *not* necessarily congruent to $\angle 1$?

- F $\angle 3$
- G $\angle 9$
- H $\angle 12$**
- J $\angle 16$

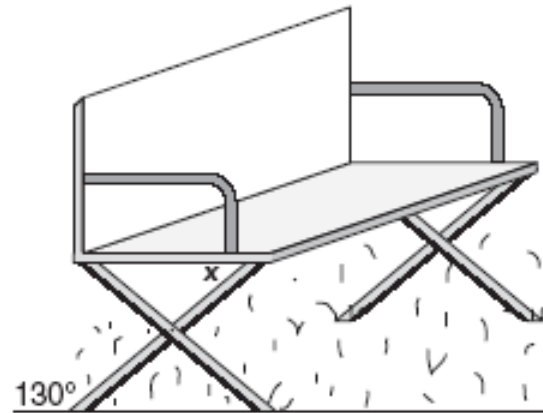
Angles 1, 3, 9, and 16 are obtuse

Angle 12 is acute

Angles 3 and 9 are corresponding

Angle 16 is an alternate exterior angle to Angle 3

- 5 The support legs on a bench are attached in such a way that the angle made by one leg with the ground is 130° .



SSM:

- x is acute
- 180 is magic number
- $180 - 130 = 50$

What must the measure of the angle marked x be in order for the seat of the bench to be parallel to the ground?

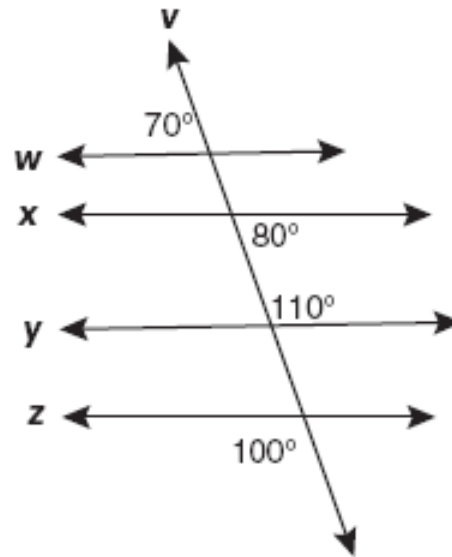
- A** 50°
B 65°
C 90°
D 130°

No special relationship between x and 130 .

Angle x is alternate interior with the angle that forms a linear pair with 130

So $x + 130 = 180$, then $x = 50$

6 Line v is a transversal.



SSM:

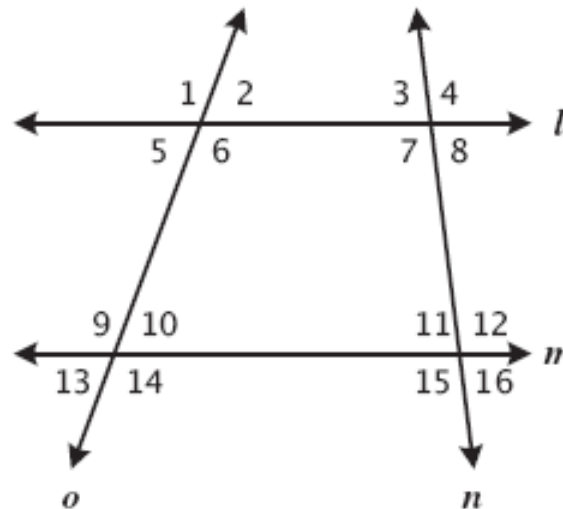
- extend lines as far as possible
- w and x intersect
- y and z intersect

Which is a true statement?

- F** $w \parallel y$ and $x \parallel z$
- G** $w \parallel x$ and $y \parallel z$
- H** $w \parallel z$ and $x \parallel y$
- J** $w \parallel x$ and $x \parallel y$

Make linear pair combinations for each line
 w : 70, 110; x : 80, 100; y : 110, 70; z : 100, 80
 w and y match up and x and z match up

7

**SSM:**

- 4 and 12 are same side of n
- 4 is exterior and 12 is interior
- corresponding

In the drawing above, $\angle 4$ and $\angle 12$ are —

- A alternate interior angles
- B consecutive interior angles
- C** corresponding angles
- D a linear pair

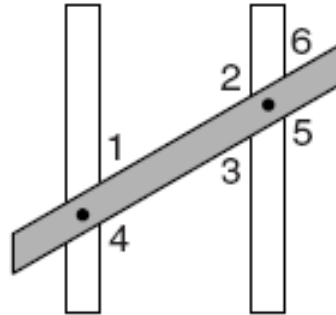
Angles 4 and 12 are corresponding

They are on the same side of n so A is incorrect

Angle 4 is exterior so B is incorrect

They aren't on the same line so D is incorrect

8 A carpenter nailed a board across two beams, forming the angles shown.



Which equal measures would ensure the beams are parallel?

- F $m\angle 1 = m\angle 2$
- G** $m\angle 1 = m\angle 3$
- H $m\angle 2 = m\angle 5$
- J $m\angle 3 = m\angle 4$

SSM:

- pair of angles must involve both lines
- must be same classification
- only one answer, G, works

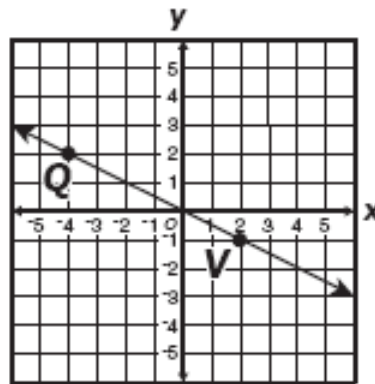
Angles 1 and 2 are consecutive interior (supplementary)

Angles 2 and 5 are vertical angles (always =)

Angles 3 and 4 are consecutive interior (supplementary)

Angles 1 and 3 are alternate interior (equal)

41



SSM:

- falling → negative slope
- less than a one to one change

What is the apparent slope of \overleftrightarrow{QV} ?

A -2

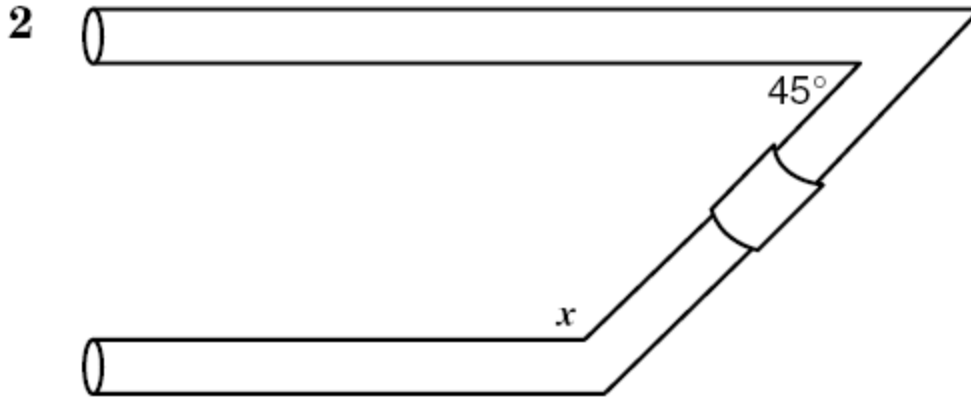
B $-\frac{1}{2}$

C $\frac{1}{2}$

D 2

$$\text{slope} = \Delta y / \Delta x$$

$$\frac{(2 - -1)}{(-4 - 2)} = \frac{3}{-6} = -\frac{1}{2}$$



SSM:

- angle is obtuse
- 180 is “magic” number
- $180 - 45 = 135$

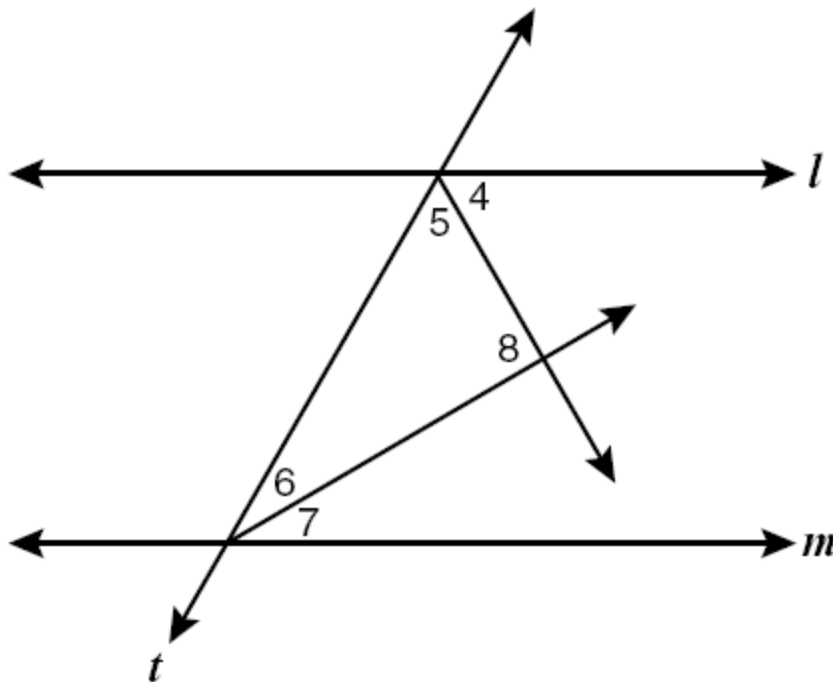
Two parallel sections of pipe are joined with a connecting pipe as shown. What is the value of x ?

- F** 90°
G 115°
H 135°
J 160°

$\angle x$ is a consecutive interior angle with 45
so its supplementary

$$180 - 45 = 135$$

- 3 Parallel lines l and m are cut by transversal t , $m\angle 4 = m\angle 5$, and $m\angle 6 = m\angle 7$.



SSM:

- use corner of scratch paper to check and see if angle is 90

What is the measure of $\angle 8$?

- A 120°
- B 90°**
- C 65°
- D 45°

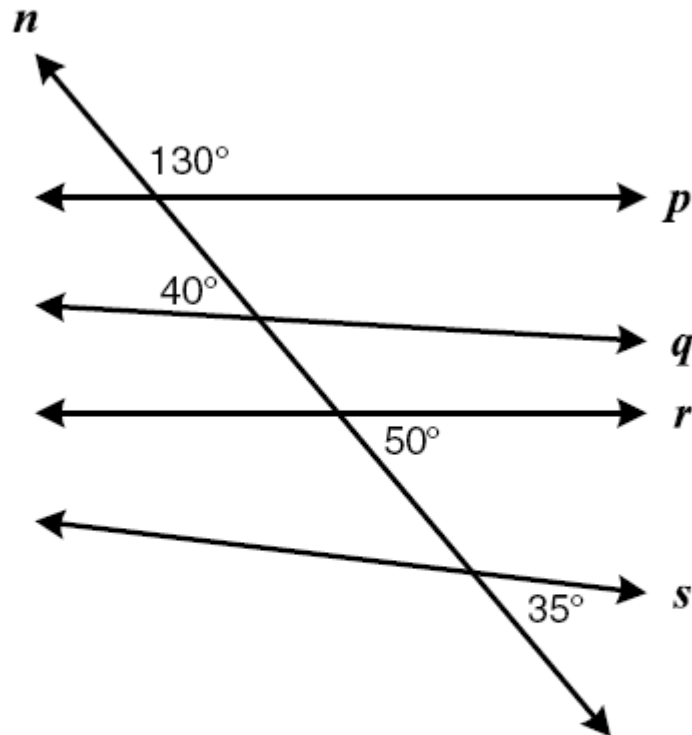
Angles 4 and 5 are equal

Angles 6 and 7 are equal

Together they add to 180 $\rightarrow 2(\angle 5) + 2(\angle 6) = 180$
so angle $5 + 6 = 90$

therefore angle $8 = 90$

- 5 Line n intersects lines p , q , r , and s , forming the indicated angles.



SSM:

- extend lines using ruler
- p and q intersect
- q and r intersect
- r and s intersect

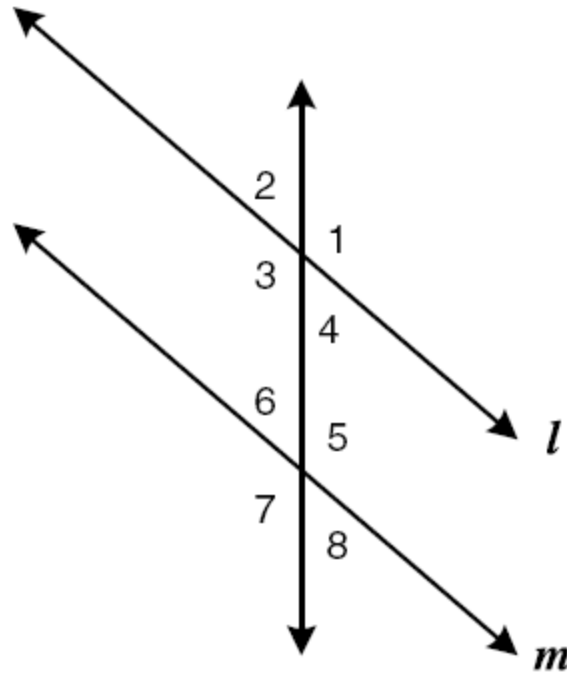
Which two lines are parallel?

- A p and q
- B** p and r
- C q and r
- D r and s

form linear pair numbers for each line

lines with same numbers are parallel

6

**SSM:**

- angles must be with both lines
 - angles must be same size
- F, G, H are wrong**

Which will prove that line l is parallel to line m ?

F $\angle 2 \cong \angle 7$

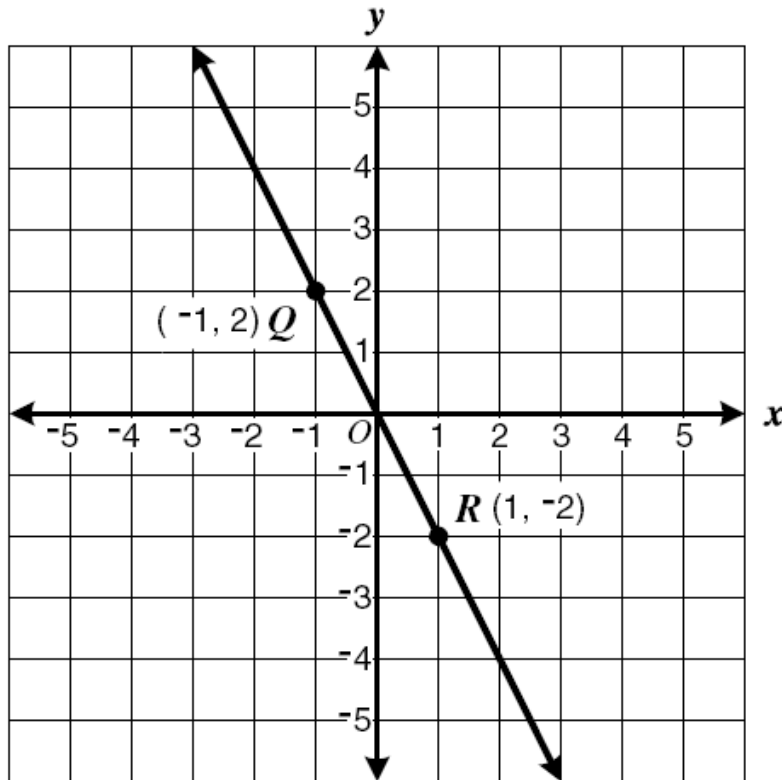
G $\angle 3 \cong \angle 6$

H $\angle 5 \cong \angle 2$

J $\angle 7 \cong \angle 1$

Angles 1 and 7 are alternate exterior angles

7



Which two points determine a line
parallel to \overleftrightarrow{QR} ?

- A** (1, 1) and (2, -1)
- B** (-1, -1) and (-2, -3)
- C** (1, 4) and (5, 2)
- D** (2, 1) and (-2, -1)

SSM:

- plot points and draw the lines connecting them

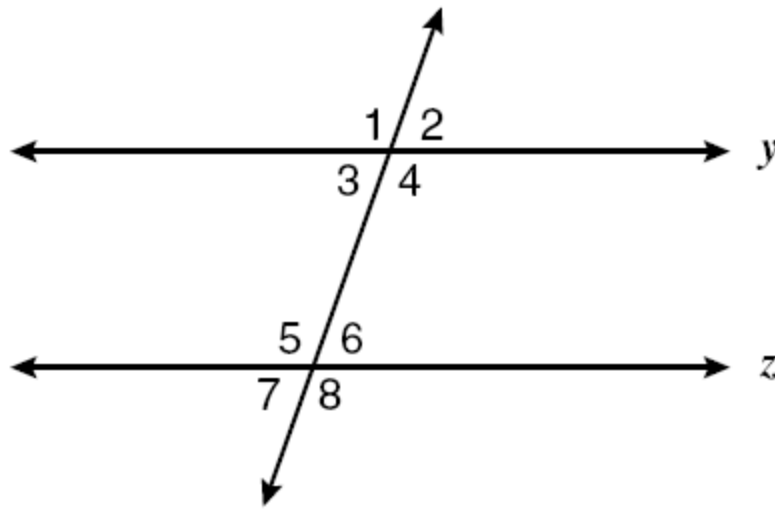
$$\text{slope, } m = \frac{y_2 - y_1}{x_2 - x_1}$$

Slope of QR is -2

Slopes of B and D are positive

Slope of C is -1/2

8 Given: $m\angle 1 = 110^\circ$



SSM:

- parallel lines say only one obtuse angle measurement and only one acute angle measurement
- angle 7 is acute

Which must be true if $y \parallel z$?

F $m\angle 8 = 100^\circ$

G $m\angle 7 = 110^\circ$

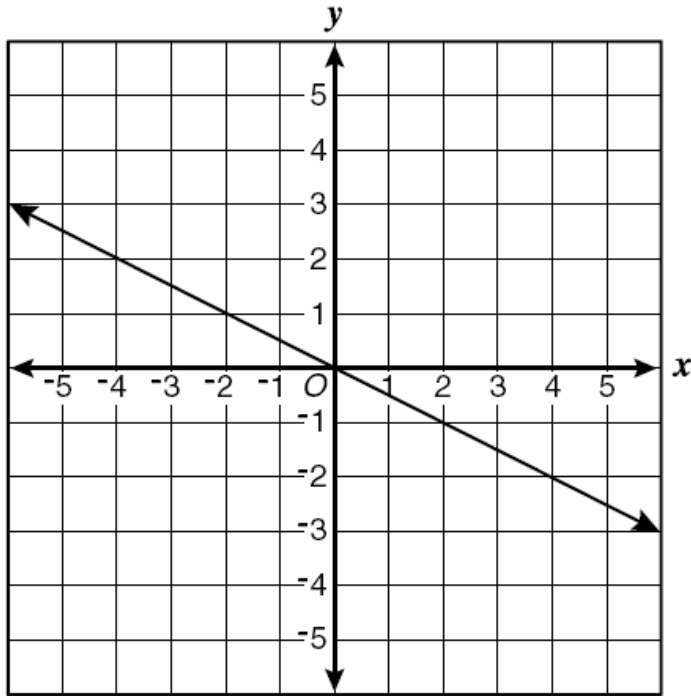
H $m\angle 6 = 80^\circ$

J $m\angle 5 = 110^\circ$

Angles 1 and 8 are alternate exterior angles, but are not equal

Angles 1 and 5 are corresponding angles and have equal measures!

42



SSM:

• falling → slope is negative

What is most likely the slope of the line graphed above?

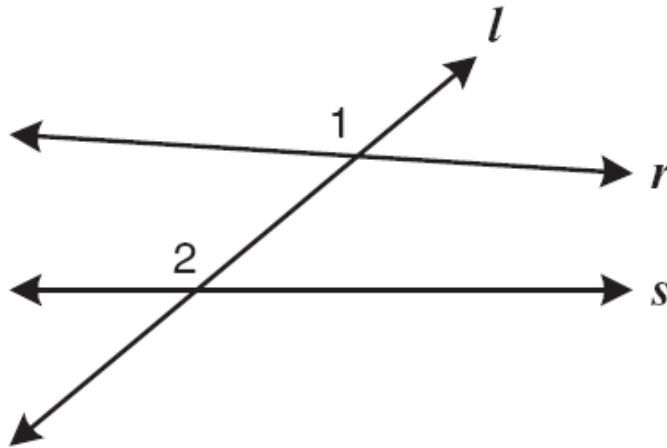
F -1

☒ G $-\frac{1}{2}$
H $\frac{1}{2}$

J 1

$$\bullet \text{ Slope, } m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - -2}{0 - 4} = \frac{2}{-4} = -1/2$$

- 2 The figure shows line l intersecting lines r and s .



SSM:

- same side of common line (alternates - wrong)
- one between and one outside (consecutive interior angles – wrong)

In the figure, $\angle 1$ and $\angle 2$ are —

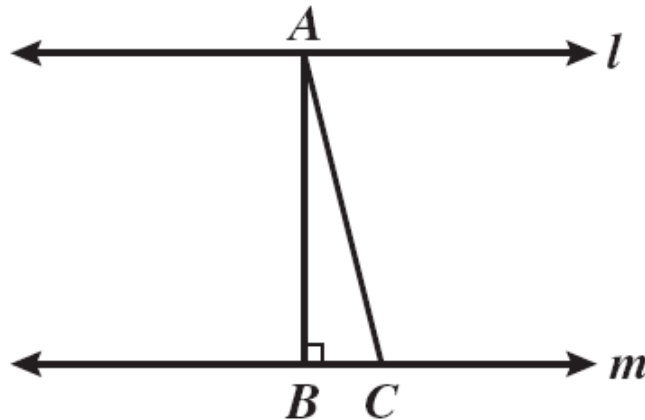
- F alternate interior angles
- G alternate exterior angles
- H** corresponding angles
- J consecutive interior angles

Angles are on the same side of transversal

One is interior (2) and one is exterior (1)

Corresponding angles

5

**SSM:**

- Use your eyes and scrap paper corner!
- two perpendiculars \rightarrow parallel

Which statement would be sufficient to prove that line l is parallel to line m ?

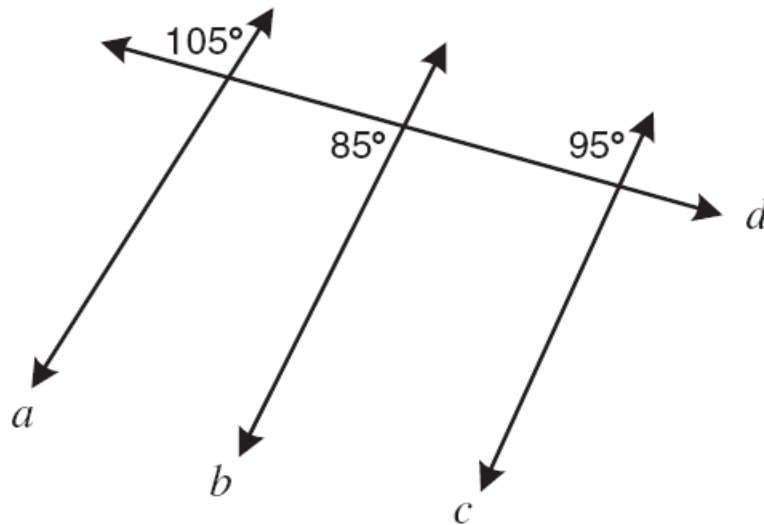
- A $\overline{AC} \perp m$
- B $\overline{AB} \perp l$**
- C $\overline{AC} \perp l$
- D $\overline{AB} \perp \overline{AC}$

angle B is 90

angle A + B = 180, so angle A = 90

AB must be perpendicular to line l

- 6 In this diagram, line d cuts three lines to form the angles shown.



SSM:

- extend lines using line drawing tool as far as possible

Which two lines are parallel?

F a and b

G a and c

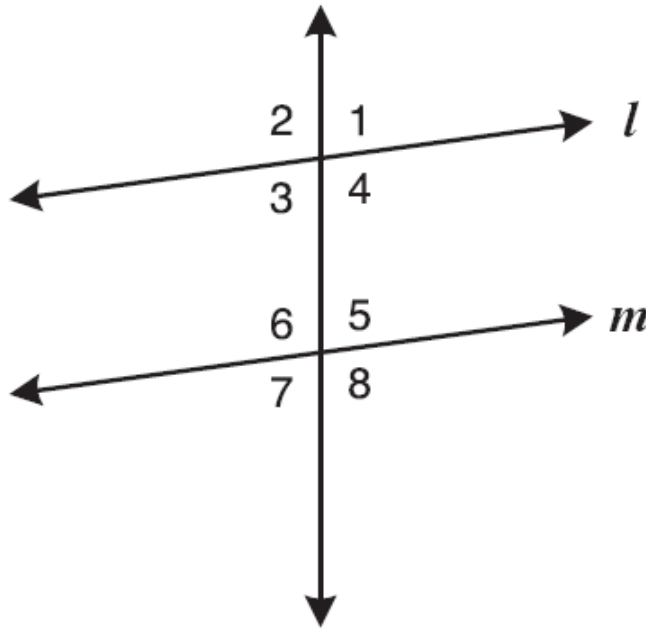
H b and c

J No lines are parallel.

Form linear pairs with given numbers

If any are the same numbers, then they are parallel

8

**SSM:**

- must involve both lines
- must be the same size

Which condition will guarantee that line l is parallel to line m ?

F $\angle 1 \cong \angle 3$

G $\angle 1 \cong \angle 6$

H $\angle 6 \cong \angle 5$

J $\angle 3 \cong \angle 5$

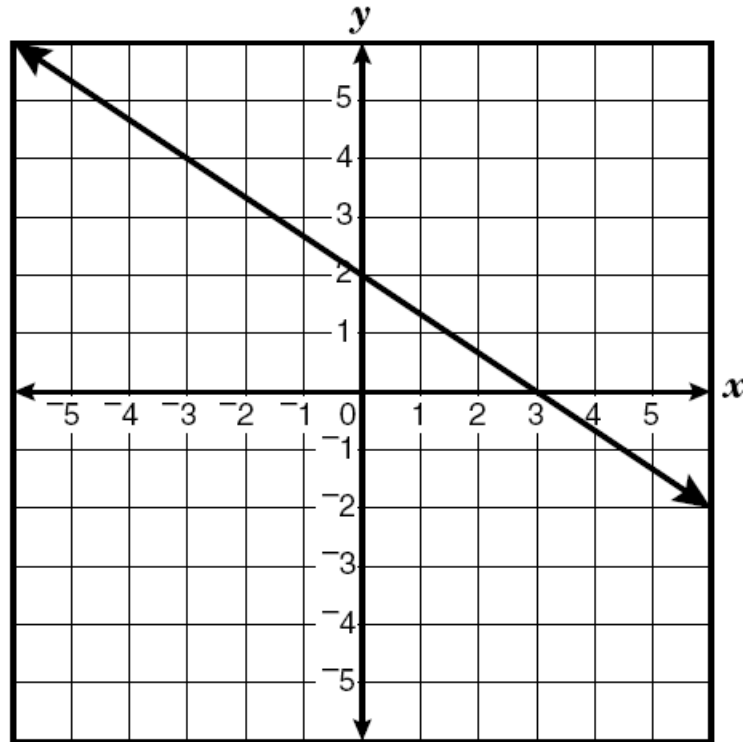
Angles 1 and 3 are vertical angles

Angles 1 and 6 are different sizes

Angles 6 and 5 are linear pairs

Angles 3 and 5 are alternate interior

44



Which is most likely the slope of the line graphed?

F -4

H $-\frac{2}{3}$

G $-\frac{3}{2}$

J 4

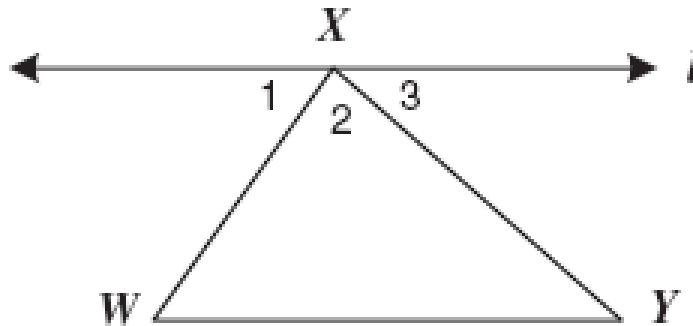
SSM:

- falling → negative slope
- less than a one to one change

$$\text{slope} = \Delta y / \Delta x$$

$$\frac{(2 - 0)}{(0 - 3)} = \frac{2}{-3} = -\frac{2}{3}$$

2



SSM:

• looking H doesn't look true

If $\angle 3 \cong \angle Y$, which of the following must be true?

F $\angle W \cong \angle Y$

G \overline{WX} is perpendicular to \overline{XY}

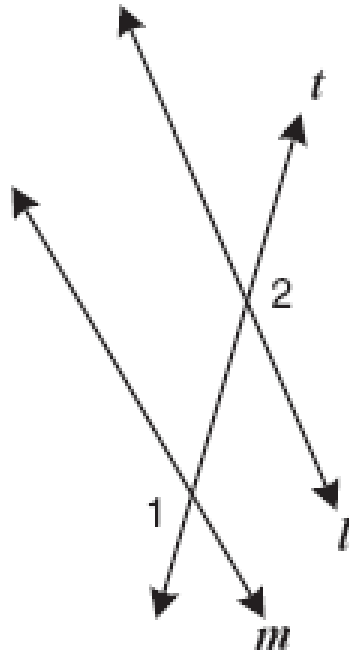
H $\angle W \cong \angle 2$

J Line l is parallel to \overline{YW}

angle 3 and angle y are alternate interior angles

so WY is parallel to line l

- 4 In the figure, line t is a transversal for lines l and m .



SSM:

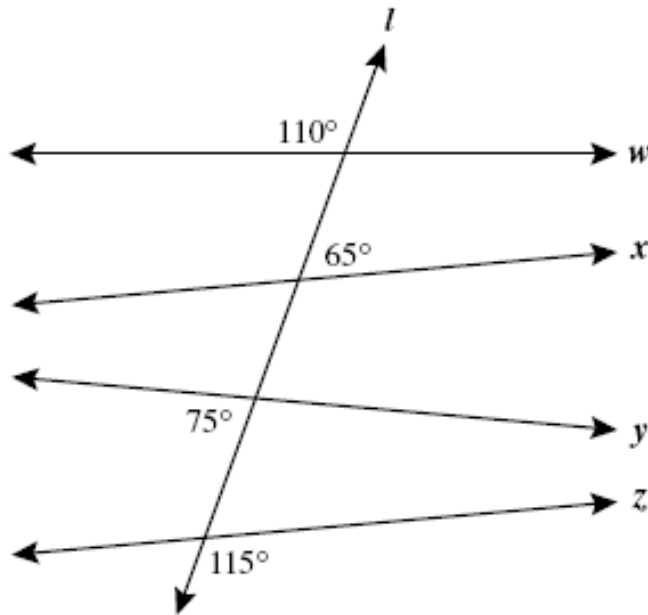
- opposite sides of t
- not between l and m

Which of the following best describes the relationship between $\angle 1$ and $\angle 2$?

- F Alternate interior angles
- G Consecutive interior angles
- H Corresponding angles
- J** Alternate exterior angles

opposite sides \rightarrow alternate
both outside \rightarrow exterior

- 5 Line l intersects lines w , x , y , and z , forming angles with measures as indicated on the drawing.



SSM:

- form linear pair numbers
- which are the same

Which two lines are parallel?

- A w and x
- B x and z**
- C y and z
- D w and y

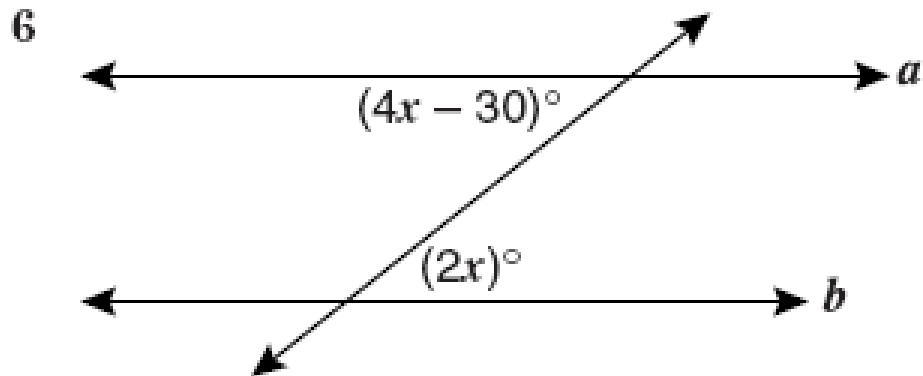
110, 70 for w

115, 65 for x

75, 105 for y

65, 115 for z

so x and z have the same and are parallel



SSM:

- angle is medium acute
- plug in answers to see which fit
- F too small, J too big

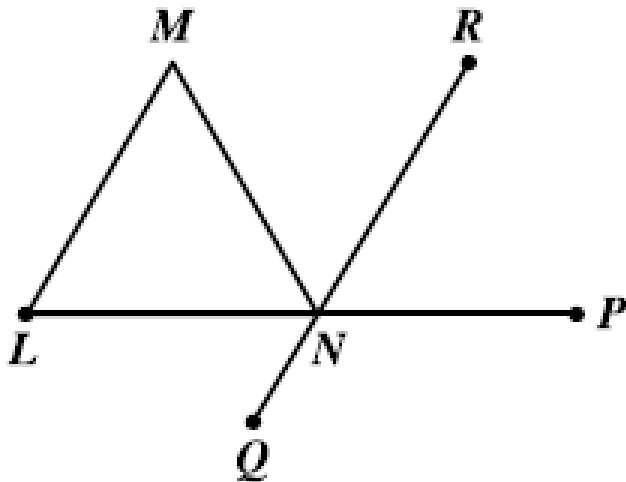
Which value for x will make a parallel to b ?

- F 5
G 15
H 20
J 35

alternate interior angles

$$\begin{aligned}4x - 30 &= 2x \\4x &= 2x + 30 \\2x &= 30 \\x &= 15\end{aligned}$$

- 7 In the figure drawn below, \overleftrightarrow{LM} and \overleftrightarrow{QR} are parallel and $m\angle M = m\angle L = 60^\circ$.



SSM:

- angle is obtuse

A and D are wrong

What is $m\angle QNP$?

- A 90°
- B 120°**
- C 150°
- D 180°

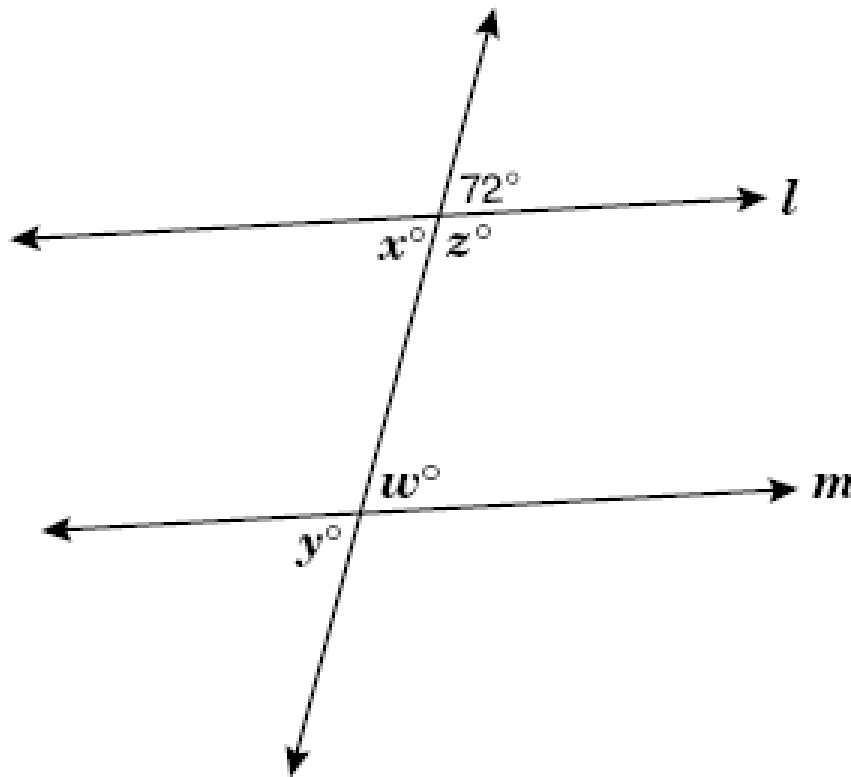
angle L and angle RNP are corresponding angles

angle RNP + angle QNP = 180 (linear pair)

$$60 + x = 180$$

$$x = 120$$

8

**SSM:**

- $x = 72$ vertical angles
- if $w = 72$ then parallel

Which additional piece of information would verify $l \parallel m$?

F $x = 72$

G $y = w$

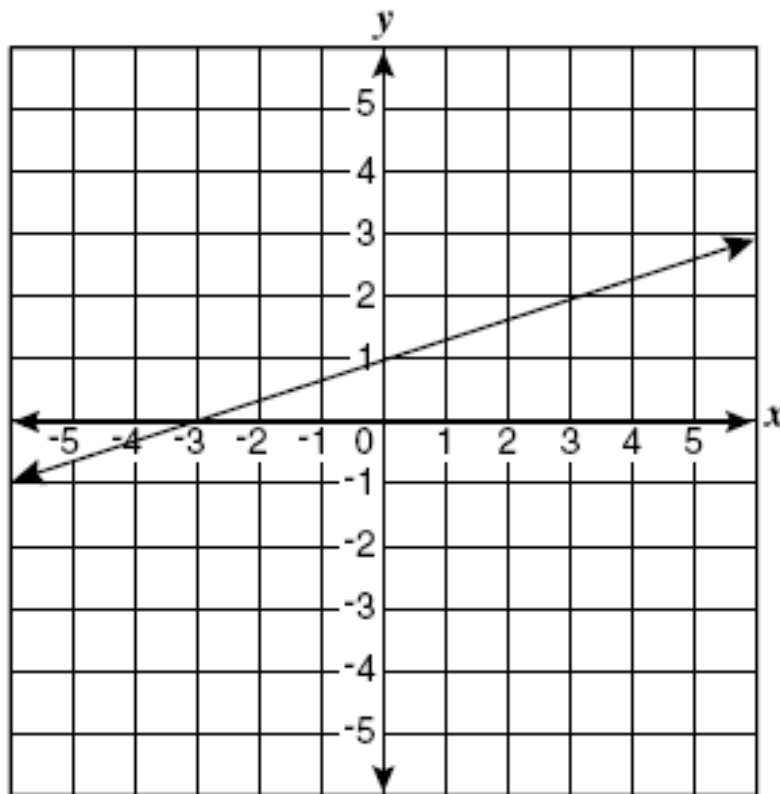
H $z = 108$

J $x = w$

opposite sides \rightarrow alternate
both inside \rightarrow interior

x and w are alternate interior angles

42



What is most likely the slope of the line graphed above?

F $\frac{1}{3}$

H 2

G $\frac{2}{3}$

J 3

SSM:

- positive slope (increasing)
- compare to $y = x$ (graph it)
- slope is less than 1

slope = $\Delta y / \Delta x$

$$\frac{(1 - 0)}{(0 - -3)} = \frac{1}{3}$$

6 Line m contains points $(1, -3)$ and $(2, 2)$. Which of the following pairs of points define a line parallel to line m ?

F $(0, 0)$ and $(-1, 1)$

G $(0, 0)$ and $(1, 5)$

H $(1, 1)$ and $(6, 2)$

J $(-4, 0)$ and $(5, 5)$

SSM:

• graph all points involved on graph paper and draw lines

parallel lines have equal slopes (slope = change in y / change in x)

slope of line m is $(-3 - 2) / (1 - 2) = (-5) / (-1) = 5$

figure slopes for each answer

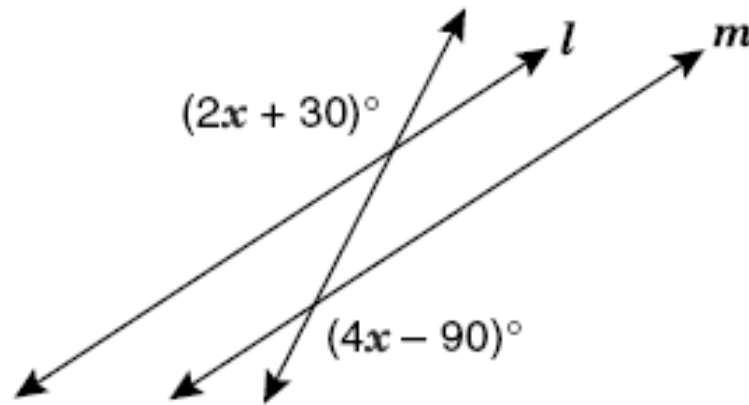
F slope = -1

G slope = 5

H slope = $1/5$

J slope = $5/9$

7

**SSM:**

- angles are both obtuse
- plug in answers to see which are equal

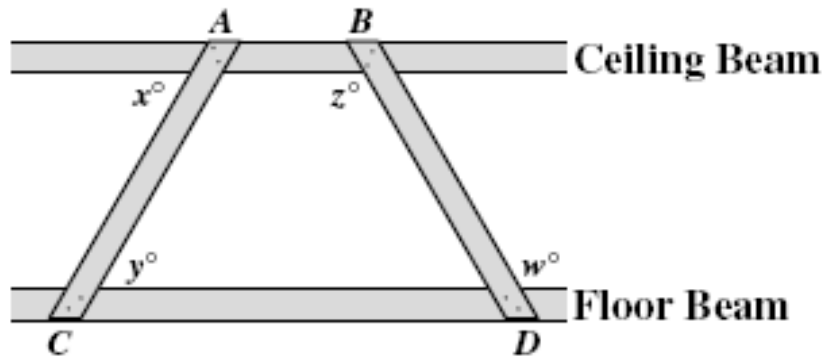
What value for x will show that lines l and m are parallel?

- A 25
- B 30
- C 40
- D 60**

Alternate exterior angles

$$\begin{aligned}2x + 30 &= 4x - 90 \\2x + 120 &= 4x \\120 &= 2x \\60 &= x\end{aligned}$$

8



SSM:

- look at picture and see which angles could be equal (by sight)

A construction engineer needs to make sure a ceiling beam is parallel to its corresponding floor beam. Using the drawing as a guide, which pair of measurements is sufficient to show the beams are parallel?

F $x = z$

G $y = w$

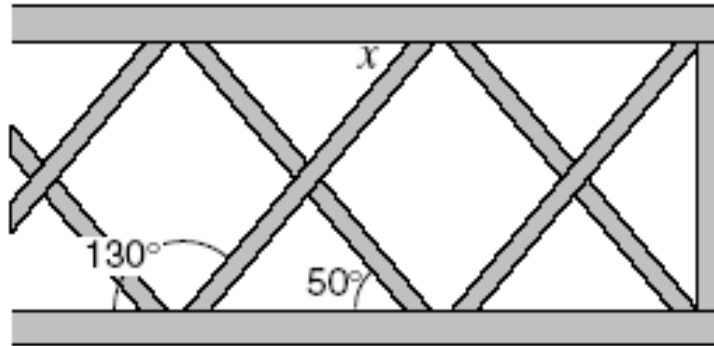
H $x = y$

J $y = z$

angles x and y form alternate interior angles

if they are equal then the beams are parallel

- 2 George used a decorative fencing to enclose his deck.



SSM:

- **x is an acute angle**

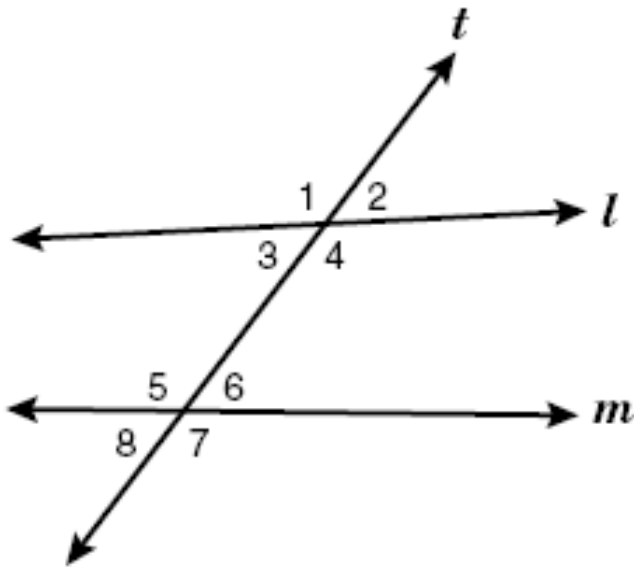
Using the information on the diagram and assuming the top and bottom are parallel, the measure of $\angle x$ is —

- F** 50°
- G 80°
- H 100°
- J 130°

In parallel construction, all acute angles are equal and all obtuse angles are equal

so since x is acute it must be 50

- 4 In the figure, lines l and m are cut by the transversal t forming the angles shown.



SSM:

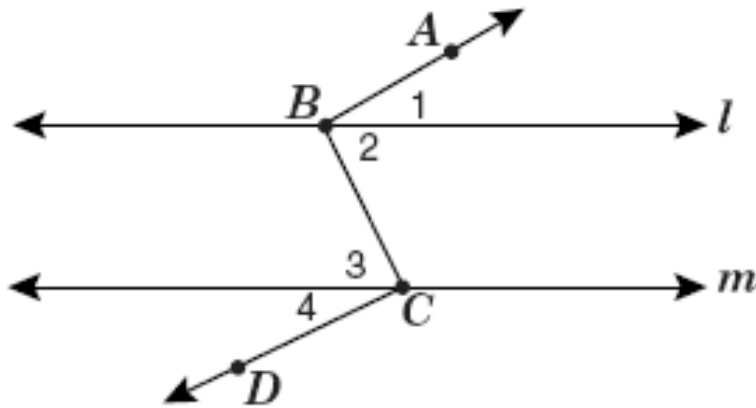
- opposite sides of t
- both inside of l and m

$\angle 3$ and $\angle 6$ are —

- F Vertical angles
- G Corresponding angles
- H** Alternate interior angles
- J Alternate exterior angles

Alternate Interior angles \rightarrow both inside of l and m and on opposite sides of the transversal t

5 Use this figure to answer the following.



SSM:

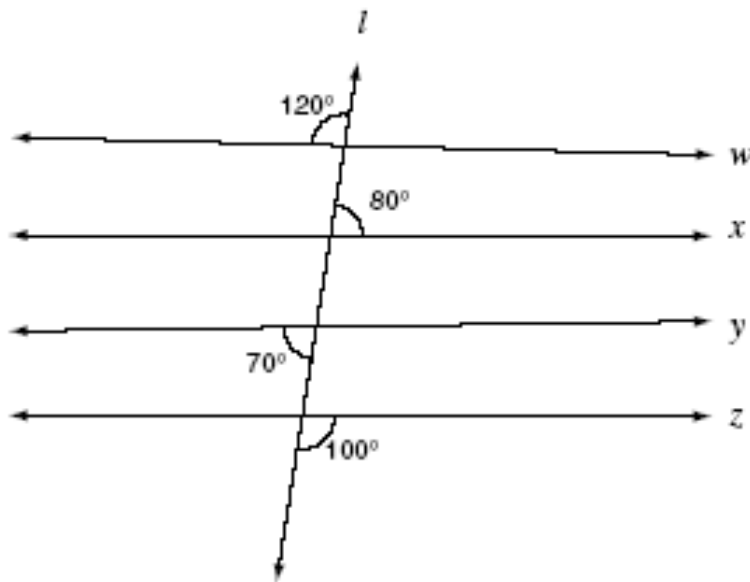
- have to involve both rays
- answers A, B and C do not

\overrightarrow{BA} is parallel to \overrightarrow{CD} if —

- A $m\angle 1 = m\angle 2$
- B $m\angle 3 = m\angle 4$
- C $m\angle 1 + m\angle 2 = 90$
- D** $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4$

angles 1 and 2 combined and angles 3 and 4 combined form alternate interior angles; so answer D is correct

6

**SSM:**

- extend lines as far as possible
- see which intersect

Line l intersects lines w , x , y , and z .
Which two lines are parallel?

F Line w and line x

G Line w and line y

H Line x and line z

J Line y and line z

form linear pair combinations

compare to see which ones are the same

w: 120, 60

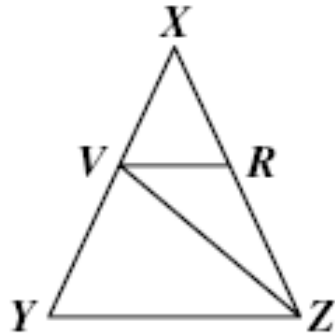
x: 80, 100

y: 70, 110

x: 100, 80

x and z

- 7 The measure of $\angle YZV$ is 40° and the measure of $\angle XYZ$ is 65° .



SSM:

- looking for an angle involving VR
- and one that's acute

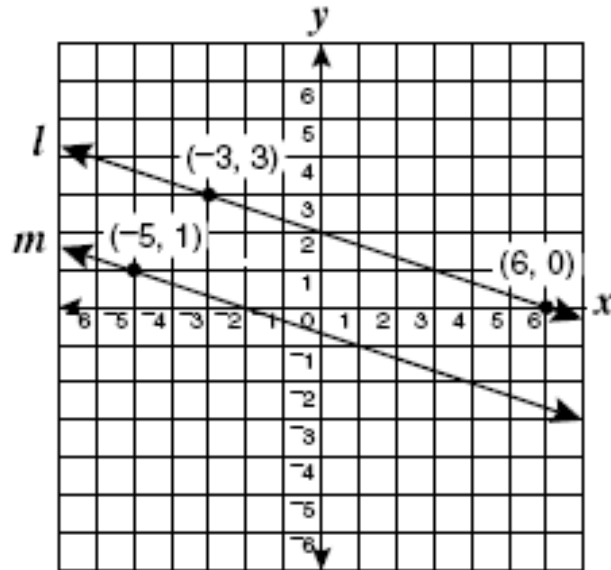
Which of these angles *must* measure 40° in order for \overline{VR} to be parallel to \overline{YZ} ?

- A $\angle YVZ$
- B $\angle ZVR$**
- C $\angle ZYV$
- D $\angle VRX$

angle ZVR is an alternate interior angle to $\angle YZV$

if they are equal, then line segments are parallel

- 8 Lines l and m contain the points shown.



SSM:

- plot each point on graph and see which is on the line

slopes must be the same

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \text{slope}$$

slope of l is $-1/3$

use each answer to figure slope

F: $-3/5$

G: $-2/5$

H: $-1/3$

J: $-2/9$

Which of the following points *must* lie on line m in order for lines l and m to be parallel?

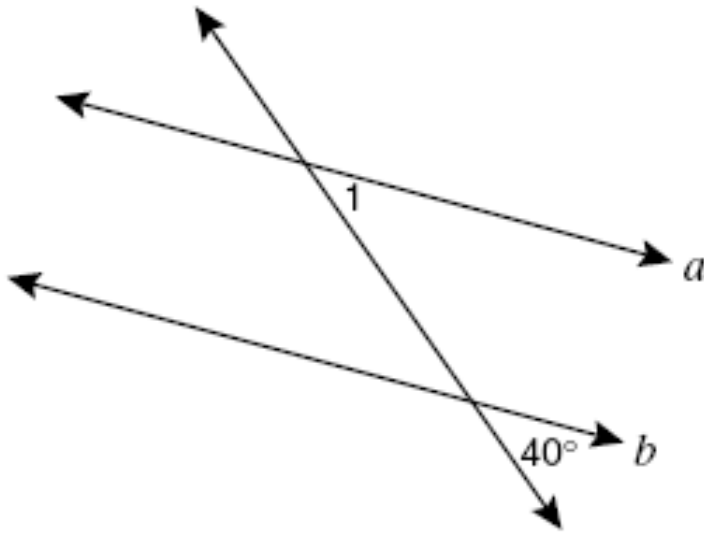
F $(0, -2)$

G $(0, -1)$

H $(1, -1)$

J $(4, -1)$

1

**SSM:**

- angle 1 is acute
eliminates C and D

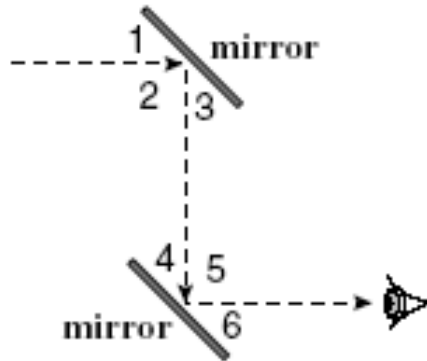
If line a is parallel to line b , what is $m\angle 1$?

- A** 40°
- B 50°
- C 90°
- D 140°

Angles 1 and the 40° angle are corresponding angles

If lines are parallel, then corresponding angles are equal

4

**SSM:**

- angle 6 is medium acute
- compare with folded corner of scrap paper, looks equal to 45

This diagram shows how a periscope works. If the two mirrors are parallel and $\angle 1 \cong \angle 3$, what is $m\angle 6$ when $m\angle 2 = 90^\circ$?

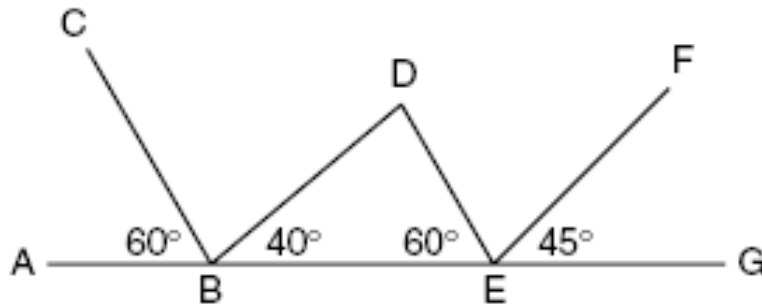
- F 30°
G 45°
 H 50°
 J 60°

Angles 1, 2 and 3 have to add to 180 and if angle 1 and 3 are equal and angle 2 equal 90, then angles 1 and 3 have to equal 45

Since the mirrors are parallel then angle 3 and 4 are alternate interior angles and equal (45)

Angle 5 equals 90, so angle 6 equals 45

6

**SSM:**

- parallel lines have all acute angles the same and all obtuse angles the same

Using the information on the diagram,
which is true?

F $\overline{BD} \parallel \overline{EF}$

G $\overline{BD} \parallel \overline{DE}$

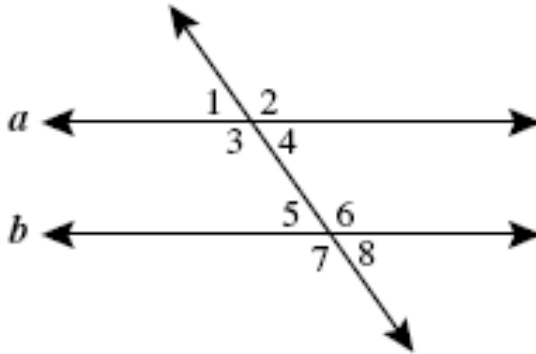
H $\overline{CB} \parallel \overline{BD}$

J $\overline{CB} \parallel \overline{DE}$

angles ABC and angle BED are corresponding and equal

so CB is parallel to DE

7

**SSM:**

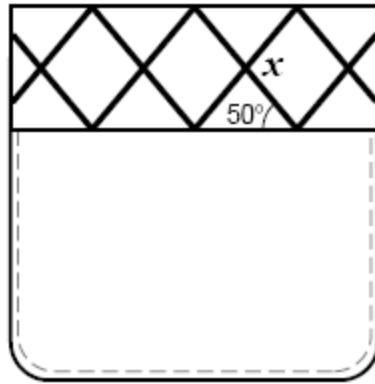
- have to involve both lines
- answers A and D do not
- have to look the same
- answer B does not work

Line a is parallel to line b if —

- A $m\angle 4 = m\angle 2$
- B $m\angle 3 = m\angle 5$
- C** $m\angle 4 = m\angle 5$
- D $m\angle 3 = m\angle 2$

angles 4 and 5 are alternate interior angles and must be equal

1

**SSM:**

- angle x is obtuse
eliminates A and B

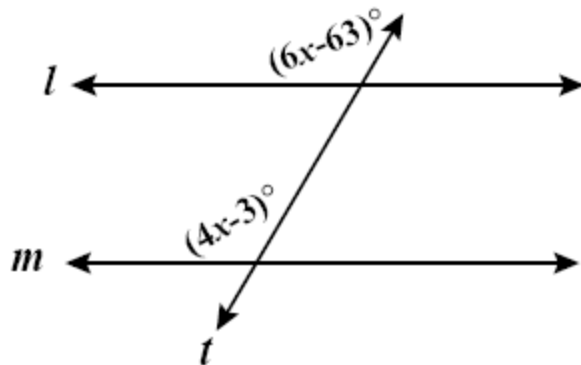
A design made with parallel lines is sewn on a pocket of a shirt as shown. What is the value of x ?

- A 50°
- B 80°
- C 100°
- D 130°**

In parallel lines the acute angles and obtuse angles are always supplementary

$$\text{So } 180 - 50 = 130 = x$$

6

**SSM:**

- angles are obtuse
- plug in answers to see which works

Line l is parallel to line m when the value of x is —

- F 3
G 12
H 30
J 38

Parallel lines \rightarrow Angles are equal

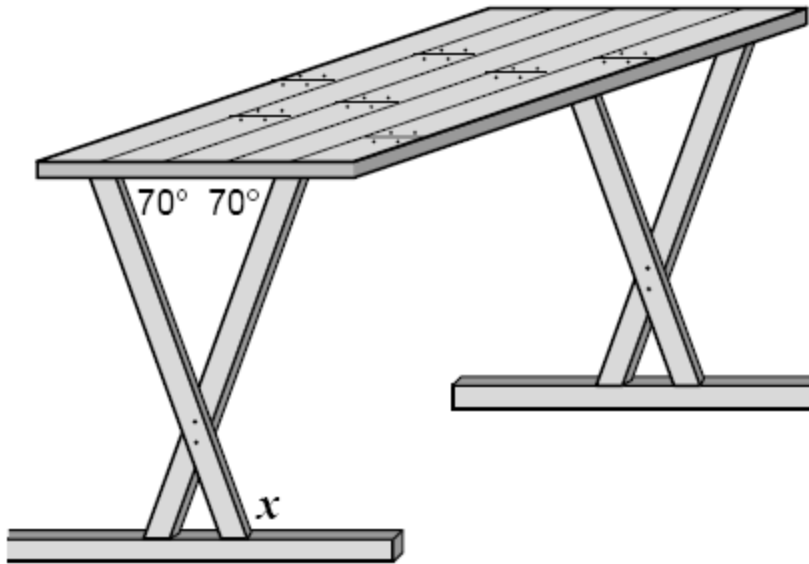
$$6x - 63 = 4x - 3$$

$$6x = 4x + 60$$

$$2x = 60$$

$$x = 30$$

7

**SSM:**

- angle x is obtuse
eliminates A , B and C

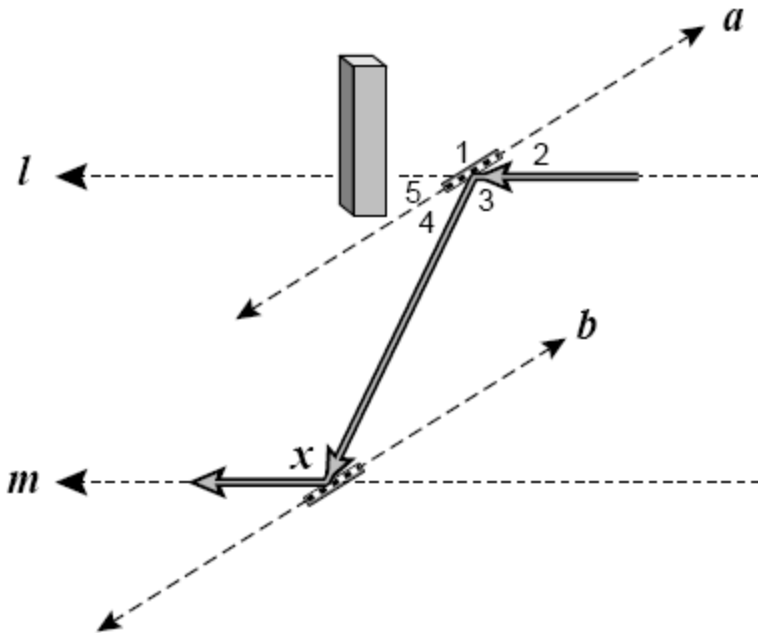
The diagram shows a table being constructed. If the leg piece forms a 70° angle with the top of the table, what must be the value of x so that the top of the table is parallel to the floor?

- A 40°
- B 70°
- C 90°
- D 110°**

In parallel lines the acute angles and obtuse angles are always supplementary

$$\text{So } 180 - 70 = 110 = x$$

- 8 This drawing shows an apparatus designed to divert light rays around an obstacle.



SSM:

- angle x is obtuse
eliminates F and G

Lines a and b are parallel and angles 2 and 4 each measure 32° . If lines l and m need to be parallel, what must be the value of x ?

- F 32°
G 64°
H 116°
J 148°

In parallel lines the obtuse angles (3 and x) are equal and angles 2, 3, and 4 form a line

$$\text{So } 180 - 2(32) = 180 - 64 = 116 = x$$

40 What is the slope of the line through $(-2, 3)$ and $(1, 1)$?

F $-\frac{3}{2}$

G $-\frac{2}{3}$

H $\frac{1}{2}$

J 2

SSM:

• plot the points

use slope formula

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{3 - 1}{-2 - 1} = \frac{2}{-3}$$