

Name: _____

Given three numbers: Do they make a triangle?

Solution: Take the smallest two numbers and add them together. If they are bigger than the largest number, then you have a triangle. If they are equal to or smaller, then you don't have a triangle.

Example 1: Given 3, 4, 5

Example 2: Given 3, 6, 9

Solution: $3 + 4 = 7$, $7 > 5$ so triangle

$3 + 6 = 9$, $9 \text{ not } > 9$ so no triangle

1. 5, 6, 9 Y or N

2. 2, 8, 11 Y or N

3. 2, 5, 6 Y or N

4. 9, 2, 8 Y or N

5. 6, 3, 2 Y or N

6. 8, 8, 8 Y or N

Given two numbers: Find the range of possible values of the third side of the triangle

Solution: Take the two numbers, subtract the smaller from the larger number; this is the lower bound (LB). Add them together; this is the upper bound (UB). The third side must lie between the two bounds: lower bound < third side < upper bound

Example: Given 12 and 19 $LB = 19 - 12 = 7$ $UB = 19 + 12 = 31$

So the third side must be bigger than 7, but less than 31.

$7 < n < 31$

1. 3, 9 $< n <$

2. 5, 12 $< n <$

3. 7, 3 $< n <$

4. 9, 15 $< n <$

5. 14, 21 $< n <$

Given three sides of a triangle or three angles of a triangle, order the other from largest to smallest (L to S) or smallest to largest (S to L)

Solution: Write the given numbers in correct order (L to S or S to L). Substitute the letter(s) of what the numbers represent. Then substitute the missing letters of the triangle. This gives us the order of the other piece.

Example 1: Given $AB = 3$, $BC = 6$, $AC = 5$

Arrange angles smallest to largest

Solution:

$$3 < 5 < 6$$

$$AB < AC < BC$$

$$\angle C < \angle B < \angle A$$

Arrange given in order

Sub in letters

Put in missing letter(s)

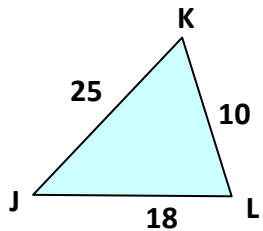
Example 2: Given $\angle A = 30^\circ$, $\angle B = 60^\circ$, $\angle C = 90^\circ$

Arrange sides largest to smallest

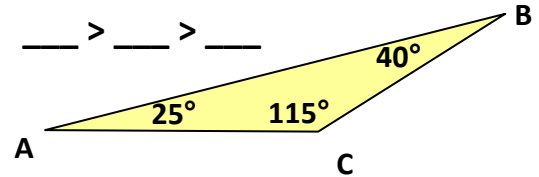
$$90 > 60 > 30$$

$$\angle C > \angle B > \angle A$$

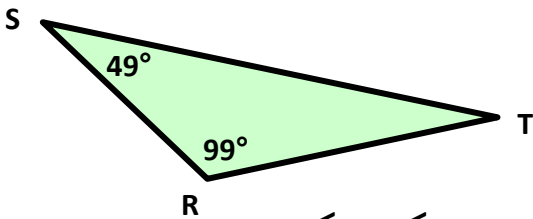
$$AB > AC > BC$$



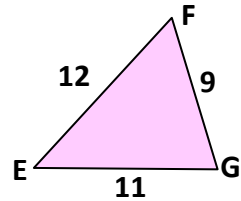
$$______ < ______ < ______$$



$$______ > ______ > ______$$



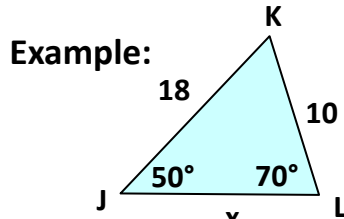
$$______ < ______ < ______$$



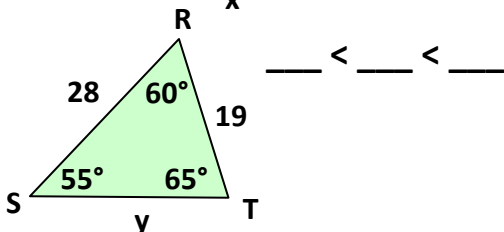
$$______ > ______ > ______$$

Given two angles and their opposite sides: Find the range of possible values of the third side of the triangle

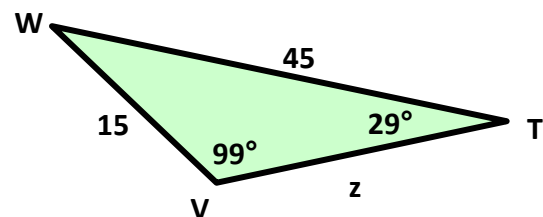
Solution: Find the largest angle (largest side is opposite it). Find the smallest angle (smallest side is opposite it). The third side must lie between the two sides:
smallest side < middle side < largest side



60 is the missing (middle) angle. 18 is the largest side (opp lg \angle) and 10 is the smallest side (opp sm \angle). So JL must be between the smallest and largest sides: $10 < x < 18$



$$______ < ______ < ______$$



$$______ < ______ < ______$$