

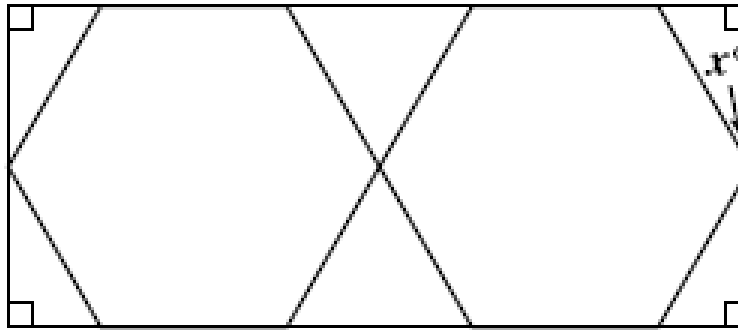
Modified and Animated By Chris Headlee  
Dec 2011

# **CHAPTER 7 SOL PROBLEMS**

**SSM: Super Second-grader Methods**

SOL Problems; not Dynamic Variable Problems

25 This figure shows a pattern of triangles and regular hexagons.



What is the value of  $x$  ?

- A** 30
- B** 60
- C** 90
- D** 120

**SSM:**

- $x$  is acute so C and D are wrong.
- $x$  is smaller acute (compared to other acute angle in  $\Delta$ )

**Regular hexagon: each angle is  $[(n - 2) \times 180 = 720] \div 6 = 120$**

**120 is an exterior angle to triangle  $\rightarrow$  so  $90 + x = 120$   
 $x = 30$**

26 Which figure has all sides of equal measure but not necessarily all angles of equal measure?

- F Square
- G Rectangle
- H Rhombus**
- J Trapezoid

**SSM:**

- Look to find examples of each figure
- Rectangles and squares have 4 –  $90^\circ$  angles
- One side of a trapezoid is shorter or longer than the others

**Squares and Rhombus are only quadrilaterals with four equal sides.  
Squares have all 90 angles.**

29 In rectangle  $ABCD$ , the slope of  $\overline{AB}$  is  $\frac{1}{2}$ . What is the slope of  $\overline{CD}$  ?

A  $-2$

B  $-\frac{1}{2}$

**C**  $\frac{1}{2}$

D  $2$

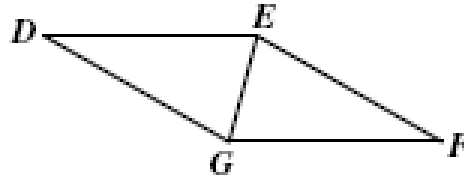
**SSM:**

- look at the opposite sides of a rectangle
- They are parallel!

**Rectangles are parallelograms**

**Parallelograms opposite sides are parallel**  
**parallel lines have the same slope**

31  $DEFG$  is a rhombus with  $m\angle EFG = 28^\circ$ .



What is  $m\angle GDE$  ?

- A  $14^\circ$
- B  $28^\circ$**
- C  $30^\circ$
- D  $56^\circ$

**SSM:**

- compare  $\angle EFG$  to  $\angle GDE$
- they are the same!

rhombus is a parallelogram  
opposite angles in parallelogram are equal

32 This figure is a traffic sign in the shape of a regular octagon.



**SSM:**

- $x$  is an acute angle; eliminate H and J
- fold corner of paper in half to compare to 45  $\rightarrow$  equal!

What is the value of  $x$  ?

- F** 45
- G** 60
- H** 135
- J** 180

$x$  is an exterior angle of an octagon (8 sides)

$8x = 360$  (sum of exterior angles = 360)

$$x = 45$$

- 33 A rectangular rug is 24 feet long and 10 feet wide. A rhombus design is formed inside the rug by joining the midpoints of each side of the rectangle. What is the length of each side of the rhombus?

- A** 13 ft
- B** 26 ft
- C** 169 ft
- D** 240 ft

**SSM:**

- Numbers in C and D don't fit inside the sides of the rectangle

Drawing a picture gives us a right-triangle in a corner →  
so Pythagorean Thrm applies  
midpoints divide rectangle sides in half!

$$5^2 + 12^2 = x^2$$

$$25 + 144 = x^2$$

$$169 = x^2$$

$$13 = x$$

44 Parallelogram  $RSTV$  has coordinates  $R(0, 0)$ ,  $S(2, 4)$ ,  $T(6, 0)$ , and  $V(4, -4)$ .

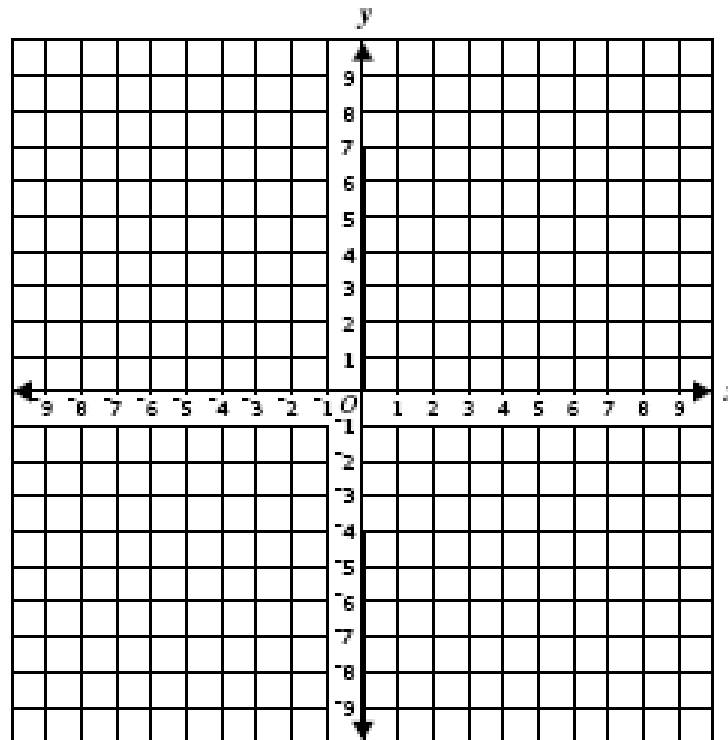
Which ordered pair represents the intersection of the diagonals of this parallelogram? (The coordinate grid may be used to help answer this question.)

F  $(2, 0)$

**G**  $(3, 0)$

H  $(3, 1)$

J  $(4, -1)$



**Midpoint formula:**

**Use to find each mid-point**

**SSM:**

- plot the answers (points)
- see which point corresponds to intersection



24 Which of the following quadrilaterals is *not* a parallelogram?

F Rectangle

G Rhombus

H Square

**J** Trapezoid

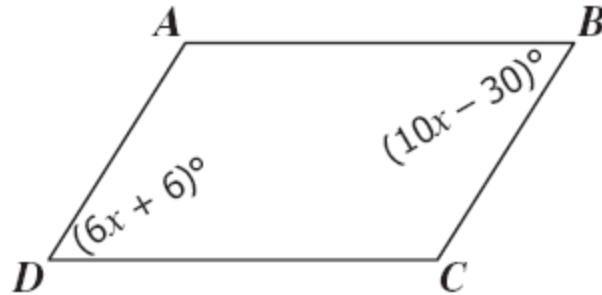
**SSM:**

• draw the answer and see if it looks like a parallelogram

**Remember Quadrilateral hierarchy:**

Parallelogram  
Rectangle      Rhombus  
Square

Trapezoid



**SSM:**

- $\angle C$  is medium obtuse  
answers A and B are wrong

In parallelogram  $ABCD$ , the measure of  $\angle C$  is —

- A  $82.5^\circ$
- B  $97.5^\circ$
- C  $120.0^\circ$**
- D  $130.0^\circ$

Opposite angles are congruent:

$$6x + 6 = 10x - 30$$

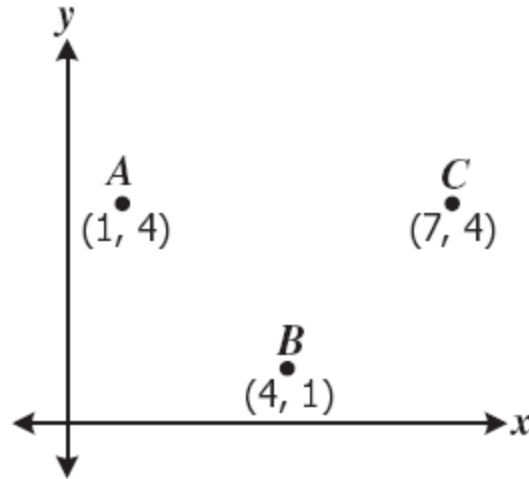
$$6 = 4x - 30$$

$$36 = 4x$$

$$9 = x$$

Consecutive angles are supplementary:

$$6(9) + 6 = 60 \quad 180 - 60 = 120$$



**SSM:**

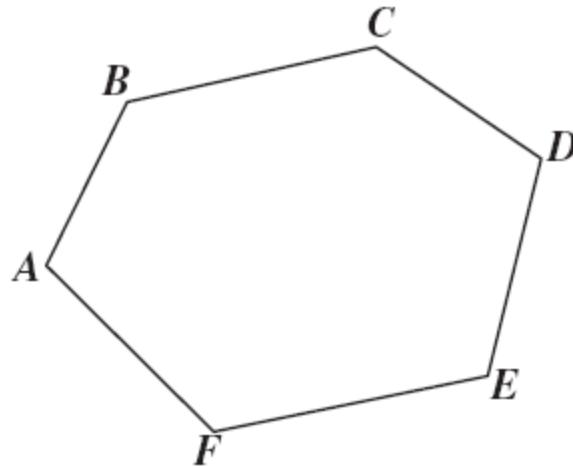
- graph all answers (points)
- pick the one that makes it a square (4,7)

In the drawing above, what must be the coordinates of  $D$  to show  $ABCD$  is a square?

- A (7, 7)
- B (4, 7)**
- C (4, 5)
- D (4, 4)

**Square – all sides equal**

up 3 and right 3 to get from B to C, so  
up 3 and right 3 to get from A to D (4, 7)

**SSM:**

- start with  $n = 3$  and  $S = 180$
- add 1 to  $n$  and 180 to  $S$
- repeat until  $n = 6$

Given the polygon shown above,  $m\angle A + m\angle F + m\angle E + m\angle D + m\angle C + m\angle B =$

**F**  $360^\circ$

**G**  $540^\circ$

**H**  $720^\circ$

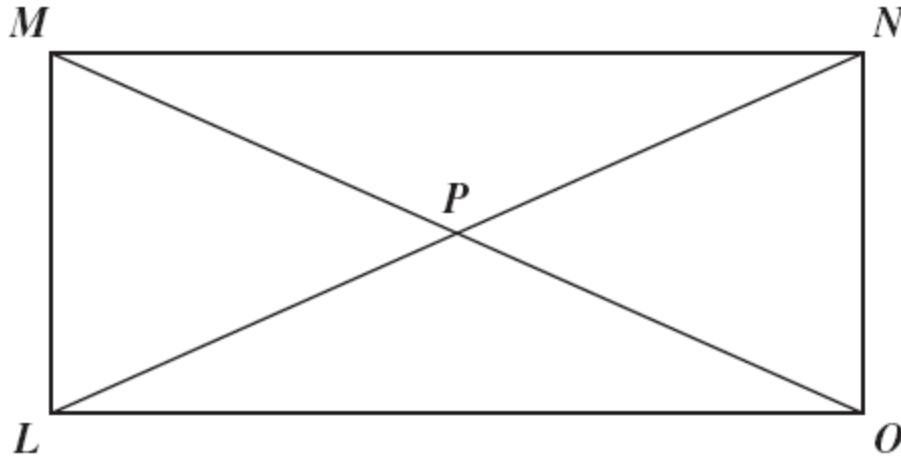
**J**  $900^\circ$

$$\text{Sum of } \angle\text{'s} = (n - 2) \times 180$$

$$= (6 - 2) \times 180$$

$$= 720$$

- 30 Rectangle  $LMNO$  represents a park that has walking paths  $\overline{LN}$  and  $\overline{MO}$  that intersect at  $P$ . The length of  $\overline{PN}$  is 195 feet, and the length of  $\overline{MN}$  is 360 feet. What is the length of  $\overline{MO}$ , one of the walking paths?



- F 150 ft
- G 195 ft
- H 360 ft
- J 390 ft**

**SSM:**

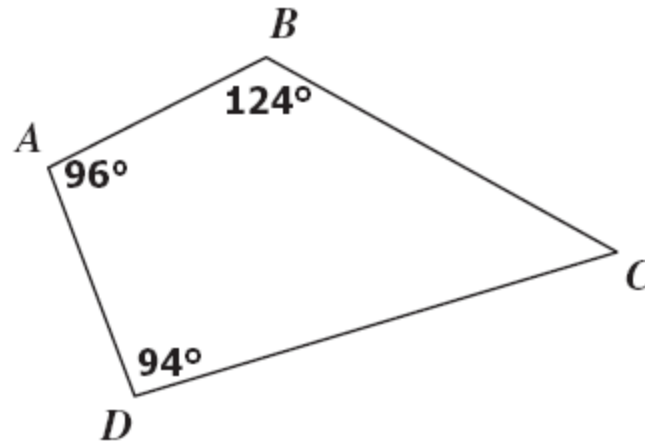
- measure PN
- compare with MP and PO
- add together

**Rectangle's diagonals bisect each other and are equal**

$$2(PN) = MO$$

$$2(195) = 390 = MO$$

31 What is the measure of  $\angle C$  in quadrilateral  $ABCD$  ?



- A**  $46^\circ$
- B**  $56^\circ$
- C**  $86^\circ$
- D**  $96^\circ$

**SSM:**

- $\angle C$  is middle acute so answers C and D are wrong
- compare with corner of paper folded in half ( $45^\circ$  angle)

Sum of  $\angle$ 's = 360

$$360 = 94 + 96 + 124 + x$$

$$360 = 314 + x$$

$$46 = x$$

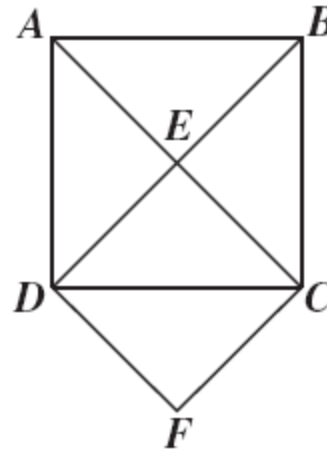
33 When tiles are tessellated in a plane, what angle measure sum is required of the tiles surrounding a single point?

- A  $90^\circ$
- B  $180^\circ$
- C  $360^\circ$**
- D  $720^\circ$

**SSM:**

• once around a point is 360

tessellation → no gaps or overlaps  
<  $360^\circ$  or  $360^\circ$  >



**SSM:**

- Use AC as a scaling reference
- EC is  $\frac{1}{2}$  AC

*ABCD* and *DECF* are both squares. If  $AC = 28$  millimeters, what is the perimeter of *DECF* ?

- F** 14 mm
- G** 28 mm
- H** 42 mm
- J** 56 mm

Square's diagonals bisect each other

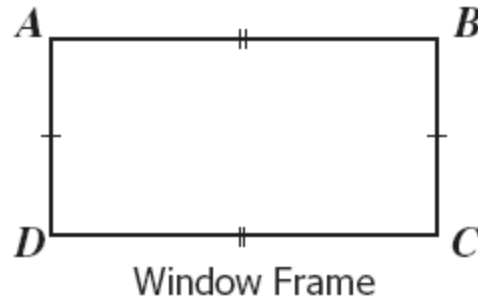
$$EC = \frac{1}{2} AC = 14$$

EC is one of the 4 equal sides of DECF

$$P_{DECF} = 4 \times 14 = 56$$



25 The opposite sides of a window frame are congruent.



SSM:

• no help

Which additional piece of information would verify that the frame is a rectangle?

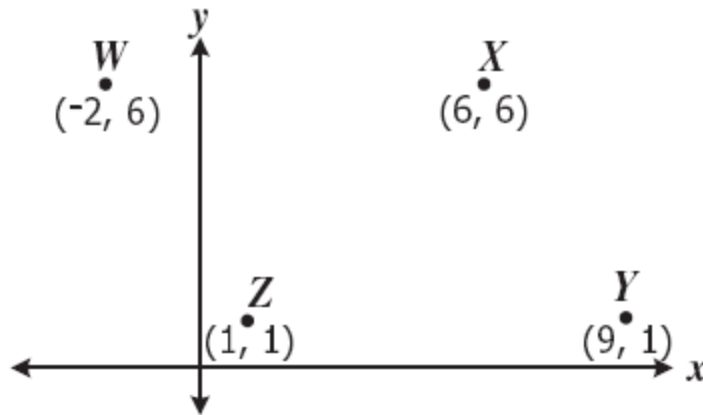
A  $\angle B \cong \angle D$

**B**  $\overline{AC} \cong \overline{BD}$

C  $\overline{AC} \perp \overline{BD}$

D  $m\angle A + m\angle D = 180^\circ$

Rectangle characteristic (often tested) is that the diagonals are equal



**SSM:**

- Plot points on graph paper
- Draw lines connecting WY and XZ

**In parallelogram WXYZ, what are the coordinates of the point of intersection of  $\overline{WY}$  and  $\overline{XZ}$  ?**

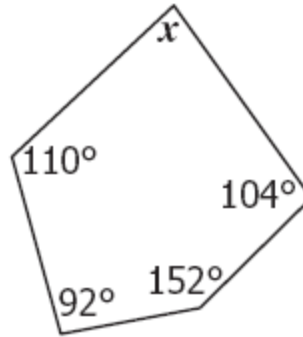
- F** (2.5, 2.5)
- G** (7.5, 3.5)
- H** (5.5, 3.5)
- J** (3.5, 3.5)

**Parallelogram's diagonals bisect each other:**

**So the midpoints of either WY or XZ is the intersection point**

**XZ midpoint is ( (1+6)/2 , (1+6)/2 ) or (3.5, 3.5)**

27 The pentagon has the angle measures shown.



**SSM:**

- Angle  $x$  is a large acute angle
- Only answer that is acute is A

What is  $m\angle x$  ?

- A**  $82^\circ$
- B**  $92^\circ$
- C**  $108^\circ$
- D**  $112^\circ$

Pentagon's interior angles sum to  $540 = (n - 2) \times 180$

$$540 = x + 104 + 152 + 92 + 110$$

$$540 = x + 458$$

$$82 = x$$

28 For a regular polygon with three sides, each interior angle has a measure of —

F  $180^\circ$

**G**  $60^\circ$

H  $45^\circ$

J  $30^\circ$

**SSM:**

- 3 sided polygon is a triangle
- regular all angles equal
- $180/3 = 60$

Triangle's interior angles sum to  $180 = (n - 2) \times 180$

$$180 = x + x + x$$

$$180 = 3x$$

$$60 = x$$

29 Each interior angle of a regular polygon measures  $156^\circ$ . How many sides does the polygon have?

A 13

B 14

**C 15**

D 16

SSM:

• not much help

Interior angle + exterior angle = 180

$$156 + x = 180$$

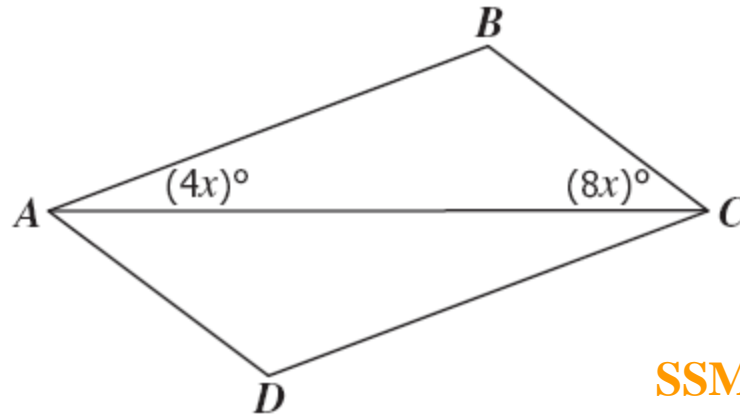
$$x = 24$$

$$360 = n \times \text{exterior angle}$$

$$360 = 24 n$$

$$15 = n$$

31 If  $ABCD$  is a parallelogram and  $x = 5$ , what is  $m\angle D$ ?



- A  $100^\circ$
- B  $120^\circ$**
- C  $140^\circ$
- D  $160^\circ$

**SSM:**

- Use corner of scrap paper: Angle  $D$  is a medium obtuse angle eliminate answers A and D

Triangle's interior angles sum to  $180 = \angle B + 4x + 8x$

where  $x = 5$

$$180 = \angle B + 4(5) + 8(5)$$

$$180 = \angle B + 60$$

$$120 = \angle B$$

Opposite angles equal in parallelogram so  $\angle D = 120$

3 One exterior angle of a regular polygon measures  $72^\circ$ . What is the measure of one interior angle?

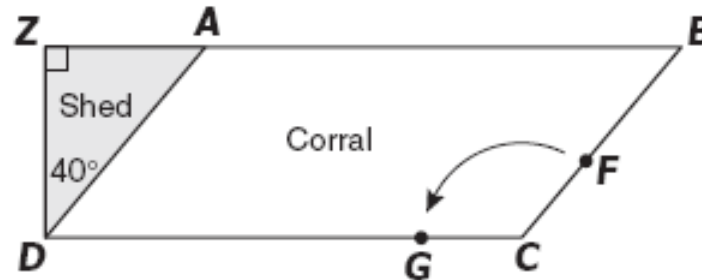
- A  $18^\circ$
- B  $108^\circ$**
- C  $360^\circ$
- D  $540^\circ$

**SSM:**

- interior angle  $< 180$
- $180 (72 + 108)$  is a “magic” #

$$\begin{aligned}\text{Interior} + \text{Exterior} &= 180 && \text{(linear pair)} \\ 180 - 72 &= 108\end{aligned}$$

- 24 Gene's horse corral, labeled  $ABCD$  in the drawing, is shaped as a parallelogram and is adjacent to the shed, labeled  $ZAD$ .



SSM:

• angle is obtuse

If a gate, labeled  $CF$ , opens all the way to the corral fence, position labeled  $CG$ , through how many degrees does the gate swing?

- F  $40^\circ$   
 G  $50^\circ$   
**H**  $130^\circ$   
 J  $140^\circ$

Parallelograms: consecutive angles are supplementary

angle D forms a right angle with  $40^\circ$  angle, so angle D =  $50$   
 $180 - 50 = 130$

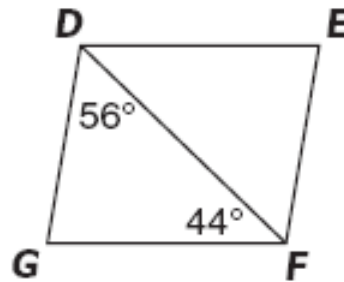
or

Parallelograms: opposite angles congruent

angle A is exterior angle to shed so angle A =  $40 + 90 = 130$   
 angle C must be 130



25 A diagonal of parallelogram  $DEFG$  forms angles with measures as shown.



SSM:

- angle is *large acute*
- only C applies

What is the measure of  $\angle DEF$ ?

- A  $44^\circ$
- B  $56^\circ$
- C  $80^\circ$**
- D  $100^\circ$

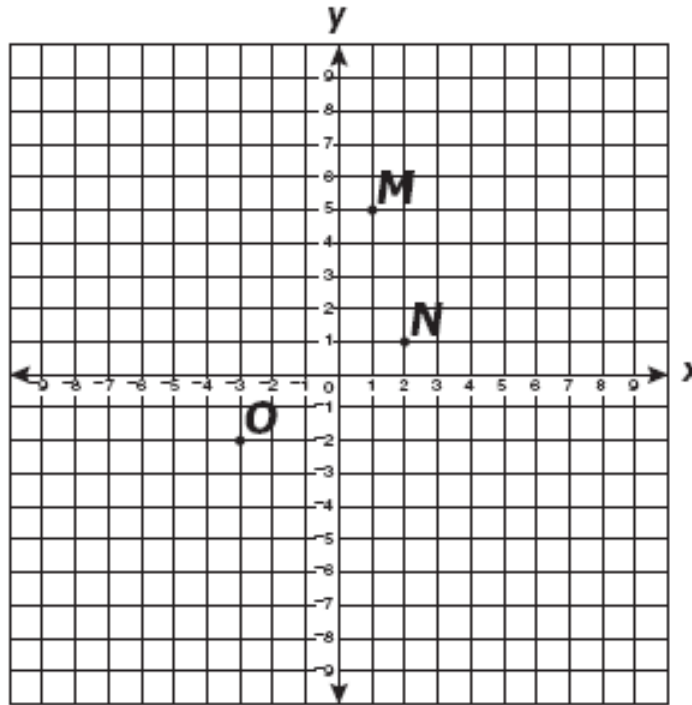
Parallelograms: diagonals form alternate interior angles

so angle D is  $56 + 44 = 100$

Parallelograms: consecutive angles supplementary

angle E =  $180 - 100 = 80$

26



SSM:

- plot each of the answer points  $(-5, 2)$ ,  $(-4, 2)$ ,  $(-3, 2)$  and  $(0, 2)$
- Use eyes to see which is correct

Quadrilateral  $MNOP$  is a parallelogram. The coordinates of three of its vertices are  $M(1, 5)$ ,  $N(2, 1)$ , and  $O(-3, -2)$ . If  $(x, 2)$  are the coordinates of  $P$ , what is the value of  $x$  ?

**F** -5

**G** -4

**H** -3

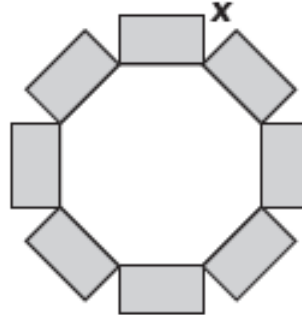
**J** 0

Parallelograms: opposite side parallel

so slope from  $MN$  must be same for  $PO$

over (left) 1 and up 4 gets to  $(-4, 2)$

- 27 Rectangular flowerbeds are built on each side of a fishpond in the shape of a regular octagon.



SSM:

- angle is acute
- answer D is wrong

What is the measure of the angle,  $x$ , between two consecutive flowerbeds?

- A  $30^\circ$   
B  $45^\circ$   
C  $60^\circ$   
D  $90^\circ$

Octagon:  $360 / 8 = 45$  (exterior angle measure)

Once around a point is  $360^\circ$

Interior angle + exterior angle =  $180$

two rectangle corners  $(90+90) = 180$

so  $x$  must be the same as the exterior angle!

$$x = 45$$

28



SSM:

• no real help

A portion of a regular polygon is shown. The polygon has —

- F** 15 sides
- G** 16 sides
- H** 18 sides
- J** 20 sides

number of sides,  $n$  is obtain by:

$$\begin{aligned} n &= 360 / \text{ext angle} \\ &= 360 / 24 \\ &= 15 \end{aligned}$$

29 Each interior angle of a regular polygon has a measure of  $162^\circ$ . The polygon has a total of —

- A 17 sides
- B 18 sides
- C 19 sides
- D 20 sides**

SSM:

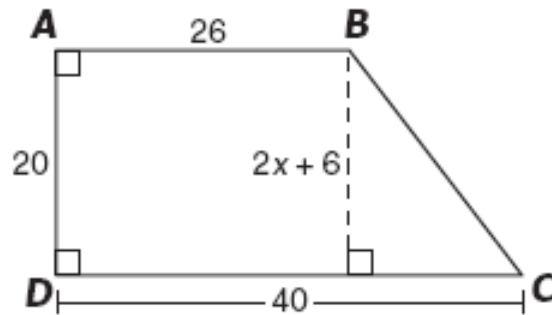
• no real help

$$\begin{array}{rclcl} \text{Exterior angle} & + & \text{interior angle} & = & 180 \\ \text{ext} & + & 162 & = & 180 \\ & & \text{ext} & = & 18 \end{array}$$

number of sides,  $n$  is obtain by:

$$\begin{aligned} n &= 360 / \text{ext angle} \\ &= 360 / 18 \\ &= 20 \end{aligned}$$

31

**SSM:**

- measure side with  $x$  in it
- compare with other sides
- must be equal to 20
- plug in answers to see which equals 20

What is the value of  $x$  in trapezoid  $ABCD$ ?

- A 17
- B 13
- C 10
- D 7**

side with  $2x + 6$  forms a rectangle  
opposite side of a rectangle are equal

$$2x + 6 = 20$$

$$2x = 14$$

$$x = 7$$

25  $XYZW$  is a rectangle.



SSM:

• choice D does not look true

Which of the following is *not* necessarily true?

A  $XY = WZ$

B  $\overline{YZ} \perp \overline{WZ}$

C  $XZ = WY$

**D**  $XY = XW$

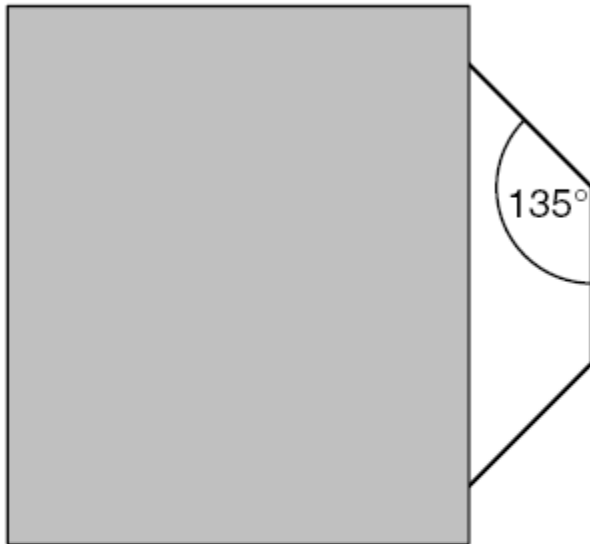
Answer A (opposite sides are congruent; parallelogram)

Answer B (all angles are right angles; rectangle)

Answer C (diagonals are congruent; rectangle)

Answer D (only true if it is a square too!)

- 26 In the drawing, a *regular* polygon is partially covered by a rectangle.



SSM:

• no real help

What is the number of sides of this polygon?

F 12

G 10

**H 8**

J 6

$$\text{int angle} + \text{ext angle} = 180$$

$$135 + \text{ext} = 180$$

$$\text{ext} = 45$$

number of sides,  $n$  is obtain by:

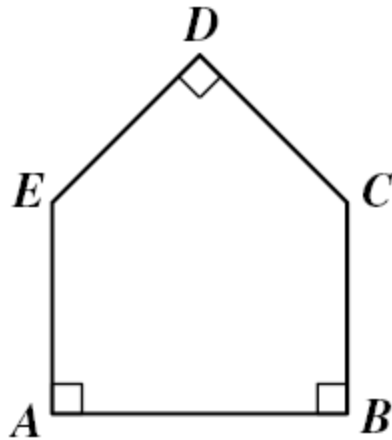
$$n = 360 / \text{ext angle}$$

$$= 360 / 45$$

$$= 8$$



27

**SSM:**

- Angle is obtuse
- Use scratch paper folded side
- angle is halfway beyond 90

If  $\angle E \cong \angle C$ , what is  $m\angle E$ ?

- A  $110^\circ$
- B  $120^\circ$
- C  $135^\circ$**
- D  $150^\circ$

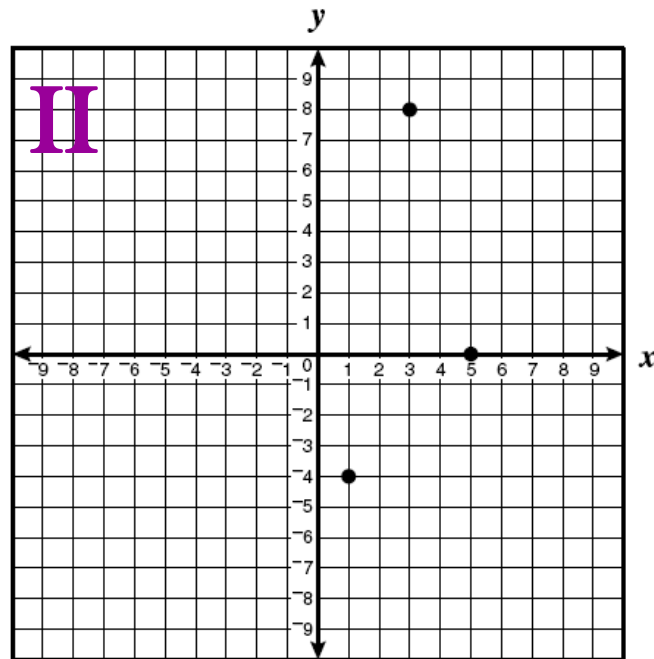
sum of interior angles for a pentagon  
 $3 \times 180 = 540$

$$3 \times 90 = 270$$

$$540 - 270 = 270 = 2\angle E$$

$$135 = \angle E$$

- 28 Three vertices of a parallelogram have coordinates  $(1, -4)$ ,  $(3, 8)$ , and  $(5, 0)$ .



What are the coordinates of the second-quadrant vertex?

- F  $(-3, 12)$   
G  $(-1, 4)$   
H  $(1, -4)$   
J  $(9, 4)$

SSM:

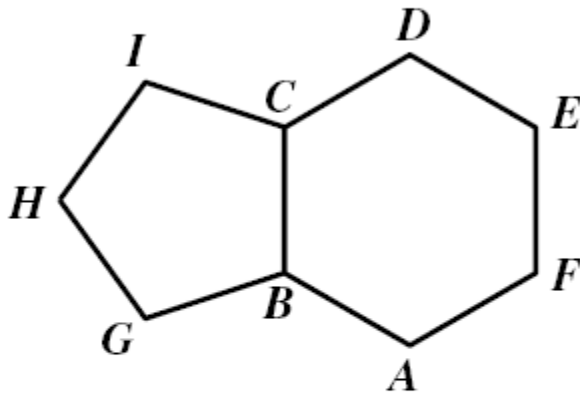
- Plot answer points
- Only F & G are Quadrant II

Opposite sides are parallel

Form triangle from  $(5,0)$  to  $(3,8)$   
(left 2 and up 8)

Go left 2 and up 8 from  $(1,-4)$

- 31 A regular pentagon and a regular hexagon share a side as shown in the figure.



What is the measure of  $\angle ABG$ ?

- A  $108^\circ$   
B  $120^\circ$   
**C  $132^\circ$**   
D  $144^\circ$

**SSM:**

- Use scratch paper folded to check how close obtuse angle is to 135
- Slightly less, but pretty close

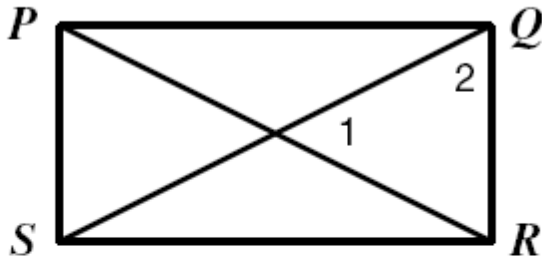
Interior angles for hexagon: 120

Interior angles for pentagon: 108

Once around a point is 360

$$360 - 228 = 132$$

32 In the rectangle  $PQRS$ ,  $m\angle 1 = 50^\circ$ .



**SSM:**

- Angle 2 is middle acute
- Eliminate answers F and G

What is  $m\angle 2$ ?

F  $130^\circ$

G  $85^\circ$

H  $70^\circ$

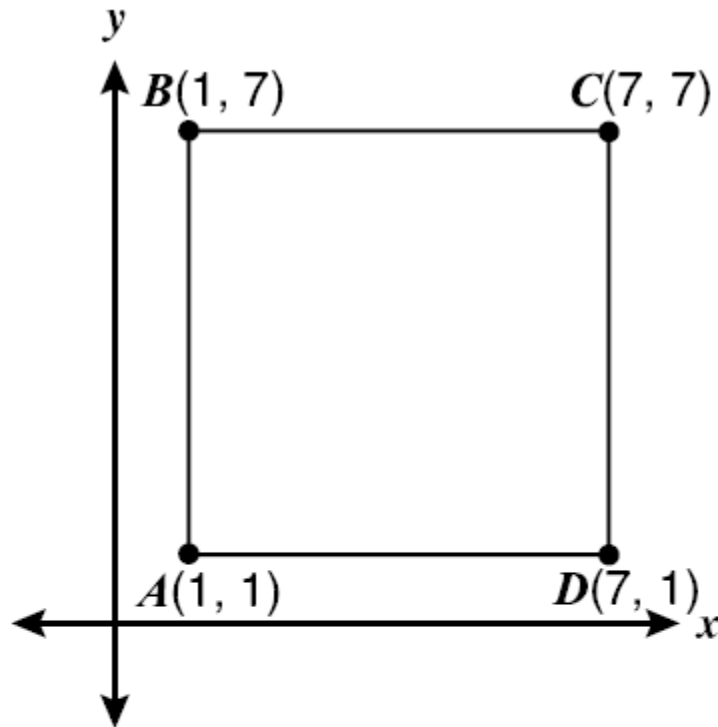
**J**  $65^\circ$

diagonals form isosceles triangles

angle 1 is 50

so angle 2 is  $\frac{1}{2} (180 - 50) = \frac{1}{2} (130) = 65$

43

**SSM:**

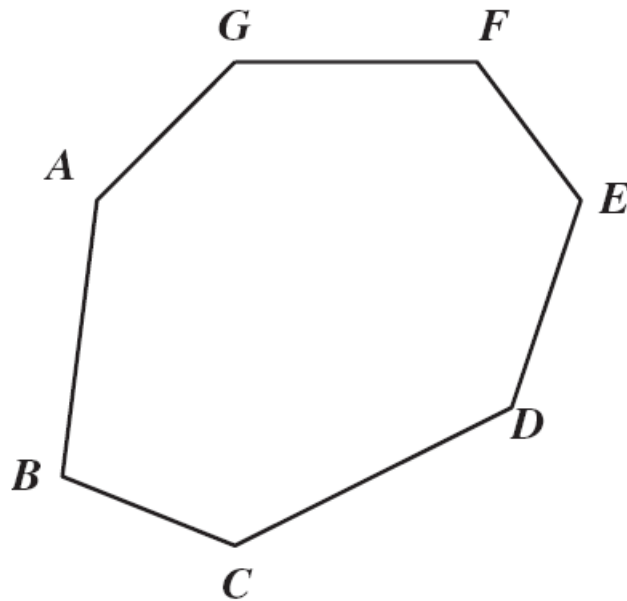
- draw on graph paper
- must be on line  $y = x$
- eliminates B and D

What is the point of intersection of  $\overline{BD}$  and  $\overline{AC}$ ?

- A (3, 3)
- B (3, 4)
- C (4, 4)**
- D (4, 3)

• Midpoint  $((1+7)/2, (1+7)/2) = (8/2, 8/2) = (4, 4)$

4 The polygon shown is convex.



SSM:

• not much help

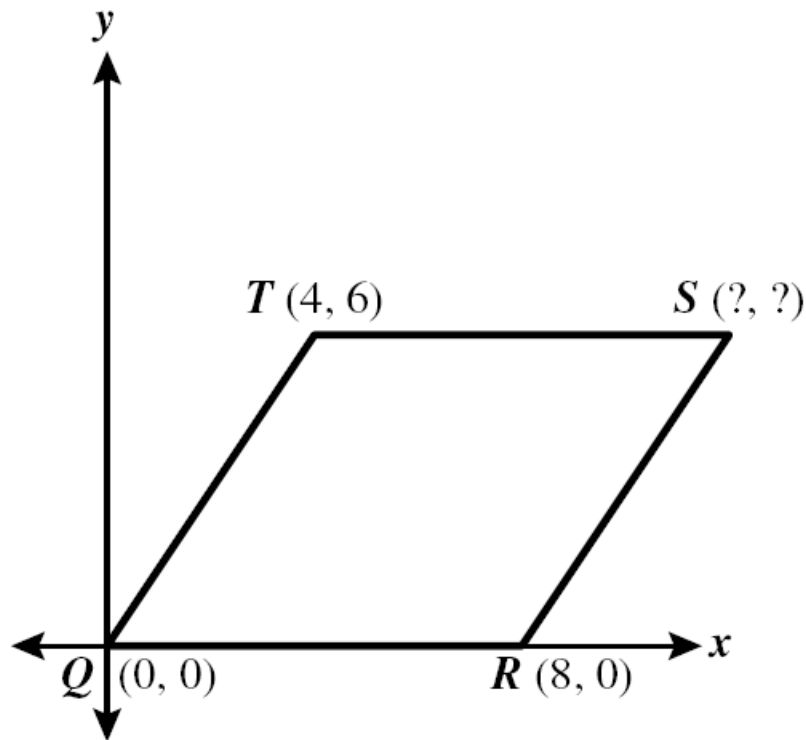
The sum of its interior angle measures is —

- F**  $900^\circ$
- G  $1,260^\circ$
- H  $1,620^\circ$
- J  $2,520^\circ$

$n$ , number of sides, is 7

$$\text{Sum of angles} = (n - 2) \times 180 = 5 \times 180 = 900$$

- 7 Quadrilateral  $QRST$  is placed on a coordinate grid as shown.



**SSM:**

- y value is along 6 eliminates B and D
- x value is beyond 8 eliminates A

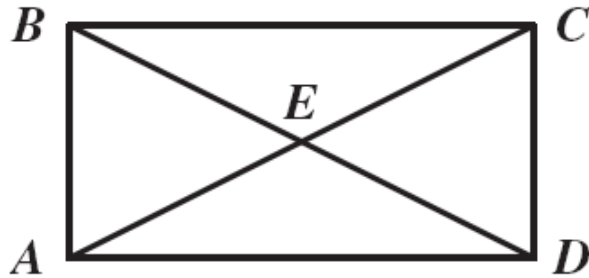
To get from Q to T: we go left 4 and up 6

To get from R to S: we do the same

What coordinates for S make  $QRST$  a parallelogram?

- A (8, 6)
- B (8, 10)
- C (12, 6)**
- D (12, 10)

24

**SSM:**

- Look at the picture
- Use your scrap paper to measure the answers

In rectangle  $ABCD$ , which of the following pairs of segments are *not* necessarily congruent?

F  $\overline{BD}$  and  $\overline{AC}$

G  $\overline{AB}$  and  $\overline{CD}$

**H**  $\overline{BC}$  and  $\overline{DC}$

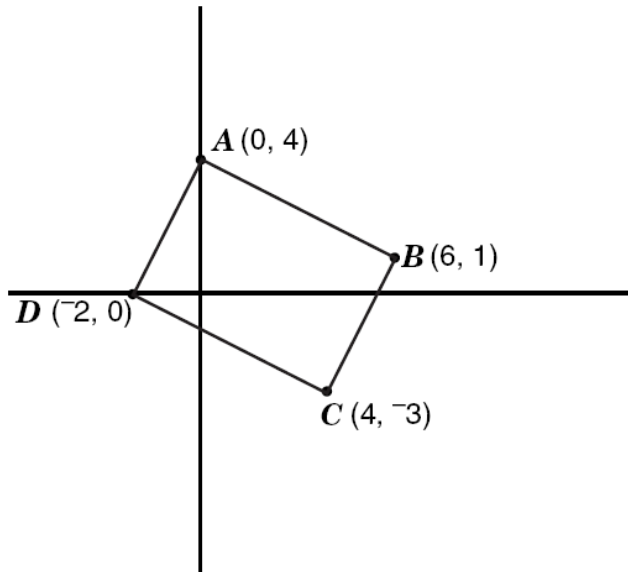
J  $\overline{BE}$  and  $\overline{CE}$

Three answers are correct; one incorrect

Answer H does not fit the drawing



- 25 The town plaza in a certain town is a parallelogram. The town's planning committee has decided to build a fountain at the center of the plaza. This sketch shows the corner points when placed on a coordinate grid.



**SSM:**

- plot all answer points
- see which one is “center”

**parallelogram: diagonals bisect each other**

**midpoint formula:**  $(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2})$

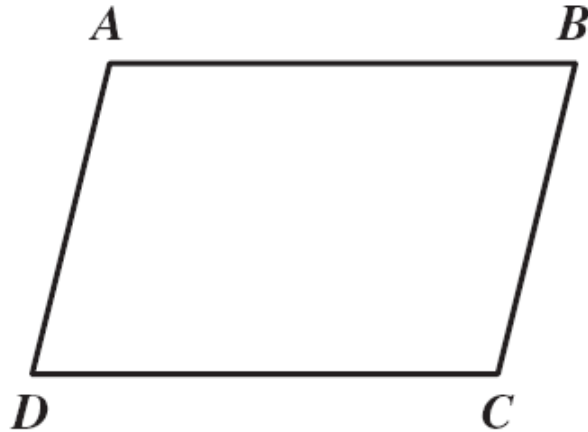
$$(\frac{-2+6}{2}, \frac{0+1}{2}) = (2, \frac{1}{2})$$

$$= (2, 0.5)$$

**Which coordinates show where the fountain will be located?**

- A** (2, 0.5)  
**B** (0.5, 2)  
**C** (3, 1.5)  
**D** (1.5, 1)

26 Quadrilateral  $ABCD$  is a parallelogram.



**SSM:**

- Look at the picture
- Use your scrap paper to measure the answers F & G
- J is only one the makes sense

Which of the following *must* be true?

F  $\overline{AB} \cong \overline{AD}$

G  $\overline{AC} \cong \overline{BD}$

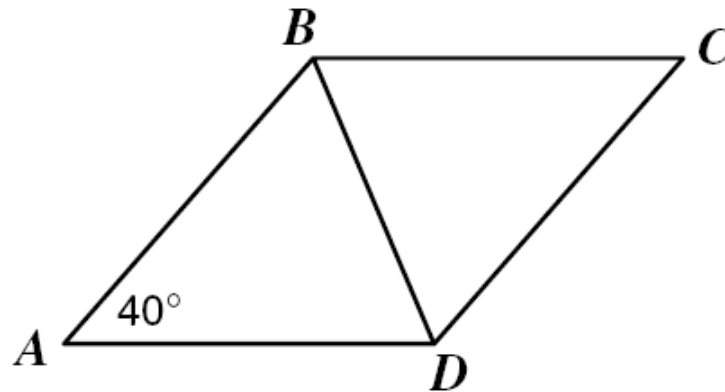
H  $\angle A \cong \angle D$

**J**  $\angle B \cong \angle D$

**Parallelogram characteristics:**

**Opposite angles are congruent**

27  $ABCD$  is a rhombus.



**SSM:**

- angle B (the whole thing) is obtuse
- use folded corner of scrap paper to compare to 135 -- pretty close so either B or C

What is the measure of  $\angle CBD$ ?

- A  $50^\circ$
- B  $60^\circ$
- C  $70^\circ$**
- D  $75^\circ$

Angle B must be supplementary to angle A (from parallelogram's characteristics)

so angle B is 140

rhombus diagonals act as angle bisectors so they divide B into two  $70^\circ$  angles

**28** If each interior angle of a regular polygon measures  $120^\circ$ , how many sides does the polygon have?

**F** 14

**G** 12

**H** 8

**J** 6

**SSM:**

• not much help

**interior angle + exterior angle = 180**

$$120 + \text{Ext} = 180$$

**exterior angle = 60**

**$360 / \text{exterior angle} = n$  (nr of sides)**

$$360 / 60 = 6 = n$$

29 Which angle measure below is *not* a possible measure of an exterior angle of a regular polygon?

A  $36^\circ$

B  $40^\circ$

C  $45^\circ$

**D**  $54^\circ$

SSM:

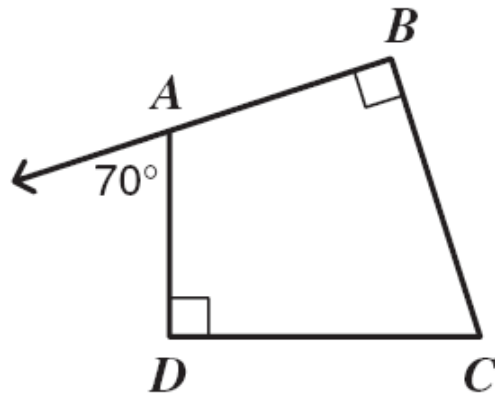
• not much help

Three answers are correct; one incorrect

divide answers into 360 to get number of sides  
and it must be a whole number

Answer D does not fit the drawing

30

**SSM:**

- Look at the picture
- angle C is acute  
eliminates all answers but F

In the figure, what is the measure of  $\angle C$ ?

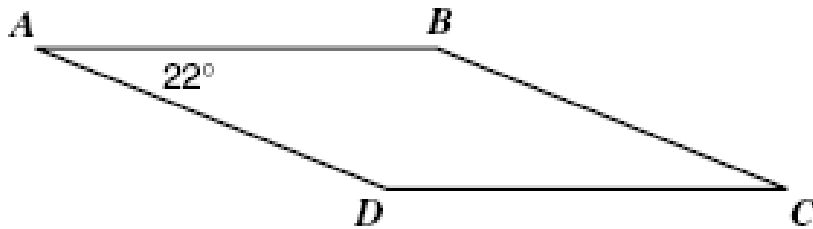
- F**  $70^\circ$   
G  $90^\circ$   
H  $100^\circ$   
J  $110^\circ$

All angles inside figure must add to 360 for quadrilateral

Angle A forms linear pair with  $70^\circ$  exterior angle  $\rightarrow$  so angle A = 110

$$360 - (90 + 90 + 110) = \text{angle C} = 70$$

24

**SSM:**

- angle C is small acute
- only answer F fits

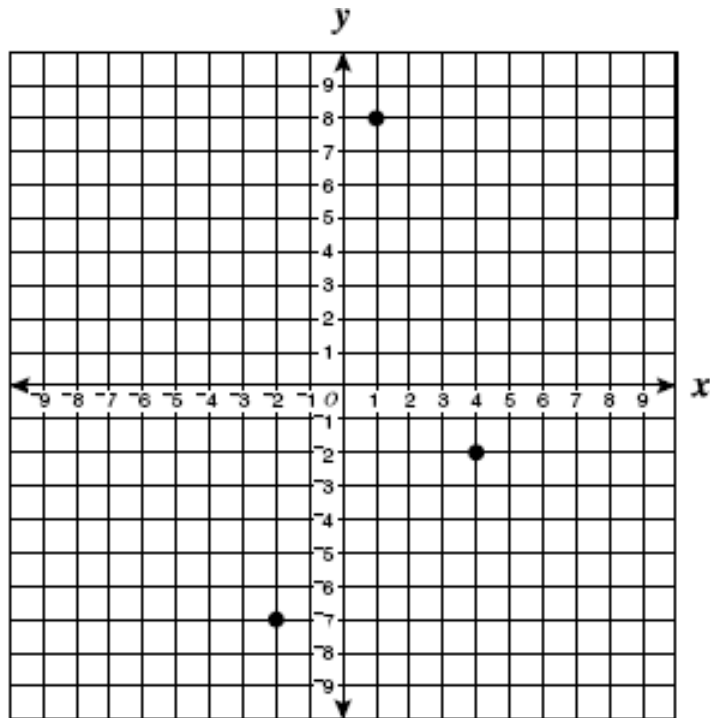
Quadrilateral  $ABCD$  is a parallelogram.  
The measure of  $\angle C$  is —

- F**  $22^\circ$
- G  $68^\circ$
- H  $112^\circ$
- J  $158^\circ$

parallelogram:

opposite angles are congruent

- 25 The vertices of parallelogram  $ABCD$  have coordinates  $A(1, 8)$ ,  $B(4, -2)$ , and  $C(-2, -7)$ .



SSM:

- plot answer points on graph paper
- D is in QII

Since opposite sides of a parallelogram are parallel:

B to A is left 3 and up 10

C to D must be left 3 and up 10

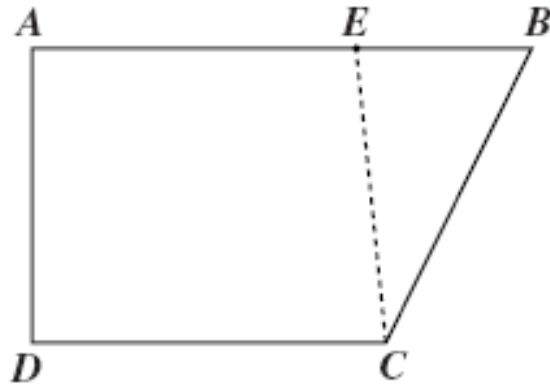
$$C \text{ to } D(-2 - 3, -7 + 10) = (-5, 3)$$

What are the coordinates of  $D$ ?

- A**  $(-5, 3)$
- B  $(-3, 5)$
- C  $(2, 3)$
- D  $(5, -3)$



- 26 A desktop was made from the scrap of plywood shown by cutting (in a straight line) from  $C$  to  $E$ .



SSM:

- look at picture and see which answers make any sense

Which measurement would ensure that the desktop is rectangular?

- F  $AE = EB$
- G  $AC = BD$
- H  $EC = CD$
- J**  $DE = CA$

Key characteristic of a rectangle is that the diagonals are congruent !

27 Which of the following is *not* true about a parallelogram?

- A Any two opposite sides are congruent.
- B Any two opposite angles are congruent.
- C The diagonals bisect each other.
- D** Any two consecutive angles are complementary.

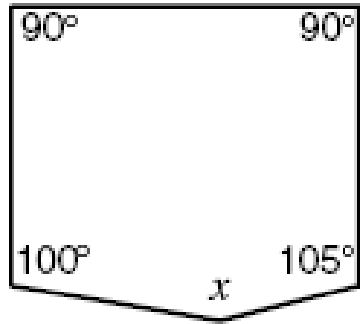
**SSM:**

• 3 are true and 1 is false

complementary  $\rightarrow$  two angles add to 90

consecutive angles of a parallelogram are supplementary

28

**SSM:**

- $x$  is a large obtuse angle
- only answer G fits

What is the value of  $x$  in the pentagon above?

- F  $90^\circ$   
G  $155^\circ$   
H  $245^\circ$   
J  $335^\circ$

Sum of the interior angles of a pentagon,  $n = 5$

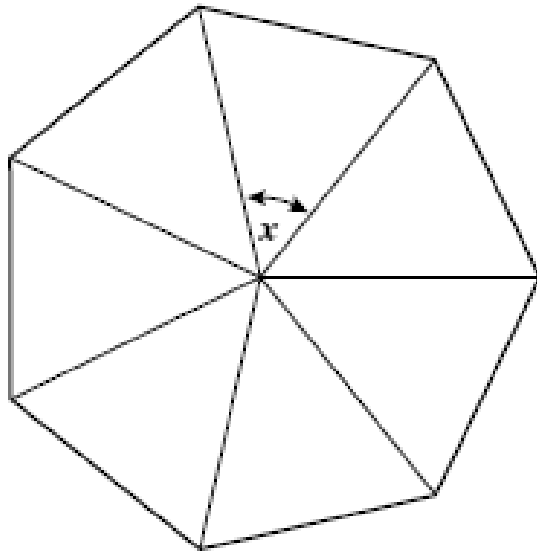
$$(n - 2) \times 180 = (3) \times 180 = 540$$

$$540 = 2 \times 90 + 100 + 105 + x$$

$$540 = 385 + x$$

$$155 = x$$

29

**SSM:**

- **x** is medium acute
- circle  $\rightarrow 360^\circ$
- **7** even pieces

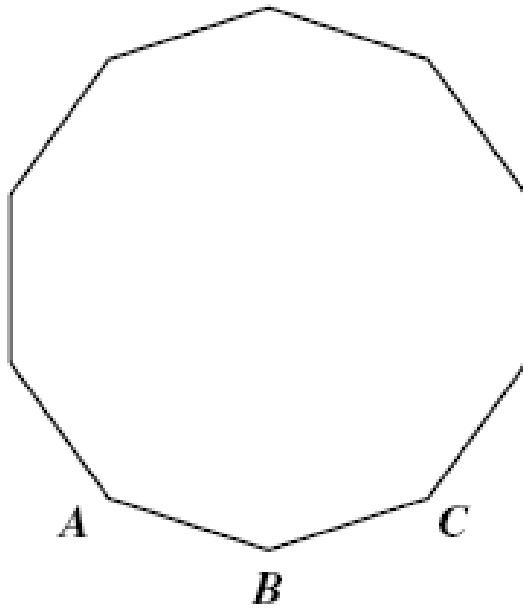
Which is the *closest* to the measure of a central angle  $x$  in this regular polygon?

- A  $40^\circ$
- B  $45^\circ$
- C  $50^\circ$**
- D  $60^\circ$

**Once around the circle is  $360^\circ$**

$$360 \div 7 = 51.42$$

30

**SSM:**

- angle is medium obtuse  
eliminates F and G

What is the measure of interior angle  $ABC$  of the regular polygon shown?

F  $225^\circ$

G  $180^\circ$

H  $160^\circ$

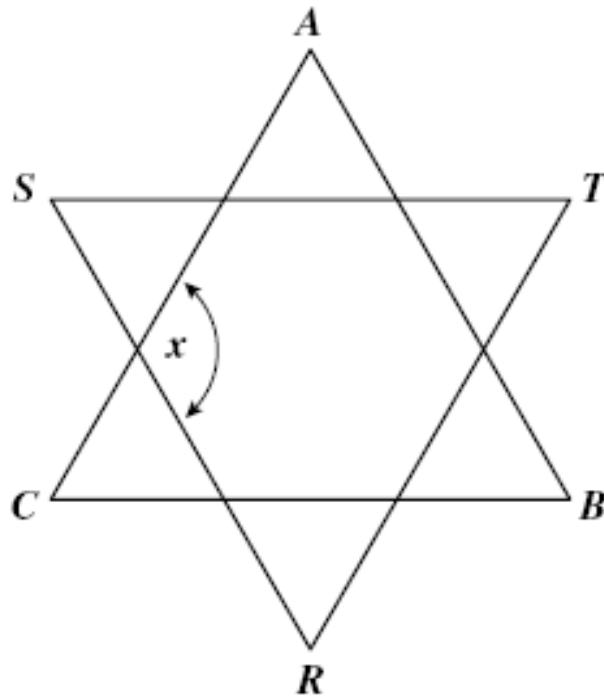
**J**  $144^\circ$

$n = 10 \rightarrow$  decagon

$360 \div 10 = 36$  (exterior angle)

$180 - 36 = 144$  (interior angle)

4

**SSM:**

- **x is an obtuse angle**

In the diagram,  $\triangle ABC$  and  $\triangle RST$  are congruent equilateral triangles with corresponding sides parallel. What is the value of  $x$ ?

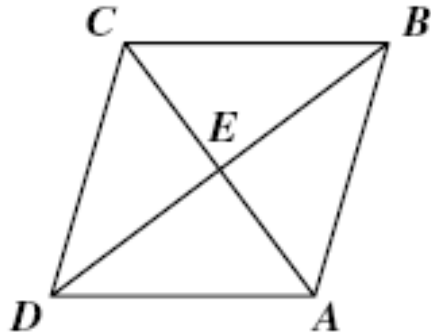
F  $90^\circ$ **G**  $120^\circ$ H  $135^\circ$ J  $144^\circ$ 

**x and the angle next to it toward S form a linear pair**

**the angle next to x is 60 (angle S is 60 from equilateral triangles and angle C is 60 for same reason; angle to the right of S in small triangle is an alternate interior angle to C and also equal to 60)**

$$180 - 60 = 120 = x$$

- 24 In rhombus  $ABCD$ ,  $AC = 30$  inches and  $BD = 40$  inches.



**SSM:**

- Use AC as a ruler to estimate CD
- $CD < 30$  (by a little)
- multiply estimate by 4 and H is only close answer

What is the perimeter of the rhombus?

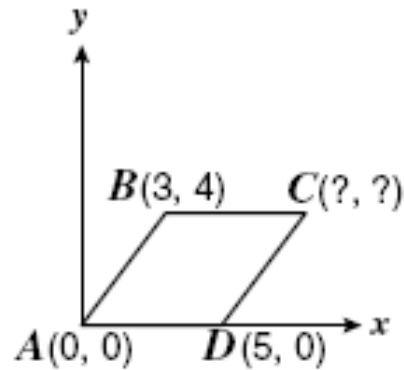
- F 25 in.  
G 50 in.  
**H** 100 in.  
J 200 in.

**Rhombus' diagonals are perpendicular and bisect each other**

**We get 4 right triangles that are pythagorean triples  
15, 20, 25 (hypotenuse and outside segment of rhombus)**

$$25 \times 4 = 100$$

25  $ABCD$  is a rhombus.



**SSM:**

• y-value has to be 4

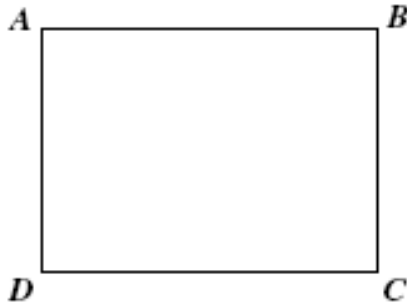
What are the coordinates of vertex  $C$ ?

- A (5, 4)
- B (6, 4)
- C (8, 4)**
- D (4, 3)

**Rhombus' sides are equal**  
so we have to add 5 to the x value of (3, 4)



- 26 The quadrilateral  $ABCD$  is a parallelogram.



SSM:

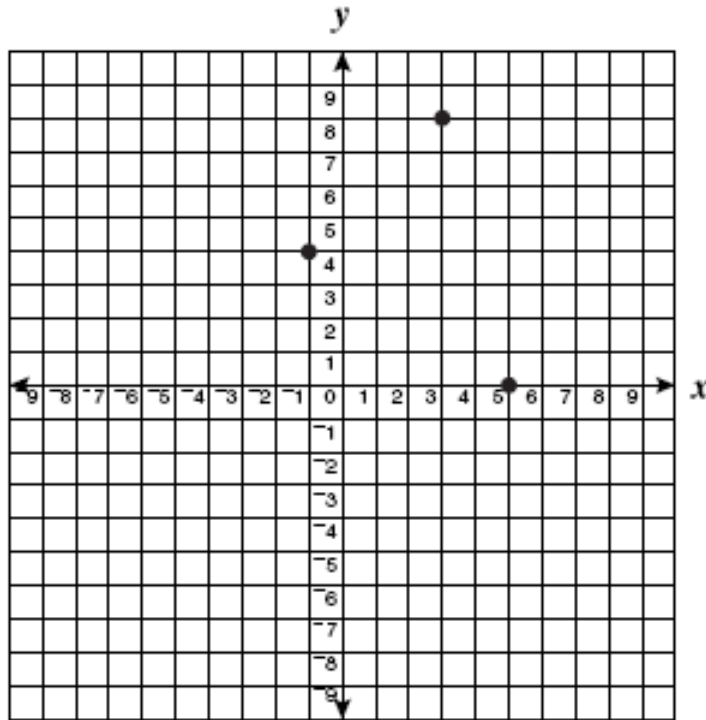
- looking at the picture:  
answer G is wrong

Which of the following pieces of information would suffice to prove that  $ABCD$  is a rectangle?

- F**  $AC = BD$
- G  $AB = AD$
- H  $m\angle B = m\angle D$
- J  $\angle A$  and  $\angle D$  are supplementary

Rectangle key characteristic is that the diagonals are equal

- 27 Three vertices of parallelogram  $ABCD$  have coordinates  $(-1, 4)$ ,  $(3, 8)$ , and  $(5, 0)$ .



SSM:

- graph the points
- answers A and B are QII

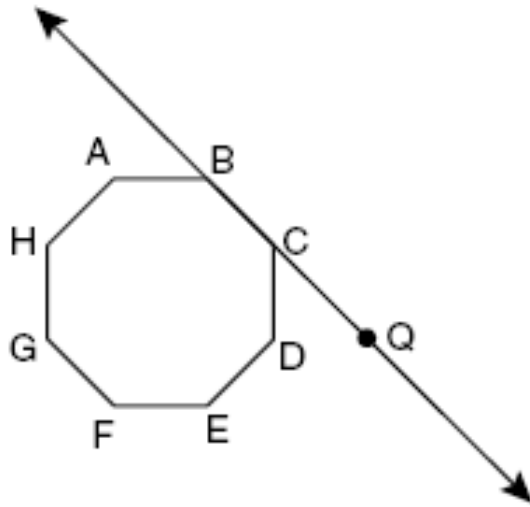
What are the coordinates of the other first-quadrant vertex?

- A  $(-3, 12)$
- B  $(-1, 4)$
- C  $(1, 4)$
- D**  $(9, 4)$

Answers C and D are only Quadrant I points

plotting points shows answer D forms a parallelogram

29

**SSM:**

- angle is medium acute  
eliminates A and possibly B
- use folded corner of scrap  
paper → its 45!

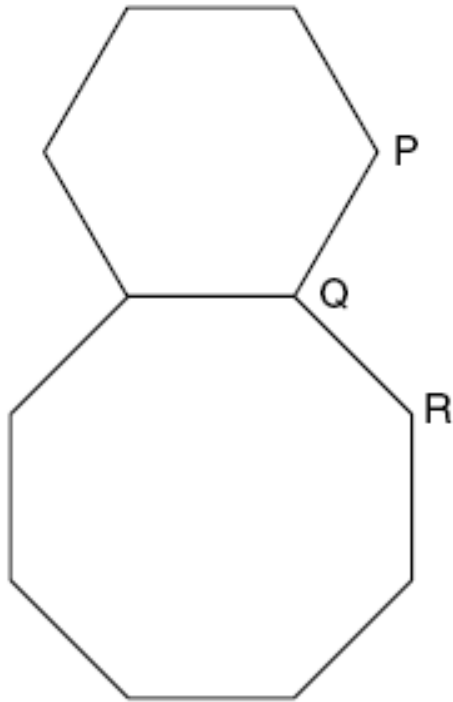
Figure *ABCDEFGH* is a regular octagon. What is the measure of  $\angle DCQ$ ?

- A  $135^\circ$
- B  $60^\circ$
- C  $45^\circ$**
- D  $30^\circ$

angle DCQ is an exterior angle

$360 \div 8$  (number of sides) = exterior angle  
 $45 = \text{exterior angle}$

30

**SSM:**

- Use corner of scrap paper
- Angle is obtuse  
eliminates F and G

Add two interior angles and subtract from 360  
or

Add two exterior angles together

$$360 \div 6 = 60 \text{ (ext } \angle \text{ for hexagon)}$$

$$360 \div 8 = 45 \text{ (ext } \angle \text{ for octagon)}$$

$$60 + 45 = 105 = \angle PQR$$

The two adjacent figures are a regular hexagon and a regular octagon. What is the measure of  $\angle PQR$ ?

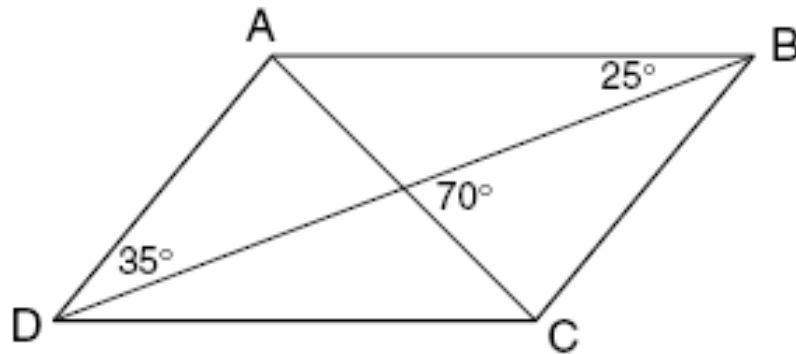
F  $87.5^\circ$

G  $90^\circ$

**H**  $105^\circ$

J  $120^\circ$

24

**SSM:**

- $\angle BDC$  is medium acute eliminates F

In parallelogram  $ABCD$ , what is  $m\angle BDC$ ?

F  $70^\circ$

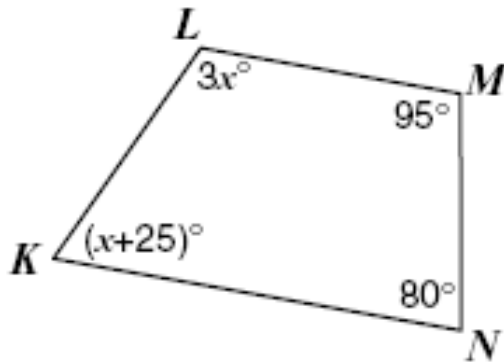
G  $45^\circ$

H  $35^\circ$

**J**  $25^\circ$

angle  $BDC$  and  $25^\circ$  angles are alternate interior and therefore equal

25

**SSM:**

- $3x$  is a medium obtuse, but  $x + 25$  is medium acute
- plug in answers and see which work (all of them do, but D)

Given quadrilateral  $KLMN$ , what is the value of  $x$ ?

- A 35
- B 40**
- C 45
- D 50

interior angles of a quadrilateral sum to 360

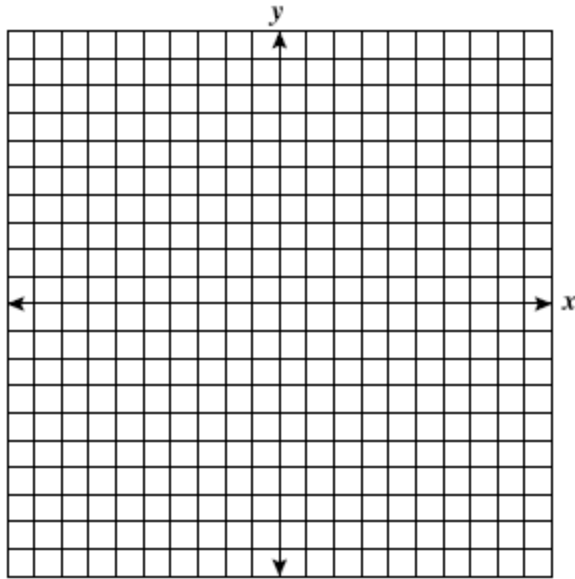
$$360 = 3x + 95 + 80 + (x + 25)$$

$$360 = 4x + 200$$

$$160 = 4x$$

$$40 = x$$

- 26 Three vertices of a parallelogram have coordinates  $(0, 1)$ ,  $(3, 7)$ , and  $(4, 4)$ . You may want to plot the points on this grid.



SSM:

- answers G and H are fourth quadrant points

What are the coordinates of the fourth-quadrant vertex?

F  $(-2, 1)$

**G**  $(1, -2)$

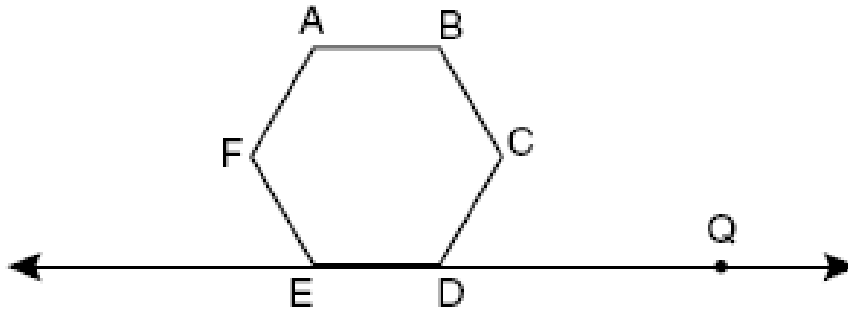
H  $(2, -1)$

J  $(3, 3)$

from  $(3, 7)$  to  $(4, 4)$  is down 3 and right 1

from  $(0, 1)$  down 3 and right 1 is  $(0+1, 1-3) = (1, -2)$

27

**SSM:**

- $\angle CDQ$  is medium acute  
eliminates C and D

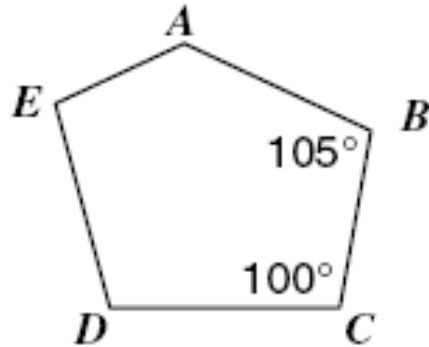
Figure  $ABCDEF$  is a regular hexagon.  
What is the measure of  $\angle CDQ$ ?

- A  $45^\circ$
- B  $60^\circ$**
- C  $90^\circ$
- D  $120^\circ$

exterior angle of hexagon is  $360 \div 6 = 60^\circ$



- 28 In pentagon  $ABCDE$ ,  $m\angle E = m\angle C$  and  $m\angle D = m\angle B$ .



**SSM:**

- $\angle A$  is a medium obtuse angle eliminates F and G

What is the measure of  $\angle A$ ?

F  $410^\circ$

G  $335^\circ$

**H**  $155^\circ$

J  $130^\circ$

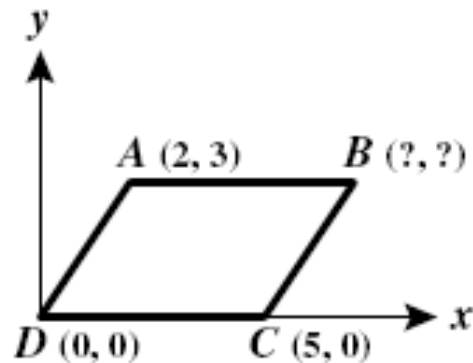
**Sum of the interior angles of a pentagon = 540**

$$540 = 100 + 100 + 105 + 105 + A$$

$$540 = 410 + A$$

$$130 = A$$

24

**SSM:**

- y-coordinate of B must be 3
- only answer J has that

If  $ABCD$  is a parallelogram, what are the coordinates of  $B$ ?

- F (3, 7)
- G (5, 5)
- H (7, 8)
- J (7, 3)**

opposite sides of parallelogram are congruent

so  $DC = 5$  and  $AB = 5$

so  $B(2 + 5, 3 + 0) = (7, 3)$

25 Which of the following quadrilaterals could have diagonals that are congruent but do *not* bisect each other?

- A A rhombus
- B A rectangle
- C A parallelogram
- ☒ D A trapezoid

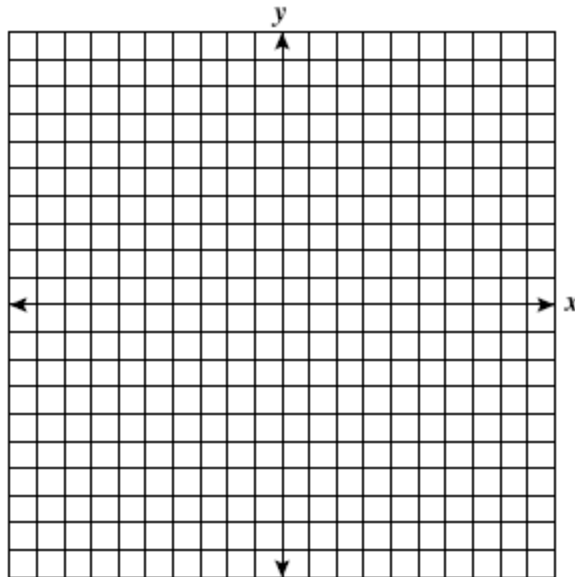
SSM:

• not much help

Since parallelogram's diagonals bisect each other, anything that is a parallelogram will not work.

A rhombus and a rectangle are also parallelograms, so the trapezoid is the only answer left. An isosceles trapezoid has diagonals that are equal, but do not bisect each other.

- 26 Three vertices of a square have coordinates  $(5, 1)$ ,  $(2, -2)$ , and  $(-1, 1)$ . You may want to plot the points on this grid.



**SSM:**

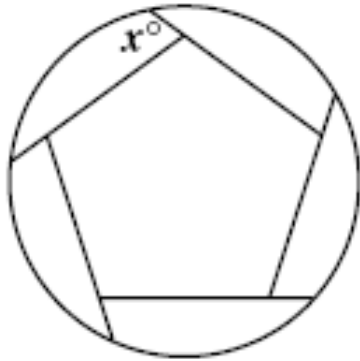
- plot the points on graph paper and see which fits
- Answer G is one of the points already give

What are the coordinates of the fourth vertex?

- F  $(-2, 2)$   
G  $(2, -2)$   
**H**  $(2, 4)$   
J  $(4, 2)$

Since a square is a rectangle, the diagonals have to be equal.  
Points  $(5, 1)$  and  $(-1, 1)$  form one diagonal  
Point  $(2, -2)$  and  $(2, ?)$  must form the other diagonal

28

**SSM:**

- $x$  is the measure of an acute angle only answer F fits

A floor tile is designed with a regular pentagon in the center of the tile with its sides extended. What is the value of  $x$ ?

- F**  $72^\circ$
- G  $90^\circ$
- H  $110^\circ$
- J  $120^\circ$

$x$  is the measure of the exterior angle of a pentagon

pentagon sides number 5

$$360 \div 5 = 72^\circ$$

- 29 Each exterior angle of a certain regular polygon measures  $30^\circ$ . How many sides does the polygon have?

A 6  
B 9  
**C 10**  
D 12

**SSM:**

• not much help

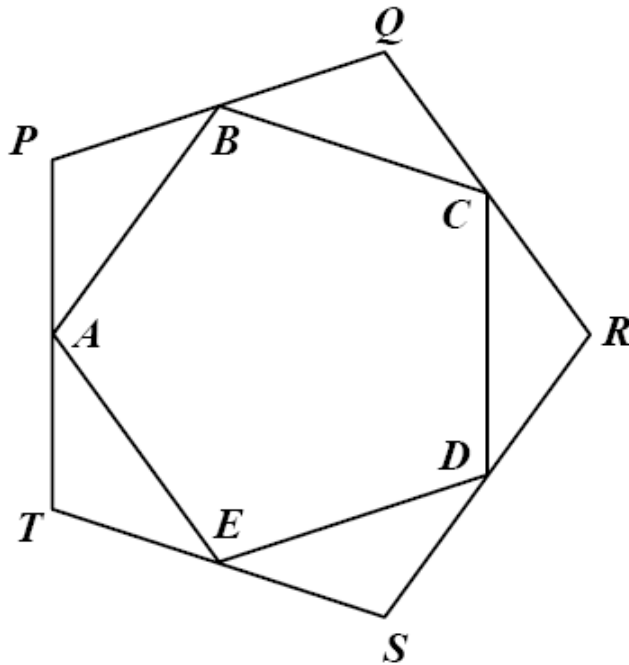
**exterior angle =  $360 \div n$  (number of sides)**

**$n \times \text{exterior angle} = 360$**

$$n \times 30 = 360$$

$$n = 10$$

4



Regular pentagon  $ABCDE$  is formed by joining the midpoints of the sides of regular pentagon  $PQRST$ .

What is the measure of  $\angle PAB$ ?

F  $30^\circ$

**G**  $36^\circ$

H  $60^\circ$

J  $72^\circ$

**SSM:**

- compare with folded corner of paper ( $45^\circ$ )
- eliminates H and J

**PT is a straight side**

so  $\angle PAB + \angle BAE + \angle TAE = 180$

$\angle BAE = 108$  (regular pentagon)

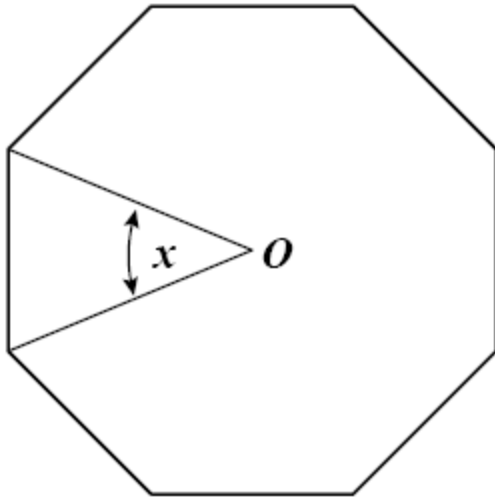
Assume  $\angle PAB = \angle TAE$

$$2x + 108 = 180$$

$$2x = 72$$

$$x = 36$$

5

**SSM:**

- compare with folded corner of piece of paper ( $45^\circ$ )
- very, very close

The polygon in the drawing is a regular octagon with  $O$  as its center. What is the value of  $x$ ?

- A  $30^\circ$
- B  $45^\circ$**
- C  $60^\circ$
- D  $72^\circ$

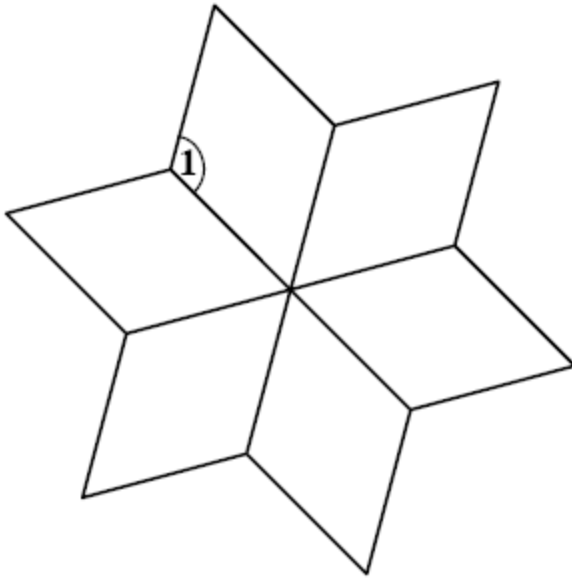
Once around a point is 360

eight parts of the circle

$$360 \div 8 = 45$$



24

**SSM:**

- angle 1 is obtuse
- eliminates F and G

The design for a quilt piece is made up of 6 congruent parallelograms. What is the measure of  $\angle 1$ ?

- F  $30^\circ$   
G  $60^\circ$   
**H**  $120^\circ$   
J  $150^\circ$

once around circle = 360

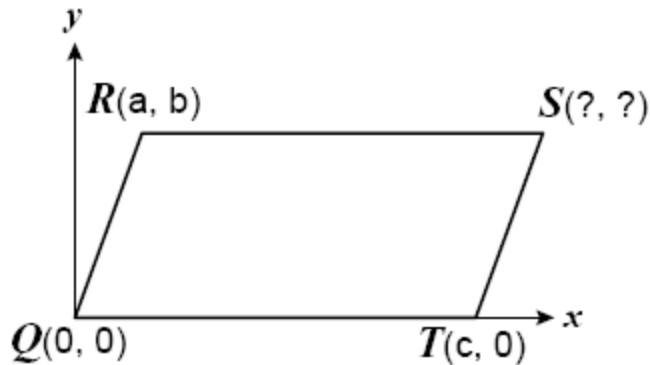
so acute angle of parallelogram is

$$360 \div 6 = 60$$

consecutive angles of parallelogram are supplementary so

$$\angle 1 = 180 - 60 = 120$$

25  $QRST$  is a parallelogram.



**SSM:**

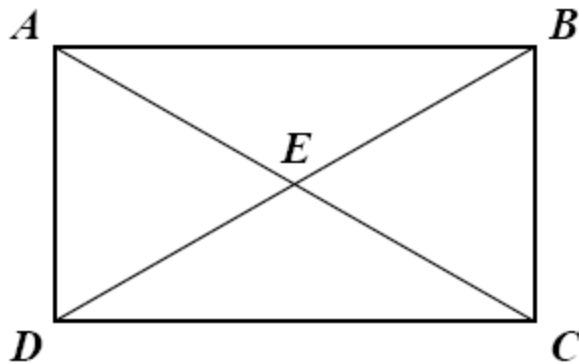
- Use points **R** and **T** to help figure **S**
- **y-value** is same as **R**
- **x-value** is greater than **T's**

What are the coordinates of vertex  $S$ ?

- A  $(c, b)$
- B  $(a + b, c)$
- C  $(c - a, b)$
- D**  $(c + a, b)$

opposite side in parallelogram are congruent  
QT is  $c$  long, so RS has to be  $c$  long  
if R starts at  $a$  the S must end at  $a+c$

26

**SSM:**

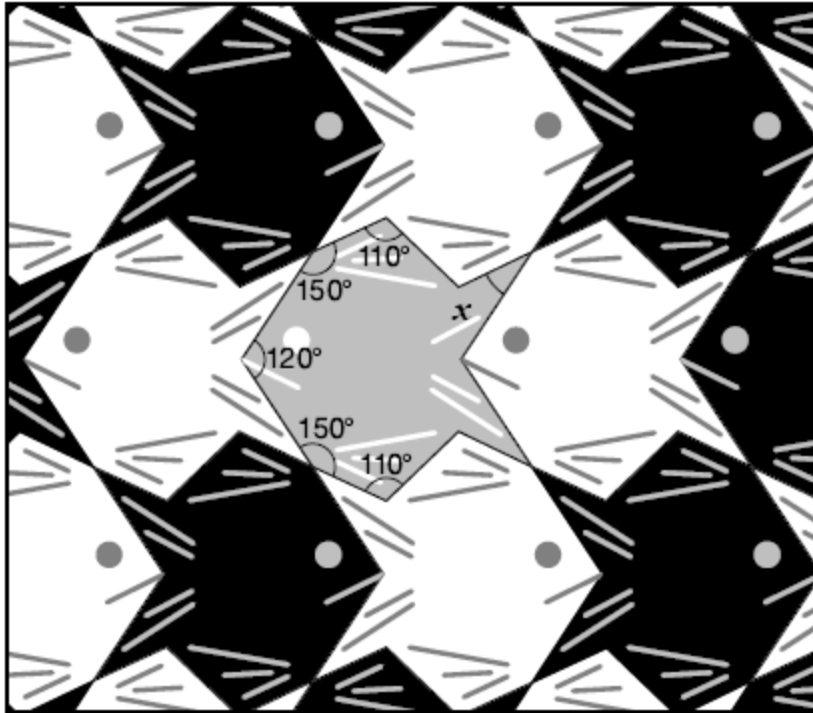
- Use scrap paper to measure AC
- Use that measurement to estimate DE
- $2 DE = AC$

Figure  $ABCD$  is a rectangle.  $\overline{AC}$  and  $\overline{BD}$  are diagonals.  $AC = 25$  meters and  $BC = 15$  meters. What is the length of  $\overline{DE}$ ?

- F 10 m  
G 12.5 m  
H 13.5 m  
J 15 m

rectangle's diagonals bisect each other and are congruent  
so  $AC = BD$  and  $2DE = BD$   
 $2DE = 25$   
 $DE = 12.5$

- 27 Some of the angle measures are given for one of the fish-shaped polygons in this tessellation.



SSM:

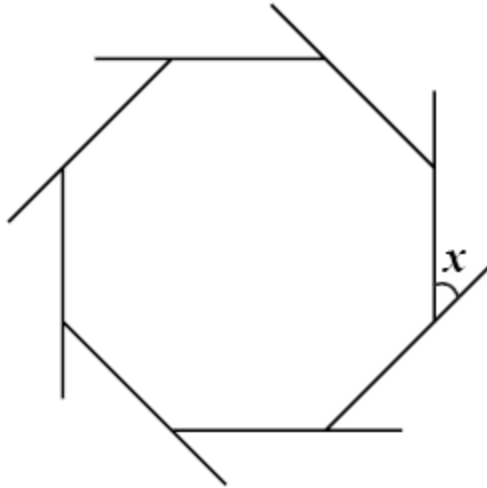
- $x$  is small acute
- use folded corner of scrap paper
- $x < 45$

What is the value of  $x$ ?

- A  $60^\circ$
- B  $45^\circ$
- C  $40^\circ$
- D  $30^\circ$**

line up angle that forms linear pair with  $x$   
 its below the mouth of the fish  $\rightarrow 150$   
 so  $180 - 150 = 30 = x$

- 28 The figure is a regular octagon with each side extended.



SSM:

- $x$  is acute
- use folded corner of scrap paper
- $x = 45$

What is the value of  $x$ ?

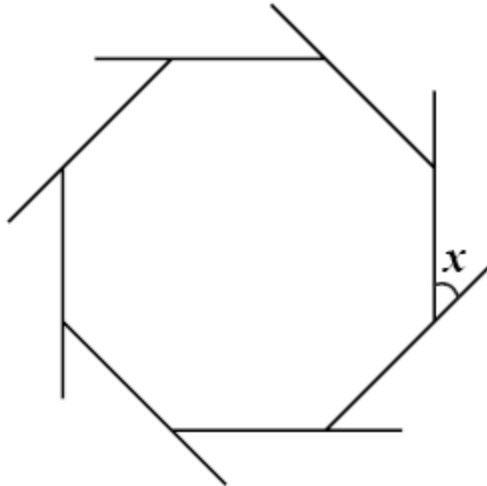
- F**  $45^\circ$   
G  $60^\circ$   
H  $75^\circ$   
J  $135^\circ$

$x$  is an exterior angle

since  $\text{ext angle} \times \text{number of sides} = 360$

then  $360 \div 8 (\text{number of sides}) = 45 = x$

- 28 The figure is a regular octagon with each side extended.



SSM:

- $x$  is acute
- use folded corner of scrap paper
- $x = 45$

What is the value of  $x$ ?

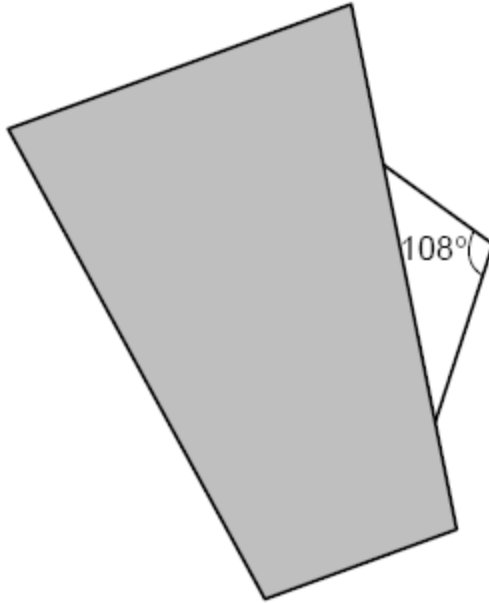
- F**  $45^\circ$   
G  $60^\circ$   
H  $75^\circ$   
J  $135^\circ$

$x$  is an exterior angle

since  $\text{ext angle} \times \text{number of sides} = 360$

then  $360 \div 8 (\text{number of sides}) = 45 = x$

- 29 In the drawing, a *regular* polygon is partially covered by the trapezoid.



SSM:

• not much help

How many sides does the covered polygon have?

- A 4  
B 5  
C 6  
D 8

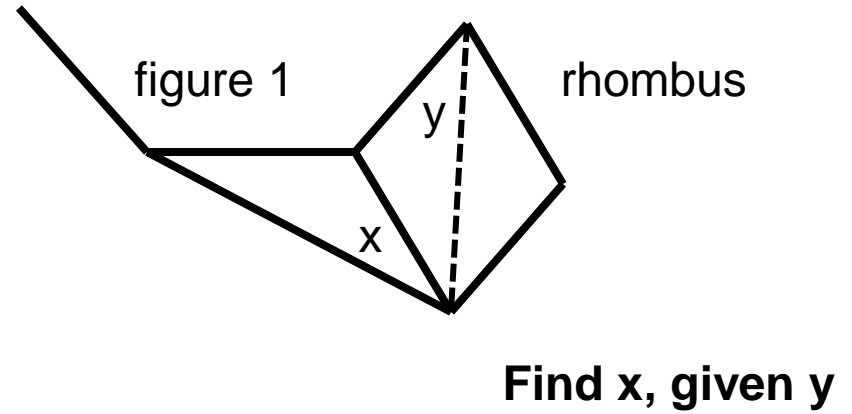
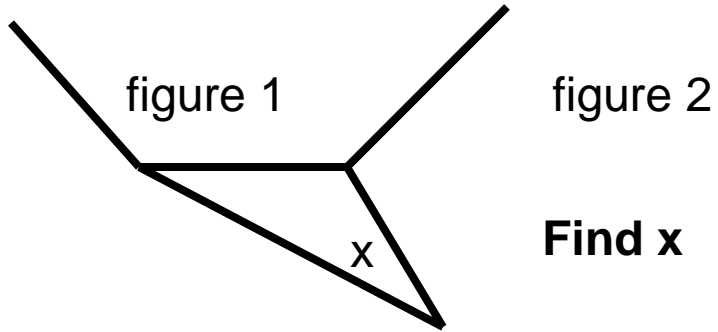
108 is an interior angle

since interior + exterior = 180, then ext = 72

then  $360 \div 72 = (\text{number of sides}) = 5 = x$

## Ideas for other problems

### Given certain regular figures



Given the number of sides,  $n$ , find the interior and exterior angles of the polygon