

Modified and Animated By Chris Headlee
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CHAPTER 9 SOL PROBLEMS

SSM: Super Second-grader Methods

SOL Problems; not Dynamic Variable Problems

40 Which line of reflection maps point K at $(-2, 2)$ to point K' at $(2, -2)$?

F $y = 2$

G $y = x$

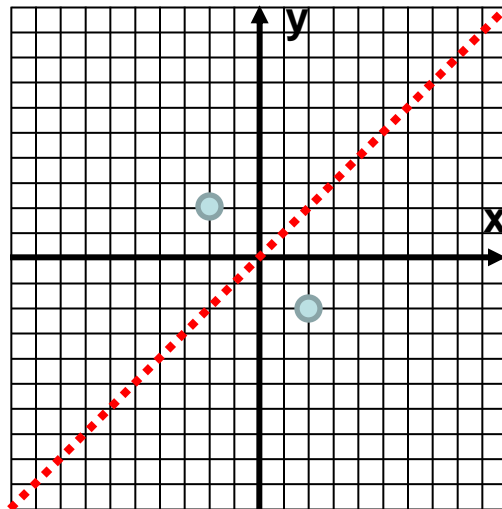
H x -axis

J y -axis

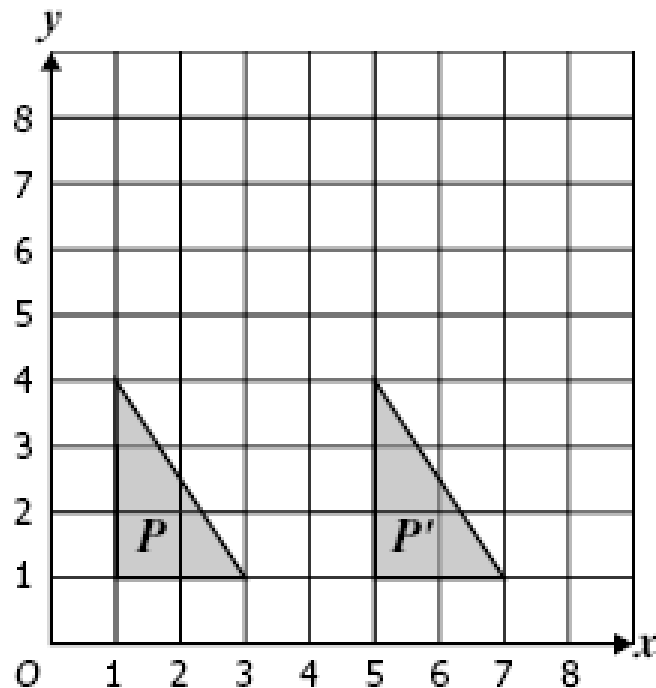
SSM:

- plot the points and the lines of reflection
- see which is equal distant

plot points and then the lines of reflection



42 Which transformation could move the triangle P to triangle P' in a single step?

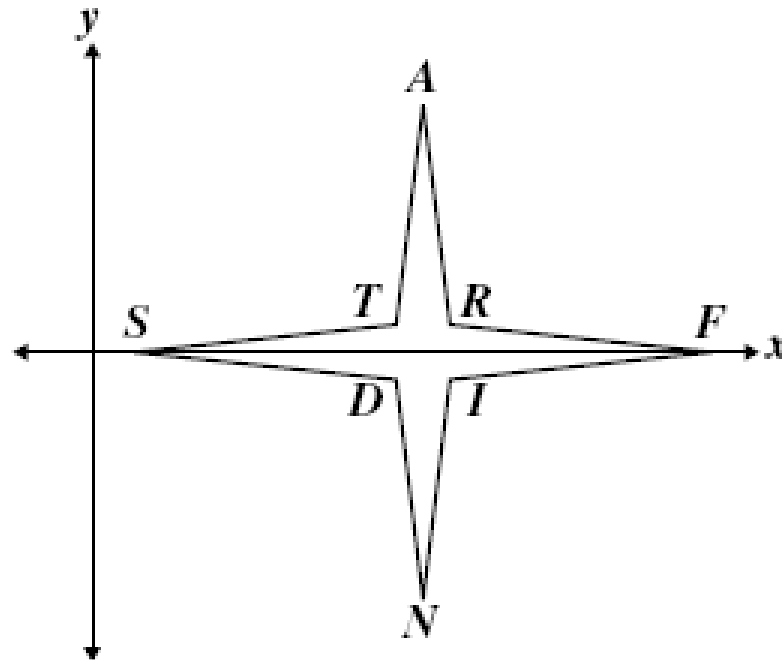


SSM:
• slide

- F Reflection over $x = 4$
- G Rotation about $(2, 3)$
- H Reflection over $y = 4$
- J** Translation

Triangle slid over \rightarrow Translation

- 43 Figure *STARFIND* is symmetric with respect to the x -axis. The coordinates of point A are $(8, 6)$. What are the coordinates of point N ?



SSM:

- fold over x -axis
- y value switches sign

- A** $(8, -6)$
B $(6, -8)$
C $(-6, 8)$
D $(-8, 6)$

symmetric to x -axis is $(-1) \times y$ -value

45 A regular quadrilateral has what type of symmetry? **Coordinate Relations and Transformations**

- A** Line symmetry only
- B** Point symmetry only
- C** Both point and line symmetry
- D** Neither point nor line symmetry

SSM:

- **draw figure**
- **draw lines of symmetry**

Regular quadrilateral is a square and has four lines of symmetry
Even numbered regular polygons have a point of symmetry

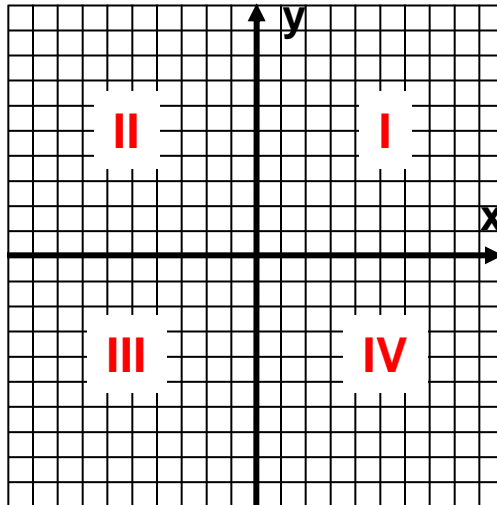
- 40 A trapezoid is located entirely in quadrant II. If this trapezoid is reflected across the x -axis, in which quadrant will the new trapezoid be located?

F I
G II
H III
J IV

SSM:

- plot an example
- flip

flip it over the x axis and it goes to the 3 quadrant



42 Which of the following letters has both line symmetry and point symmetry?

S D M H

F S

G D

H M

J H

SSM:

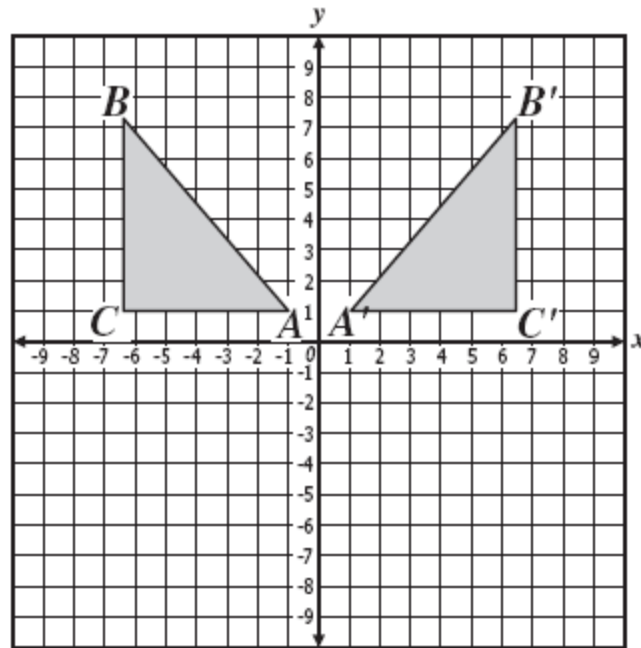
• no help

M has a line of symmetry

S and D do not have a line of symmetry

H has two lines of symmetry and a point of symmetry
(at the intersection of the two lines)

- 43 Triangle ABC was transformed into triangle $A'B'C'$. Which term most accurately describes this transformation?

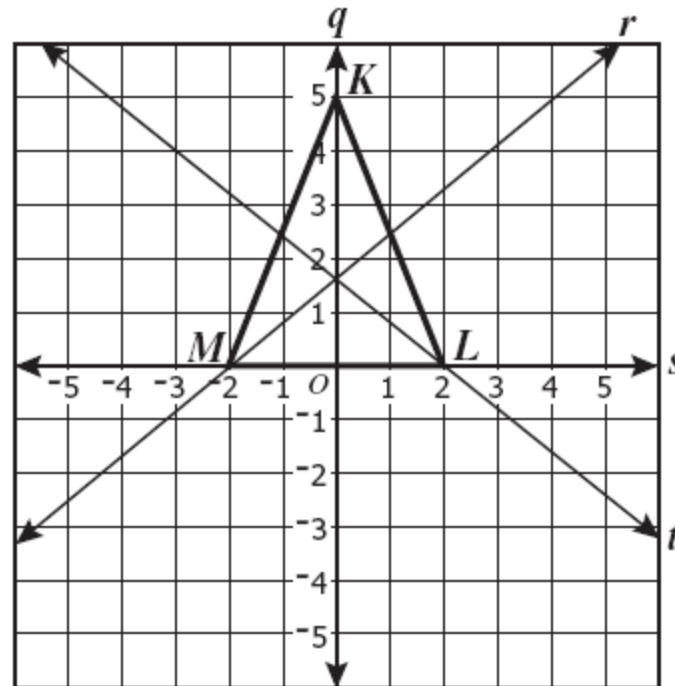


SSM:

- orientation changed
- flip or turn
- folded over y-axis

- A** Tessellation
B Reflection
C Rotation
D Translation

Since A was closest to y-axis and A' is closest to y-axis, a reflection or flip occurred



SSM:

- which line can the triangle be folded in half over

Which is most likely a line of symmetry for triangle KLM ?

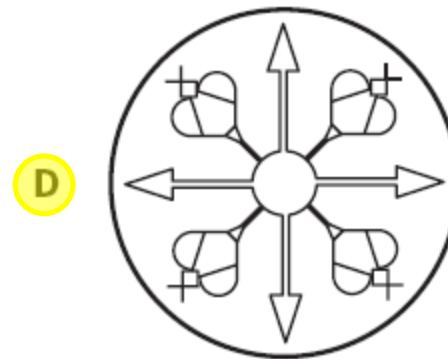
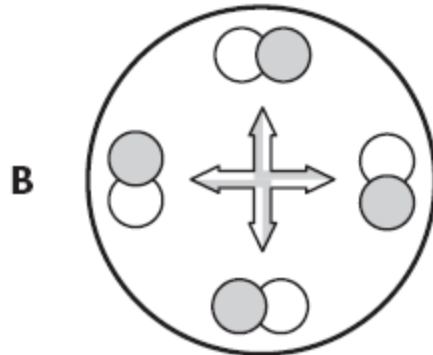
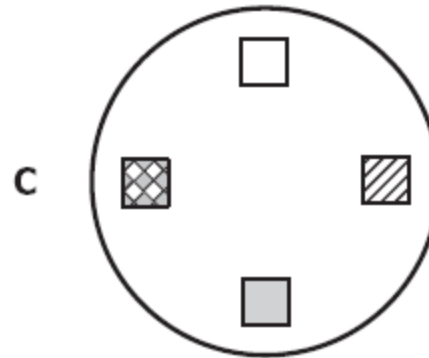
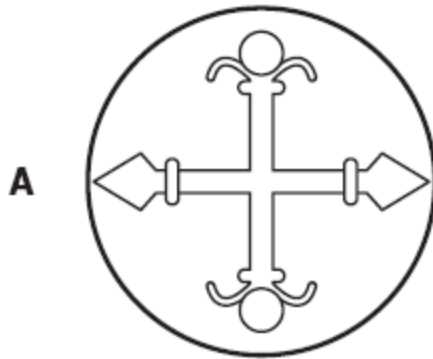
- A** q
- B** r
- C** s
- D** t

Only line q allows the figure to be folded in half perfectly

- 41 Janelle is looking at plate designs. Which design has exactly 4 lines of symmetry?

SSM:

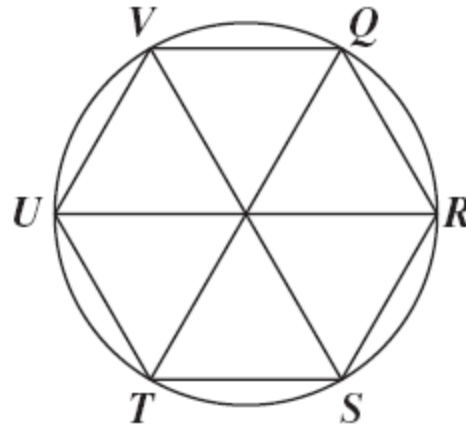
- look for pattern that repeats 4 times



Eliminate answers:

- A. only 2 lines of symmetry (pattern repeats twice)
- B. no lines of symmetry (no pattern)
- C. shaded circles mess up repeating patterns
- D. pattern repeats in all four quadrants

42 In the design, a hexagon is inscribed in a circle.



SSM:

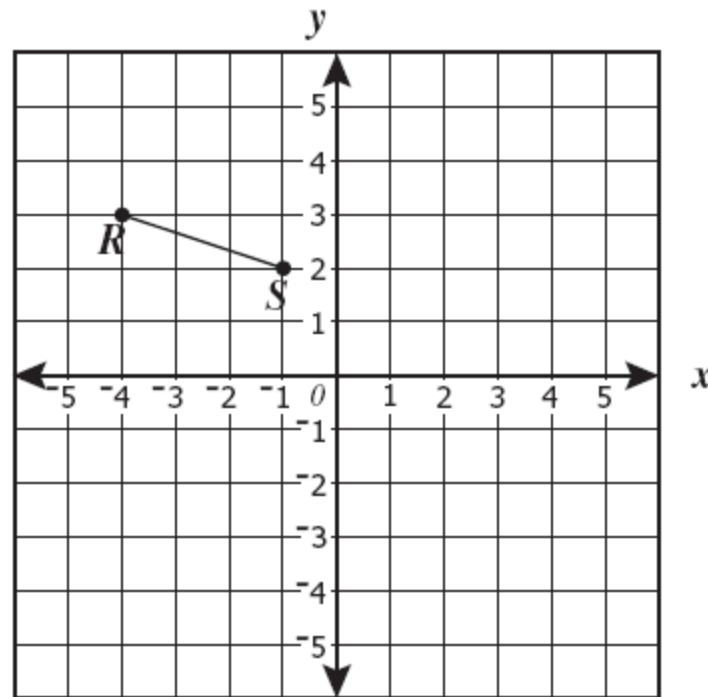
- draw a compass with Q as North
- answer between South (T) and West (between U & V)

Which point shows the location of Point Q after a 240° clockwise rotation around the center?

- F S
- G T
- H U**
- J V

Clockwise rotation is in the RS direction from Q
180 is at point T
270 is between U&V

43



SSM:

- fold \overline{RS} over y -axis in your mind
- plot answer points on graph

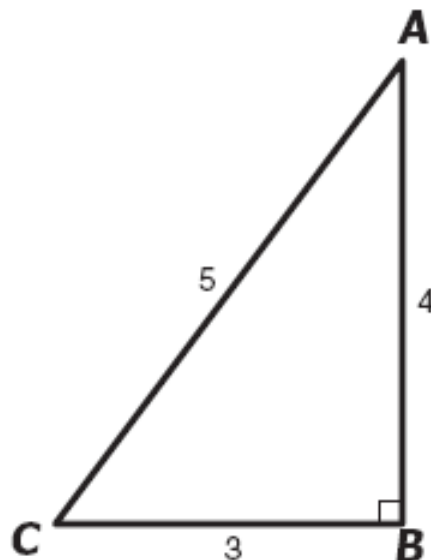
What are the *most* likely coordinates of R' if $\overline{R'S'}$ is a reflection of \overline{RS} across the y -axis?

- A** $(4, 3)$
- B** $(-4, -3)$
- C** $(4, -3)$
- D** $(3, 4)$

Equal distant from y -axis or $(x, y) \rightarrow (-x, y)$

$(-4, 3) \rightarrow (4, 3)$

40 Right triangle ABC has the measures shown.



SSM:

- How can the triangle be folded in half?
- It can't!

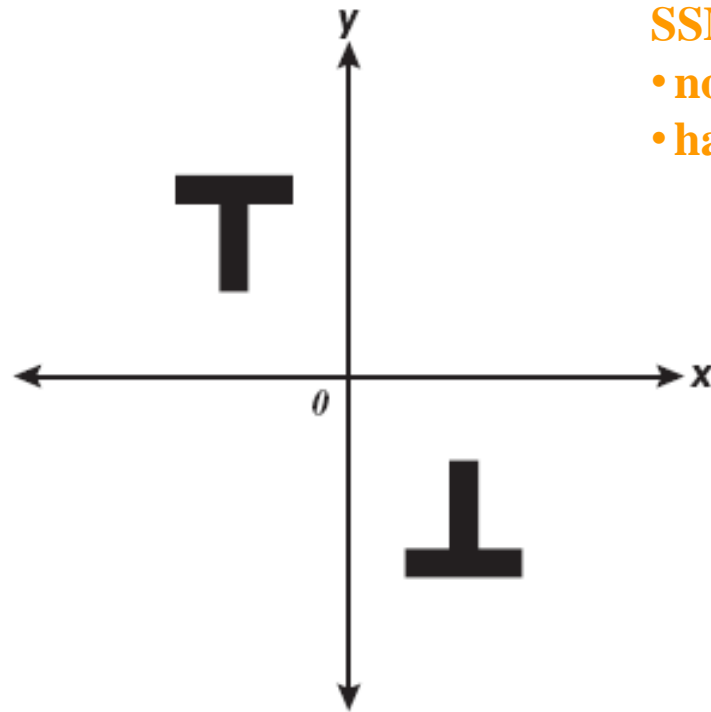
What is the *maximum* number of different lines of symmetry that can be drawn through $\triangle ABC$?

- F** 0
G 1
H 2
J 3

line of symmetry means to be able to fold in half

scalene triangles can not be folded in half
so no lines of symmetry

42

**SSM:**

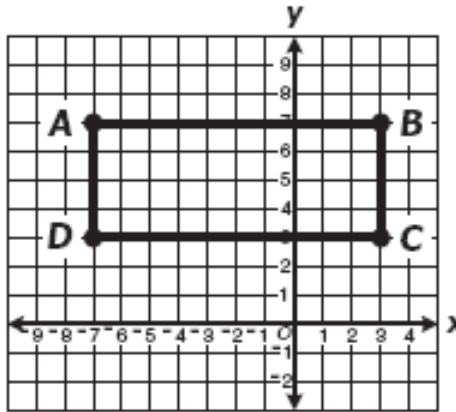
- not a reflection across a line!
- half way around the origin

In relation to one figure, the other figure is apparently a —

- F** reflection across the line $y = 1$
- G** reflection across the line $y = x$
- H** 90° rotation about the origin
- J** 180° rotation about the origin

reflection across the origin is the same as a 180° rotation about the origin

44 Rectangle $ABCD$ is placed in a coordinate plane as shown.



SSM:

- graph each answer
- which cuts rectangle in half?

Which equation describes a line of symmetry for rectangle $ABCD$?

F $x = 2$

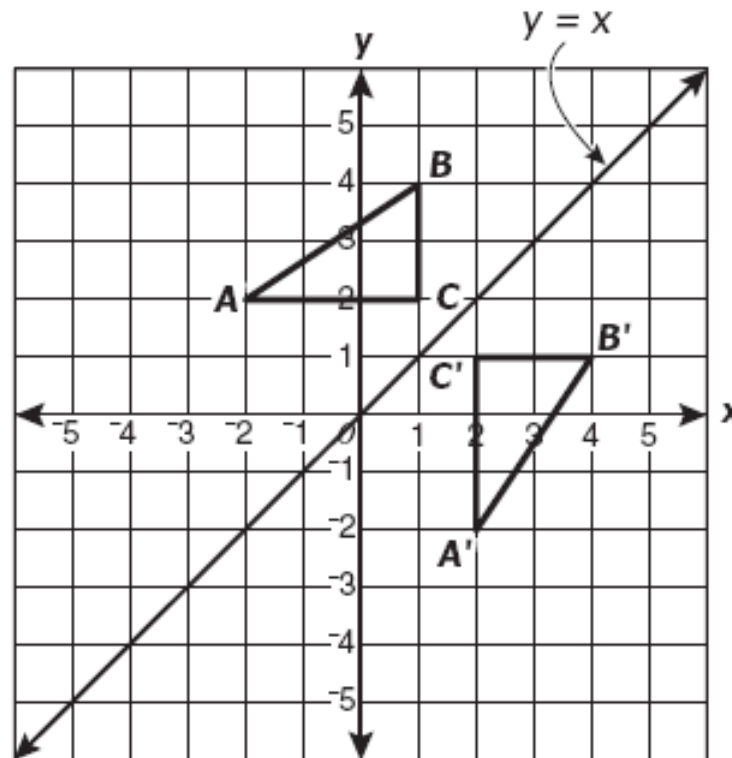
G $x = 5$

H $y = 5$

J $y = x$

Line $y = 5$ cuts the rectangle into two halves

so it is a line of symmetry



SSM:

- reflections \rightarrow equal distance
- folded over line $y = x$

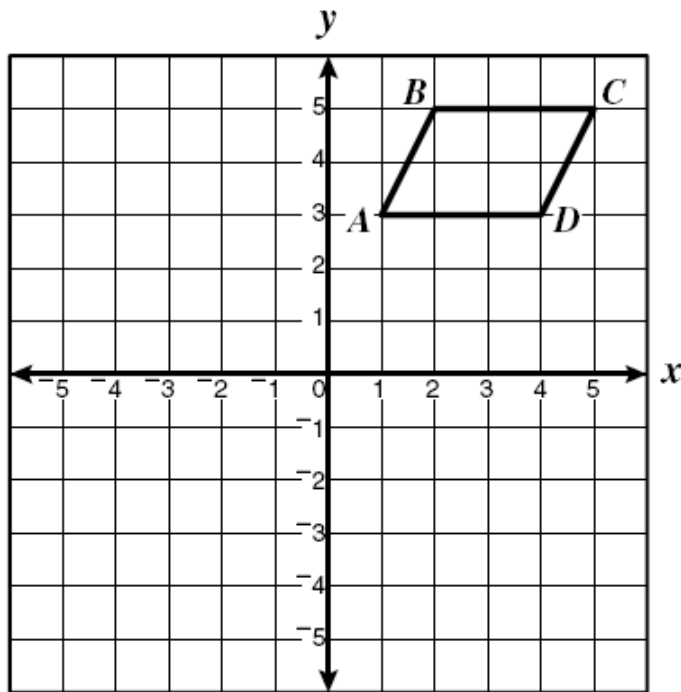
$\triangle A'B'C'$ is apparently the result of —

- A reflecting $\triangle ABC$ across the y -axis
- B reflecting $\triangle ABC$ across the x -axis
- C rotating $\triangle ABC$ about the point $(1, 2)$
- D** reflecting $\triangle ABC$ across the line $y = x$

reflection across line $y = x$

points and their reflections are
equal distance from line of reflection

40

**SSM:**

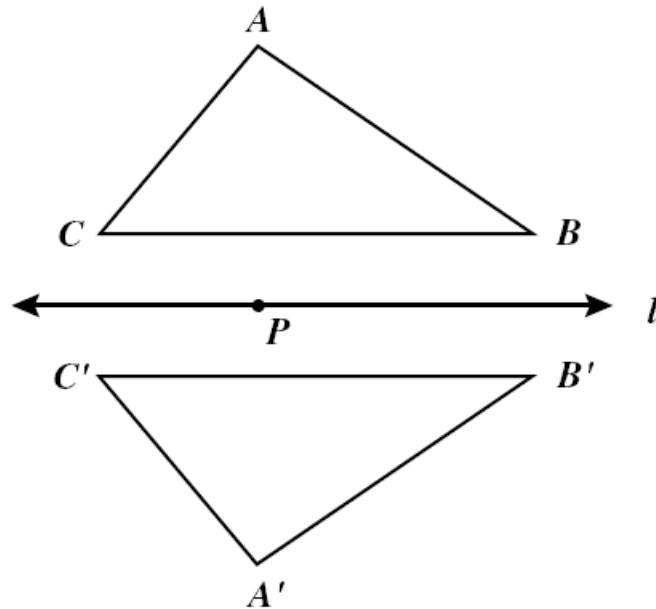
- copy figure on graph paper
- use scrap paper and copy figure and move D to new location

If parallelogram $ABCD$ is translated so that the new location of point D is $(-1, 2)$, what would be the new location of point B ?

- F $(-5, 0)$
- G $(-3, 4)$**
- H $(-2, 5)$
- J $(1, 4)$

- from D to B is left 2 and up 2
- from $(-1, 2)$ do the same

- 41 Triangle $A'B'C'$ is a transformation of triangle ABC .



If $A \rightarrow A'$, $B \rightarrow B'$, and $C \rightarrow C'$, $A'B'C'$ is a —

- A** reflection of triangle ABC across line l
- B 180° rotation of triangle ABC about Point P
- C translation of triangle ABC across the line l
- D 90° rotation of triangle ABC across the line l

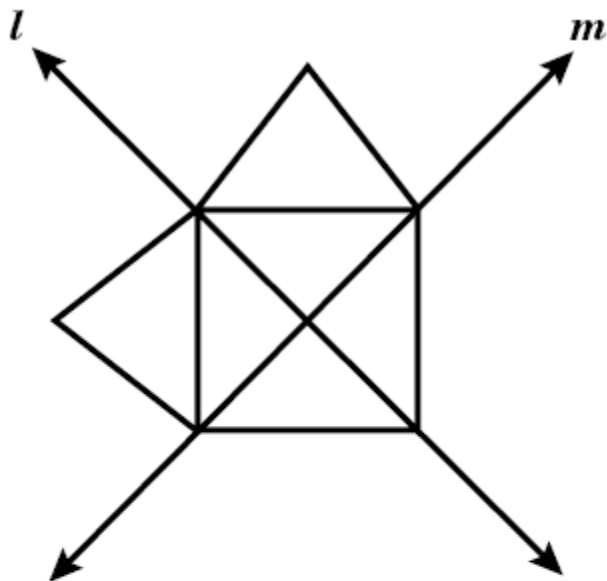
SSM:

- orientation changed for A , but not for C or B \rightarrow reflection

- Have to check each answer to see which is correct

- Answer A

44



The figure shown is apparently symmetric with respect to —

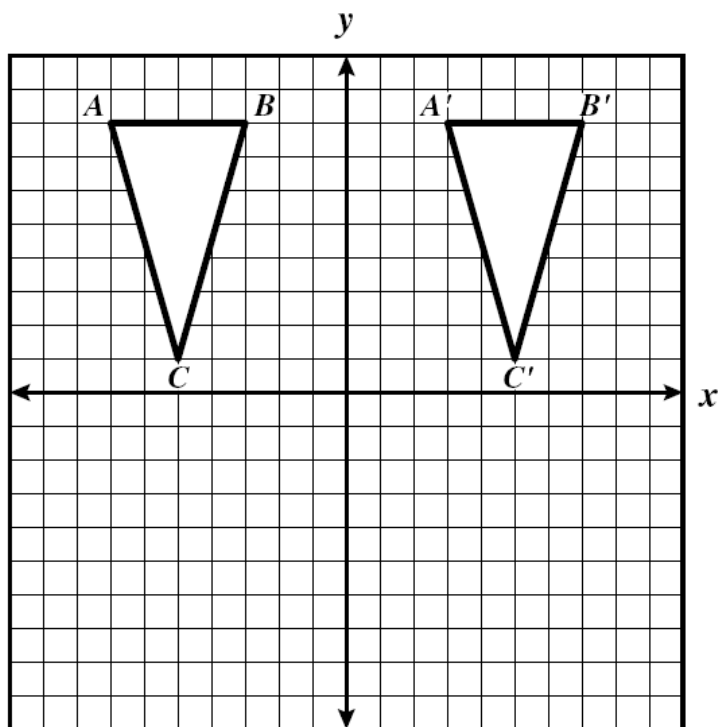
- F** line l only
- G line m only
- H both lines l and m
- J neither line l nor line m

SSM:

- copy figure on graph paper
- fold over the lines

- line of symmetry must have the same things on both sides

42



SSM:

• slide

check each answer:

A – correct

B – same orientation, so no rotation

C – A and A' still on left → no reflection

D – same side of x-axis

Triangle $A'B'C'$ is —

- F** a translation of triangle ABC across the y -axis
- G** a 90° clockwise rotation of triangle ABC about the origin
- H** a reflection of triangle ABC across the y -axis
- J** a reflection of triangle ABC across the x -axis

43 How many different lines of symmetry does a square have?

A 1

B 2

C 3

D 4

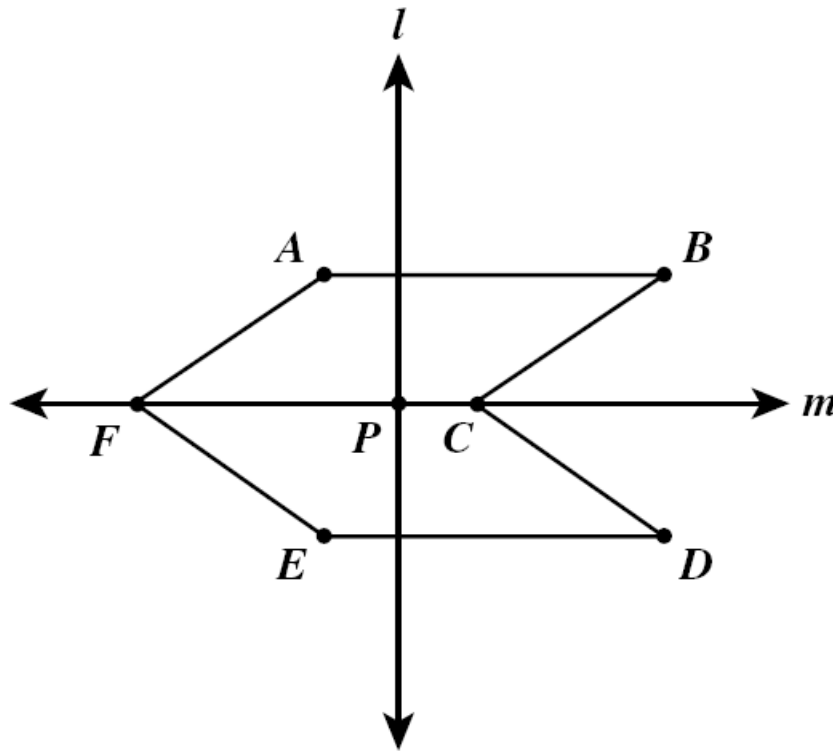
SSM:

• **draw a square and its lines of symmetry**

Regular polygons have the same number of sides as lines of symmetry

so $n = 4$

45



SSM:

- fold figure in half over lines
- draw lines connecting corners through P

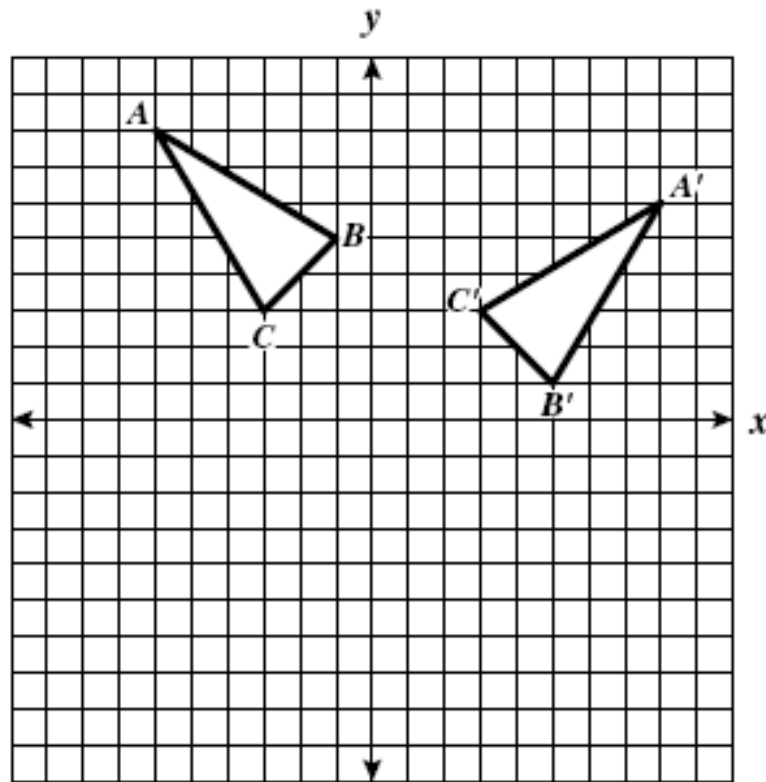
Hexagon $ABCDEF$ is apparently symmetric with respect to —

- A point P only
- B line m only**
- C line l only
- D both lines l and m only

Line m is the only symmetric item in picture

you can fold the figure in half over it and get the match ups

41

**SSM:**

- no much help

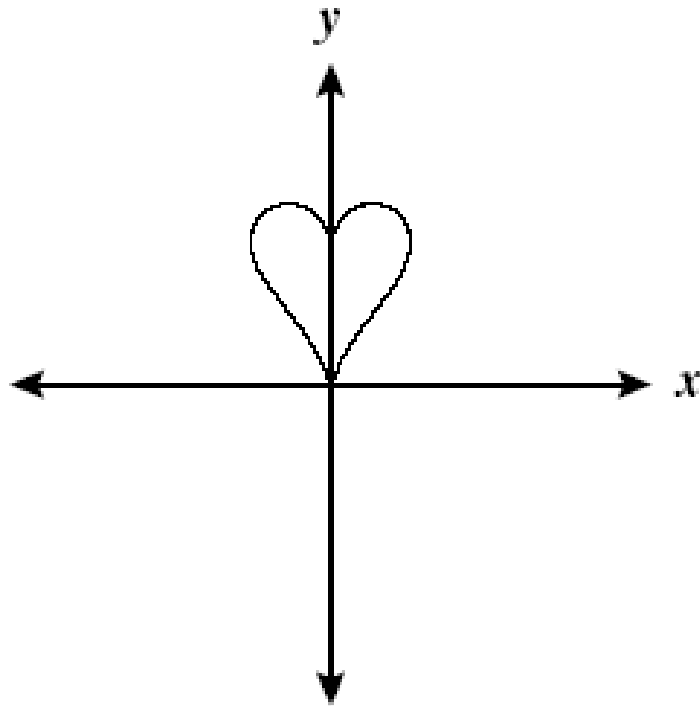
not a reflection or a translation →
orientation of the figure changes

clockwise rotation

Triangle $A'B'C'$ is apparently —

- A a translation of triangle ABC across the x -axis
- B** a 90° clockwise rotation of triangle ABC about the origin
- C a reflection of triangle ABC across the y -axis
- D a reflection of triangle ABC across the x -axis

43

**SSM:**

- fold figure in half
- which line does it fold over?

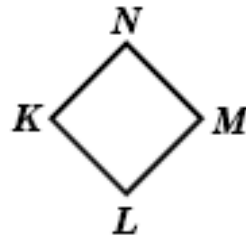
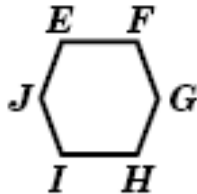
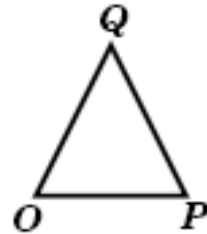
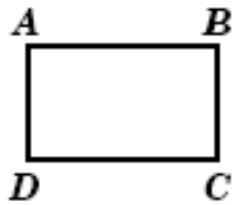
This figure is apparently symmetric with respect to —

- A the x -axis only
- B the y -axis only**
- C both the x -axis and the y -axis
- D neither the x -axis nor the y -axis

Line $x = 0$, y -axis, cuts the heart into two halves

so it is a line of symmetry

40



SSM:

- copy figures and draw in lines of symmetry

Which polygon shown above has only one line of symmetry?

- F Rectangle $ABCD$
- G Hexagon $EFGHIJ$
- H Square $KLMN$
- J** Triangle OPQ

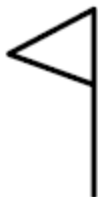
Rectangles have two

Hexagons have at least two (regular ones have 6)

Squares have four

Triangle have at most three (isosceles have 1!)

41 Consider this figure.



SSM:

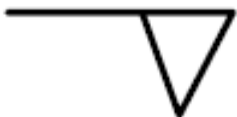
- draw figure on scrap paper and rotate the paper
- see which answer fits

Which of the following is a rotation in the plane of the given figure?

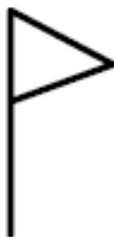
A



B



C

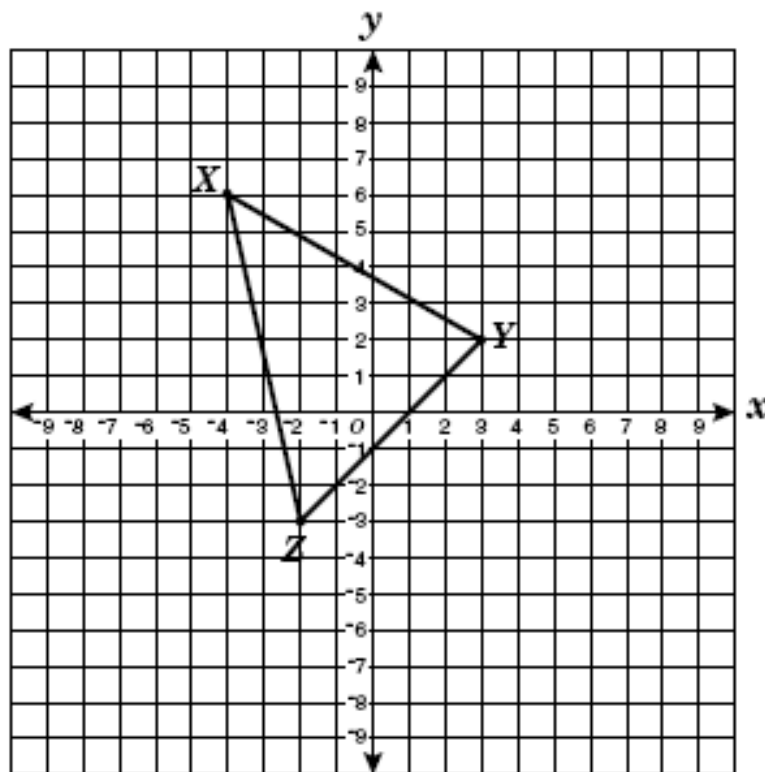


D



Rotations keep orientation within figure same
The point of the flag is to the left of the stick
as it rotates it either trails (clockwise) or leads (counterclockwise)

42

**SSM:**

- Plot points at see which is Y reflected across y-axis

If triangle XYZ is reflected across the y-axis to form triangle $X'Y'Z'$, what is the coordinate of Y' ?

F $(-3, 2)$

G $(4, 6)$

H $(2, -3)$

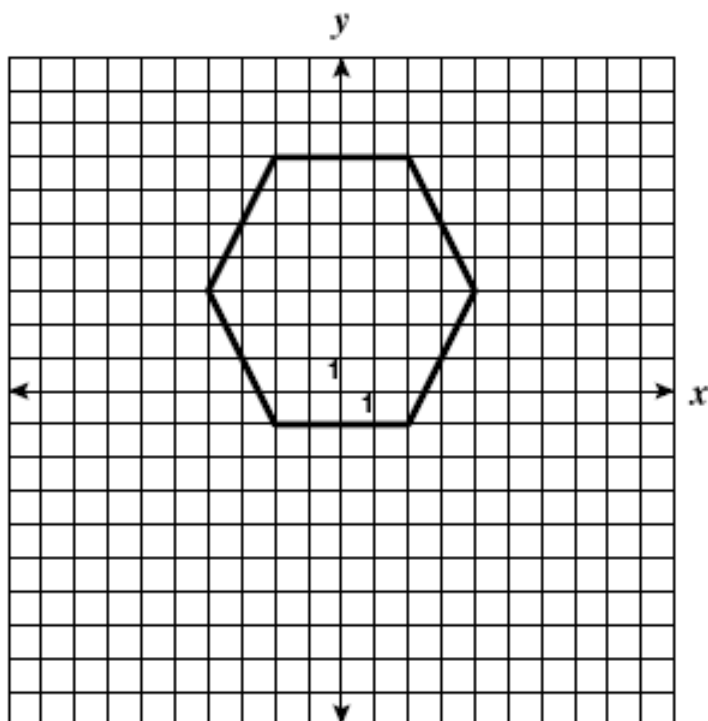
J $(3, -2)$

reflections are equal distant from reflection line

Y was 3 away from y-axis, (y-value stays at 2)

Y' is -3 away from y-axis

- 40 All the vertices of the hexagon have integral coordinates.



SSM:

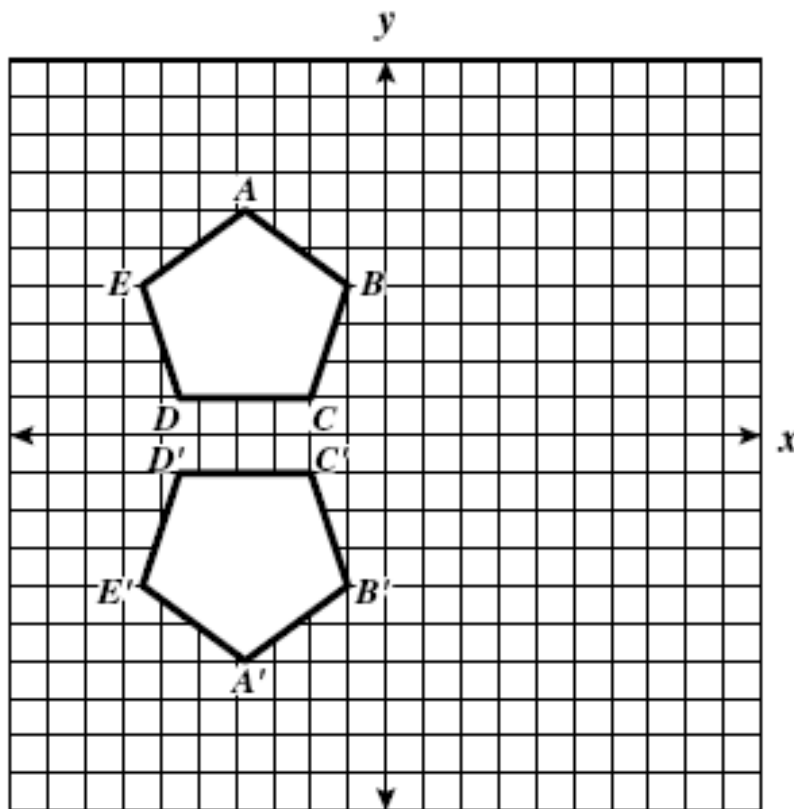
- graph each line from pair of points
- see which is a line of symmetry

One of the lines of symmetry for the hexagon goes through —

- F** $(-4, 3)$ and $(4, 3)$
- G $(-2, -2)$ and $(2, 7)$
- H $(-2, 7)$ and $(2, -2)$
- J $(2, -2)$ and $(-2, -7)$

Answer F is a horizontal line of symmetry

41



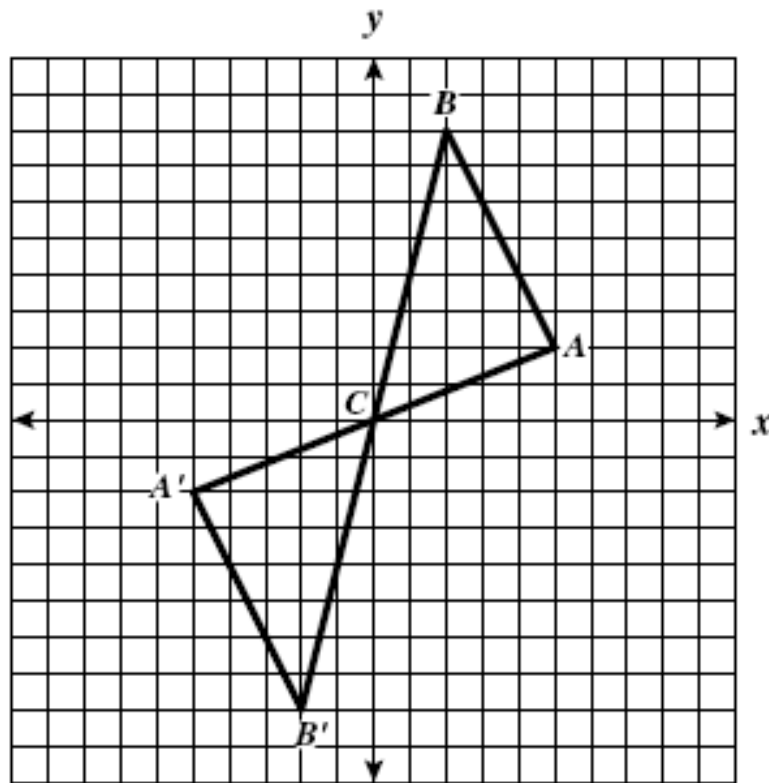
SSM:

• no help

The polygon $A'B'C'D'E'$ is —

- A a translation of $ABCDE$ across the x -axis
- B a 180° clockwise rotation of $ABCDE$ about the origin
- C a reflection of $ABCDE$ across the y -axis
- D** a reflection of $ABCDE$ across the x -axis

the pentagon has been reflected
across the x -axis



Triangle $A'B'C$ is —

- F a translation of triangle ABC across the y -axis
- G** a 180° rotation of triangle ABC about the origin
- H a reflection of triangle ABC across the y -axis only
- J a reflection of triangle ABC across the x -axis only

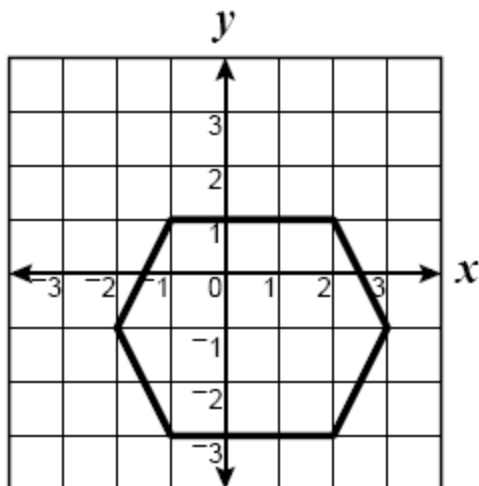
SSM:

- translation \rightarrow no
- reflection across axis \rightarrow no
- must be rotation

The figure is a reflection across the origin

Reflections across the origin are the same as 180° rotations about the origin

41

**SSM:**

- draw picture on graph paper
- draw lines of symmetry (splitting figure in half)
- see which answer fits

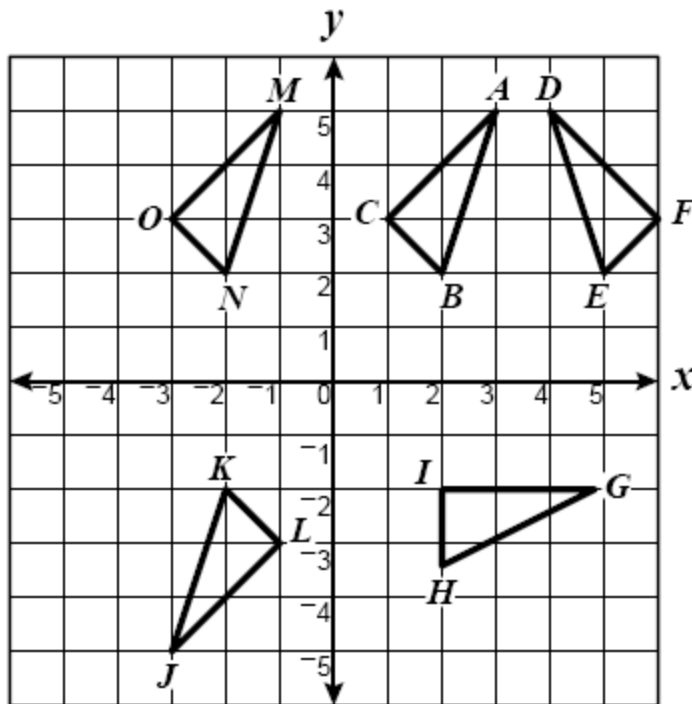
The hexagon in the drawing has a line of symmetry through —

- A $(-1, -3)$ and $(2, 1)$
- B $(1, 1)$ and $(1, -3)$
- C $(2, 3)$ and $(2, -3)$
- D** $(-2, -1)$ and $(3, -1)$

lines of symmetry cut figure in half
since it is not a regular hexagon (all sides not equal), it will have less than 6 lines of symmetry

$y = -1$ is a horizontal line of symmetry and
 $x = \frac{1}{2}$ is a vertical line of symmetry

42



SSM:

• 180 is halfway of 360

Which triangle is a 180° rotation about the origin of triangle ABC ?

F $\triangle DEF$

G $\triangle GHI$

H $\triangle JKL$

J $\triangle MNO$

180° rotation is same as a flip across origin going from QI to QIII