

1-3 Graphs of Functions

What will you learn?

- To find the Domain and Range of functions
- To use Vertical Line Test for function
- To determine intervals on which functions are
increasing
decreasing
constant
- To determine relative maximum and relative minimum values of functions
- To identify and graph step functions and other piecewise-defined functions
- To identify even and odd functions

The graph of a function f is the collection of ordered pairs

$$(x, f(x))$$

such that x is the domain of f

x = distance from the y -axis

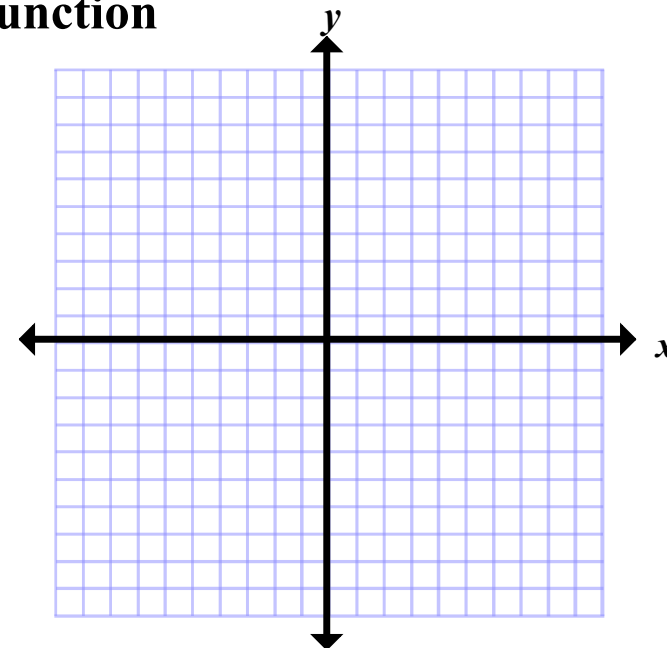
$f(x)$ = distance from the x -axis

Example 1 - Finding the Domain and Range of a Function

a.) find the Domain of f

b.) find $f(-1)$ and $f(2)$

c.) find the Range of f



See p. 38; exercise 3

Example 2 - Finding the the Domain and Range of a Function

Find the domain and range of

$$f(x) = \sqrt{x - 4}$$

Algebraic

Graphical

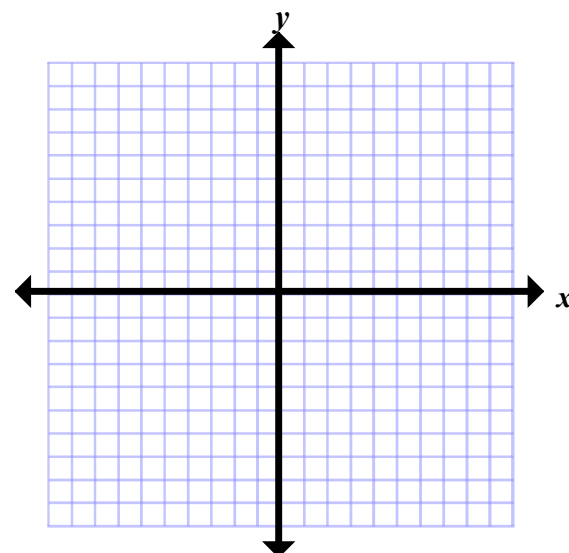
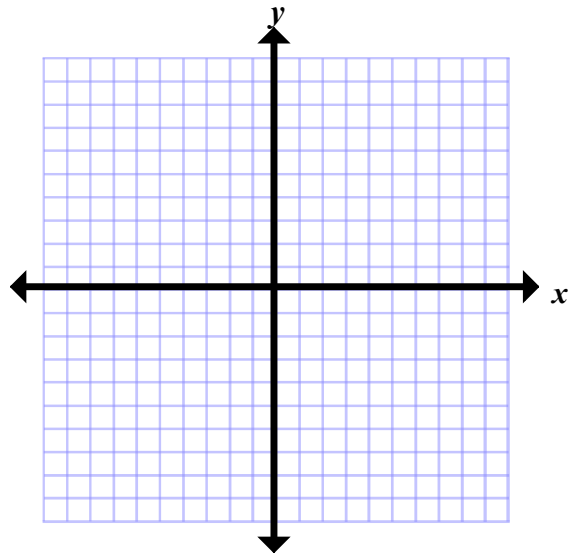
See p. 38; exercise 7

Vertical Line Test

A set of points in a coordinate plane is the graph of y as a function of x if and only if no vertical line intersects the graph at more than one point.

Example 3 - Vertical Line Test for Functions

Use the vertical line test to decide whether the graphs represent y as a function of x



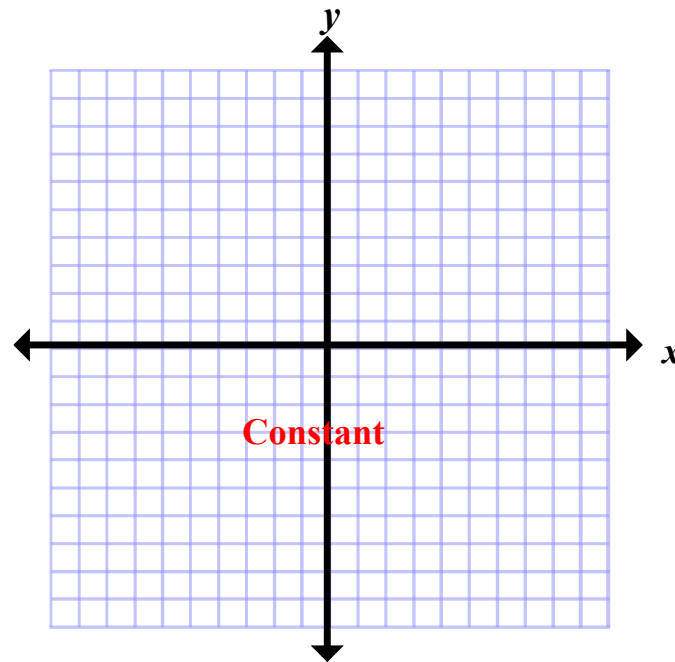
See. p. 38; exercise 13

Increasing and Decreasing Functions

- Increasing :

- Decreasing :

- Constant :

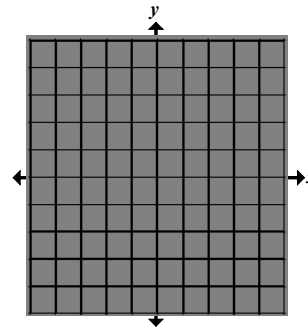


Decreasing

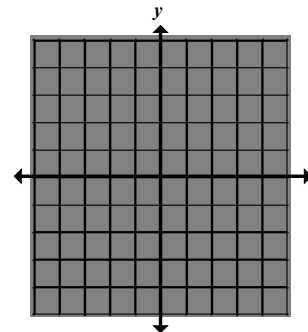
Example 4 - Increasing and Decreasing Functions

Determine the open intervals on which each function is increasing, decreasing or constant

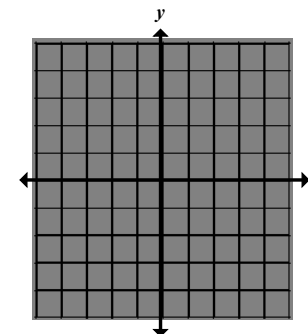
a.) $f(x) = x^3$



b.) $f(x) = x^3 - 3x$



c.) $f(x) = \begin{cases} x+1, & x < 0 \\ 1, & 0 \leq x \leq 2 \\ -x+3, & x > 2 \end{cases}$



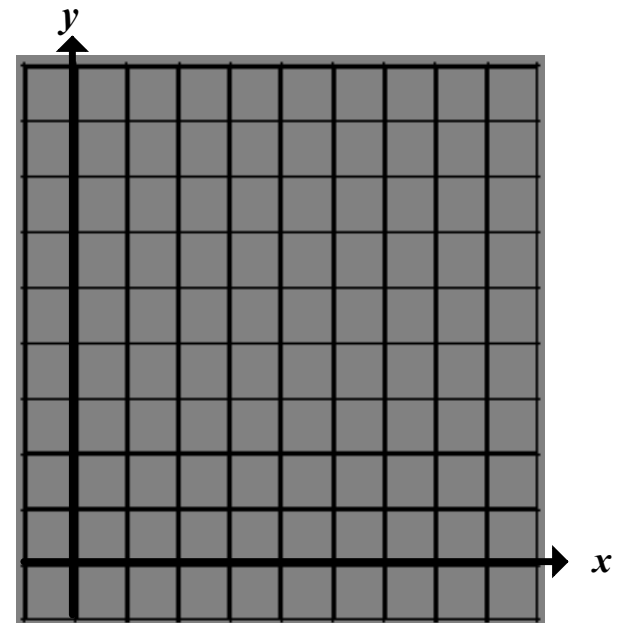
See p. 39; exercise 19

Relative Minimum and Maximum Values

The points at which a function changes its increasing, decreasing or constant behavior are helpful in determining relative maximum or relative minimum values

- A function value $f(a)$ is a Relative Minimum of f if

- A function value $f(a)$ is a Relative Maximum of f if

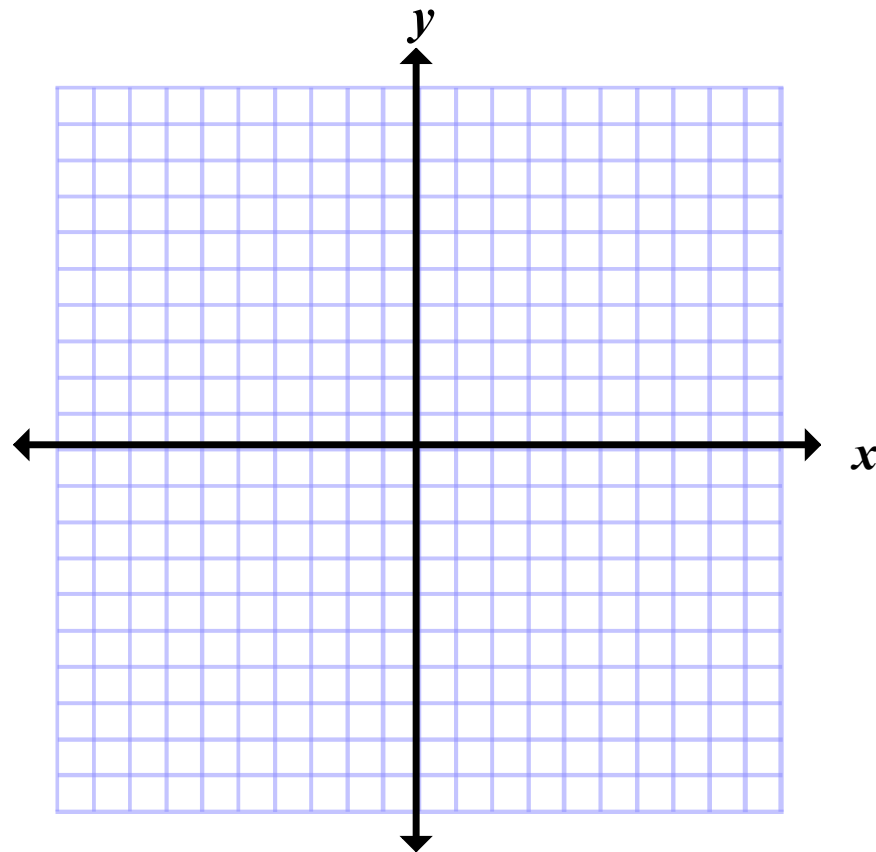


Example 5 - Approximating a Relative Minimum

Use a graphing utility to approximate the relative minimum of the function :

$$f(x) = 3x^2 - 4x - 2$$

(Use zoom and trace features)



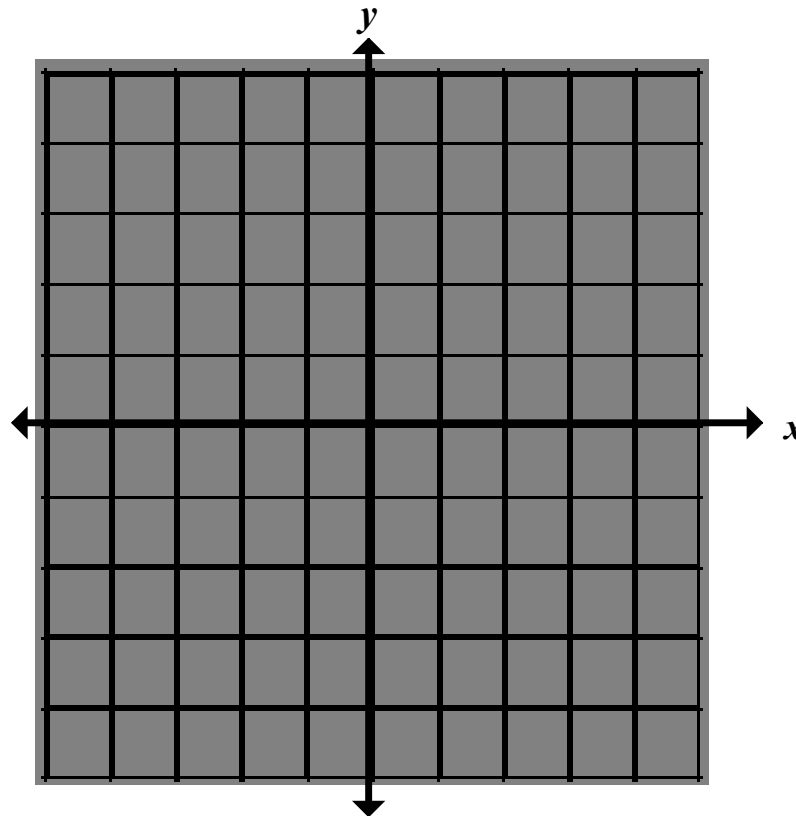
See p. 39; exercise 29

Example 6 - Approximating Relative Maxima and Minima

Use a graphing utility to approximate the relative minimum and relative maximum of the function:

$$f(x) = -x^3 + x$$

Use zoom and trace features
or
minimum and maximum features



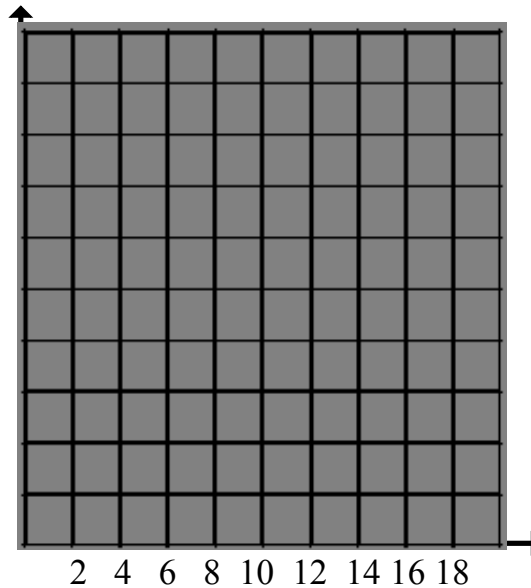
See p. 39; exercise 31

Example 7 - Temperature

During a 24-hour period, the temperature y (in degrees Fahrenheit) of a certain city can be approximated by the model

$$y = 0.026x^3 - 1.03x^2 + 10.2x + 34$$

where x represents the time of day, with $x = 0$ corresponding to 6:00 a.m.
Approximate the maximum and minimum temperatures during the 24-hour period.



Use zoom and trace
or
maximum and minimum features

See p. 40; exercise 87

Graphing Step Functions & Peicewise-Defined Functions

Step Function : Greatest Integer Function

$$\llbracket x \rrbracket \longrightarrow$$

$$f(x) = \llbracket x \rrbracket$$

Use *dot mode* on graphing calc.

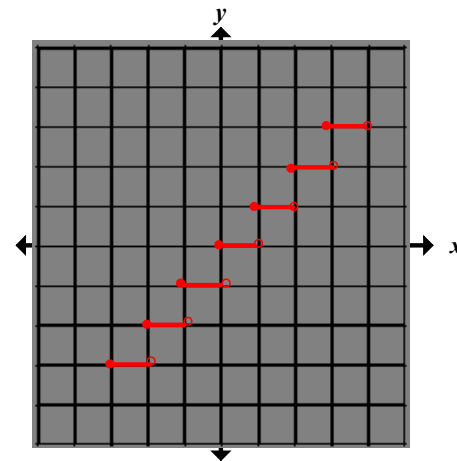
Domain:

Range :

x - intercepts:

y - intercept:

Behavior :



$$\llbracket -1 \rrbracket$$

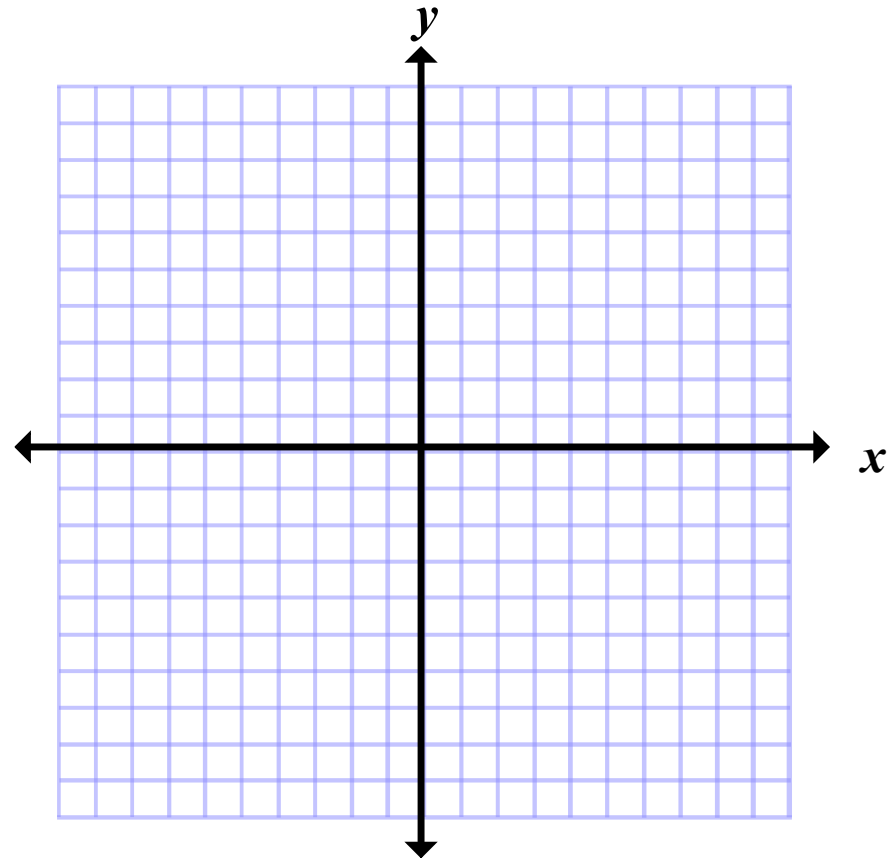
$$\llbracket \frac{1}{10} \rrbracket$$

$$\llbracket 1.5 \rrbracket$$

Example 8 - Graphing a Piecewise-Defined Function

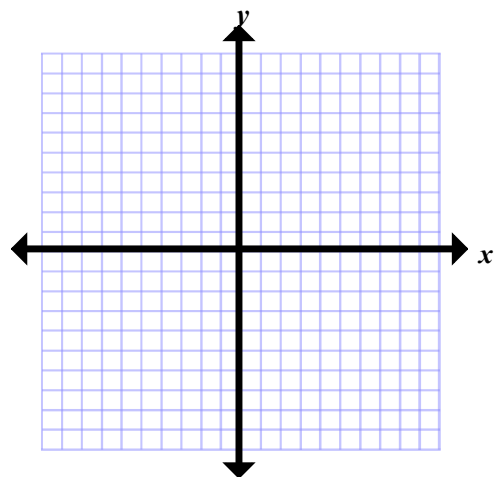
Sketch the graph of $f(x) = \begin{cases} 2x + 3, & x \leq 1 \\ -x + 4, & x > 1 \end{cases}$

What is $f(1)$?

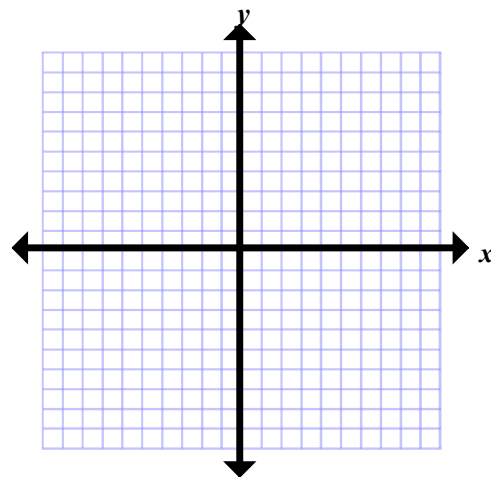


See p. 39; exercise 41

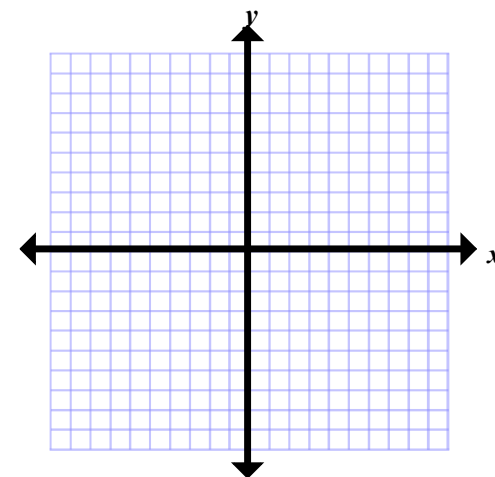
Even & Odd Functions



Symmetric to y - axis
Even Function



Symmetric to Origin
Odd Function



Symmetric to x -axis
NOT a Function

Test for Even & Odd Functions

- A function f is EVEN if
- A function f is ODD if

Even $f(-x) = f(x)$

Odd $f(-x) = -f(x)$

Example 9 - Testing for Evenness & Oddness

Is the function $f(x) = |x|$ odd, even or neither?

Algebraic

Graphical

See p. 39; exercise 49

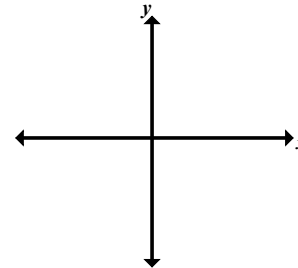
Example 10 - Even & Odd Functions

Determine whether each function is even, odd or neither.

a.) $g(x) = x^3 - x$

Algebraic

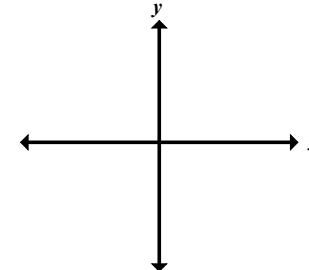
Graphical



b.) $h(x) = x^2 + 1$

Algebraic

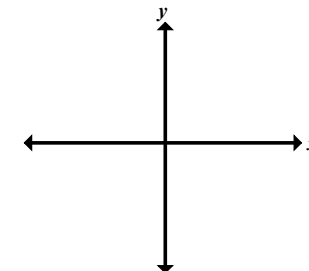
Graphical



c.) $f(x) = x^3 - 1$

Algebraic

Graphical



See p. 39; exercise 51