

9.7: Factor Special Products

Goals: *Recognize when polynomials are factorable by special products formulas

****RECALL****

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

$$(a + b)(a - b) = a^2 - b^2$$

What do all three have in common? They all start and end with perfect squares

****The important one to recognize is: $a^2 - b^2$ (the other two can be factored using the methods we have already learned, this one cannot)**

Factor:

Ex: $y^2 - 16$

$$(y + 4)(y - 4)$$

Ex: $x^2 - 9$

$$(x - 3)(x + 3)$$

Ex: $25m^2 - 16$

$$(5m - 4)(5m + 4)$$

Ex: $x^2 - 49y^2$

$$(x - 7y)(x + 7y)$$

Ex: $8 - 18n^2$

$$\begin{aligned} &2(4 - 9n^2) \\ &2(2 + 3n)(2 - 3n) \end{aligned}$$

Ex: $4y^2 - 64$

$$\begin{aligned} &4(y^2 - 16) \\ &4(y + 4)(y - 4) \end{aligned}$$

Ex: $64c^2 - 16$

$$\begin{aligned} &16(c^2 - 1) \\ &16(c - 1)(c + 1) \end{aligned}$$

Ex: $x^2 - 81y^2$

$$(x + 9y)(x - 9y)$$

Ex: $12 - 48m^2$

$$\begin{aligned} &12(1 - 4m^2) \\ &12(1 + 2m)(1 - 2m) \end{aligned}$$

Ex: $n^2 - 12n + 36$

$$(n - 6)^2$$

Ex: $9x^2 - 12x + 4$

$$(3x - 2)^2$$

Ex: $4s^2 + 4st + t^2$

$$(4s + t)^2$$

Ex: $a^2 + 6a + 9$

$$(a + 3)^2$$

Ex: $4n^2 + 20n + 25$

$$(2n + 5)^2$$

Ex: $9c^2 - 6cd + d^2$

$$(3c - d)^2$$

Ex: $-3y^2 + 36y - 108$

$$\begin{aligned} & -3(y^2 - 12y + 36) \\ & -3(y - 6)^2 \end{aligned}$$

Ex: $-2x^2 - 16x - 32$

$$\begin{aligned} & -2(x^2 + 8x + 16) \\ & -2(x + 4)^2 \end{aligned}$$

Ex: $h^2 + 4h + 4$

$$(h + 2)^2$$

Ex: $2y^2 - 20y + 50$

$$\begin{aligned} & 2(y^2 - 10y + 25) \\ & 2(y - 5)^2 \end{aligned}$$

Ex: $3x^2 + 6xy + 3y^2$

$$\begin{aligned} & 3(x^2 + 2xy + y^2) \\ & 3(x + y)^2 \end{aligned}$$

Solve:

Ex: $x^2 + \frac{2}{3}x + \frac{1}{9} = 0$

$$\begin{aligned} \left(x + \frac{1}{3}\right)^2 &= 0 \\ x &= -\frac{1}{3} \end{aligned}$$

Ex: $x^2 - 5x + \frac{25}{4} = 0$

$$\begin{aligned} \left(x - \frac{5}{2}\right)^2 &= 0 \\ x &= \frac{5}{2} \end{aligned}$$

Ex: $a^2 + 6a + 9 = 0$

$$\begin{aligned} (a + 3)^2 &= 0 \\ a &= -3 \end{aligned}$$

Ex: $w^2 - 14w = -49$

$$\begin{aligned}w^2 - 14w + 49 &= 0 \\(w - 7)^2 &= 0 \\w &= 7\end{aligned}$$

Ex: $n^2 - 81 = 0$

$$\begin{aligned}(n - 9)(n + 9) &= 0 \\n &= 9, n = -9\end{aligned}$$

Ex: $x^2 = 49$

$$\begin{aligned}x^2 - 49 &= 0 \\(x + 7)(x - 7) &= 0 \\x &= 7, x = -7\end{aligned}$$

Ex: A window washer drops a wet sponge from a height of 64 feet. After how many seconds does the sponge land on the ground?

*When you drop something its initial velocity is zero!

$$\begin{aligned}h &= -16t^2 + 64 \\0 &= -16(t^2 - 4) \\0 &= -16(t + 2)(t - 2) \\t &= 2\end{aligned}$$

Ex: A rock is dropped from a riverbank that is 4 feet above the surface of the river. After how many seconds does the rock hit the water?

$$\begin{aligned}h &= -16t^2 + 4 \\0 &= -4(4t^2 - 1) \\0 &= -4(2t + 1)(2t - 1) \\t &= \frac{1}{2} \text{ seconds}\end{aligned}$$