

## 4.7: Function Notation

- \*Goals:**
- Identify function notation
  - Find the value of a function for a given value of  $x$
  - Find the value of  $x$  for a given function value
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**Function Notation:** Another way of expressing the relationship between input and output. It is simply a notation. It does NOT mean to multiply!

$f(x) = y$  ;  $x$  is still the input. Now instead of calling  $y$  the output, it is being called  $f(x)$  (y has been substituted with  $f(x)$ )

So an ordered pair that use to be written:  $(x, y)$  could now be written:  
 $(x, f(x))$

While  $f$  is typically the most common function name, other common functions are:  $g(x), h(x), \dots$

$f(x)$  DOES NOT mean to MULTIPLY \_\_\_\_\_.

- $f(7)$  would just mean to Substitute \_\_\_\_\_ 7 in for  $x$  into the given function and find the output when the input is 7

### Finding and output given an input.

**Ex:** What is the value of the function  $f(x) = 3x - 15$  when  $x = -3$ ?

- What is this problem really asking you to do? Think in terms of input and output.

This problem is really asking you to find the output, which is  $f(x)$ , when  $x$  is  $-3$ . So everywhere you see an  $x$ , substitute in  $-3$ .

$$f(-3) = 3(-3) - 15$$

$$f(-3) = -9 - 15$$

$$f(-3) = -24$$

So what this really says is that the function equals  $-24$ , when  $x = -3$ .  
You are done here.

**Ex:** Evaluate  $h(x) = -7x$  when  $x = 7$

Replace  $x$  with 7.

$$h(7) = -7(7)$$

$$h(7) = -49$$

When the input is 7 the output is  $-49$

**Ex:** What is the value of the function  $f(x) = 2x + 12$  when  $x = -8$ ?

$$f(-8) = -4$$

### Finding an input given an output.

**Ex:** For the function  $f(x) = 2x - 10$ , find the value of  $x$  so that  $f(x) = 6$ .

- What is this problem asking you to do?

This time the problem wants you to substitute 6 everywhere you see the  $f(x)$  symbol. Then solve for  $x$ . Here you know the output, you want to know the input that created it.

$$f(x) = 2x - 10$$



$$6 = 2x - 10$$

\*Now solve like a normal multi-step equation.

$$\begin{array}{r} +10 \qquad \qquad +10 \\ \hline 16 = 2x \\ 2 \quad 2 \end{array}$$

$$8 = x$$

This means that when the output was 6, the input was 8.

**Ex:** For the function  $f(x) = -2x + 4$ , find the value of  $x$  so that  $f(x) = 16$ .

$$\begin{array}{r} 16 = -2x + 4 \\ -4 \qquad \qquad -4 \\ \hline 12 = -2x \\ -2 \quad -2 \end{array}$$

$$-6 = x$$