

**Given:**  $p \parallel q, t \perp p$   
**Prove:**  $t \perp q$   
**Proof:**

Statements	Reasons
1. $p \parallel q, t \perp p$	1. Given
2. $\angle 1$ is a right angle.	2. Definition of $\perp$ lines
3. $m\angle 1 = 90$	3. Definition of right angle
4. $\angle 1 \cong \angle 2$	4. Corresponding Angles Postulate
5. $m\angle 1 = m\angle 2$	5. Definition of congruent angles
6. $m\angle 2 = 90$	6. Substitution Property
7. $\angle 2$ is a right angle.	7. Definition of right angles
8. $t \perp q$	8. Definition of $\perp$ lines

**Given:**  $a \parallel b, c \parallel d$   
**Prove:**  $\angle 1 \cong \angle 11$

**Proof:**

Statements	Reasons
$c \parallel d$	Given
$\angle 1 \cong \angle 3$	Corresponding $\angle$ s post.
$a \parallel b$	Given
$\angle 3 \cong \angle 11$	Corresponding $\angle$ s post
$\angle 1 \cong \angle 11$	Transitive prop $\cong \angle$ s

**Given:**  $m\angle 8 + m\angle 9 = 180$   
**Prove:**  $\angle 8 \cong \angle 10$

**Proof:**

Statements	Reasons
$m\angle 8 + m\angle 9 = 180$	Given
$\angle 9$ & $\angle 10$ form a linear pair	def of linear pair
$m\angle 9 + m\angle 10 = 180$	supplement theorem
$\angle 8 \cong \angle 10$	$\cong$ supplements theorem

3-5 Proving Lines Parallel (and Perpendicular)

Additional "Ingredients" for our proofs  
 - that is, "Reasons"

- If corr.  $\angle$ s are  $\cong$ , then lines are  $\parallel$ .
- If alt. int.  $\angle$ s are  $\cong$ , then lines are  $\parallel$ .
- If cons. int.  $\angle$ s are suppl., then lines are  $\parallel$ .
- If alt. ext.  $\angle$ s are  $\cong$ , then lines are  $\parallel$ .
- If 2 lines are  $\perp$  to the same line, then lines are  $\parallel$ .

**Given:**  $\ell \perp t, m \perp t$   
**Prove:**  $\ell \parallel m$

**Proof:**

Statements	Reasons
1. $\ell \perp t, m \perp t$	1. ? Given
2. $\angle 1$ and $\angle 2$ are right angles.	2. ? Def $\perp$ lines
3. $\angle 1 \cong \angle 2$	3. ? all right $\angle$ s are $\cong$
4. $\ell \parallel m$	4. ?

Postulate: If corresponding  $\angle$ s are  $\cong$ , then the lines are  $\parallel$ .

**Given:**  $r \parallel s; \angle 5 \cong \angle 6$   
**Prove:**  $\ell \parallel m$

**Proof:**

Statements	Reasons
1. $r \parallel s; \angle 5 \cong \angle 6$	1. Given
2. $\angle 4$ and $\angle 5$ are supplementary.	2. Consecutive Interior Angle Theorem
3. $m\angle 4 + m\angle 5 = 180$	3. Definition of supplementary angles
4. $m\angle 5 = m\angle 6$	4. Definition of congruent angles
5. $m\angle 4 + m\angle 6 = 180$	5. Substitution
6. $\angle 4$ and $\angle 6$ are supplementary.	6. Definition of supplementary angles
7. $\ell \parallel m$	7. If cons. int. $\angle$ s are suppl., then lines are $\parallel$ .

Given:  $\angle 9 \cong \angle 13$   
 Prove:  $c \parallel d$

Given:  $c \parallel d \quad \angle 2 \cong \angle 12$   
 Prove:  $a \parallel b$

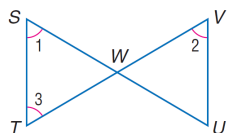
Given:  $a \perp b \quad \angle 1 \cong \angle 2$   
 Prove:  $b \perp c$

Given:  $a \perp b \quad b \perp c$   
 Prove:  $a \parallel c$

Given:  $a \parallel c \quad c \parallel d$   
 Prove:  $\angle 6 \cong \angle 12$

Given:  $a \parallel c \parallel d$   
 Prove:  $\angle 12, \angle 2, \angle 10, \angle 4, \angle 8, \angle 6$  are all congruent.

**Given:**  $\angle 2 \cong \angle 1$   
 $\angle 1 \cong \angle 3$   
**Prove:**  $\overline{ST} \parallel \overline{UV}$



**Given:**  $\overline{JM} \parallel \overline{KN}$   
 $\angle 1 \cong \angle 2$   
 $\angle 3 \cong \angle 4$   
**Prove:**  $\overline{KM} \parallel \overline{LN}$

