

Answer questions 1-5 based on the information given.  
 Show equations and setups, box your final answer.

1. What is the sum of the interior angles of a decagon?  
 $n = 10$

$$S = 180(n - 2)$$

$$S = 180(10 - 2)$$

$$\boxed{S = 1440^\circ}$$

2. What is the measure of one exterior angle of a regular 12-gon?  
 $n = 12$

$$m \text{ ext } \angle = \frac{360}{n}$$

$$= \frac{360}{12}$$

$$\boxed{m \text{ ext } \angle = 30^\circ}$$

3. What is the measure of one interior angle of a regular heptagon?  
 $n = 7$

$$S = 180(n - 2)$$

$$= 180(7 - 2)$$

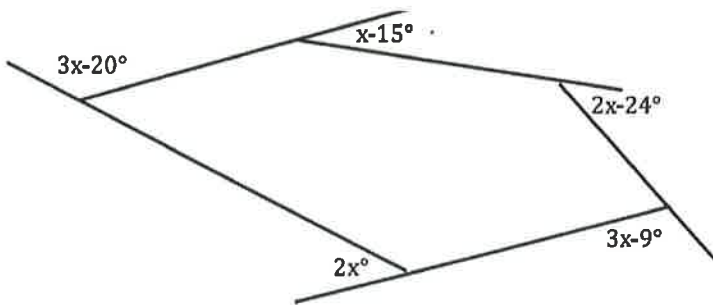
$$S = 900$$

$$m \text{ int } \angle = \frac{S}{n}$$

$$= \frac{900}{7}$$

$$\boxed{m \text{ int } \angle \approx 128.6^\circ}$$

4. Find the value of  $x$ .



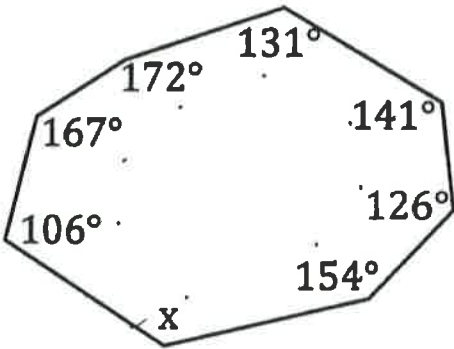
$$x - 15 + 2x - 24 + 3x - 9 + 2x + 3x - 20 = 360$$

$$11x - 68 = 360$$

$$11x = 428$$

$$\boxed{x \approx 38.9}$$

5. Find the measure of the missing angle.



$$n = 8$$

$$S = 180(n - 2)$$

$$= 180(8 - 2)$$

$$S = 1080$$

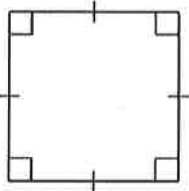
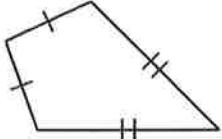
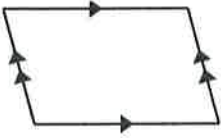
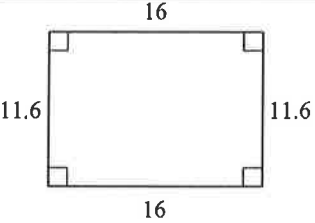
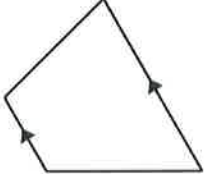
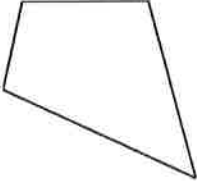
$$x + 106 + 167 + 172 + 131 + 141 + 126 + 154 = 1080$$

$$x + 997 = 1080$$

$$\boxed{x = 83^\circ}$$

For # 6-11, using the definitions that you know: *oops!* "quadrilateral" is an option, too.

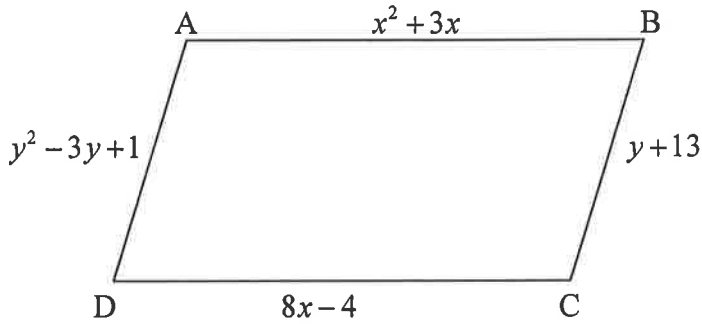
- Classify each of the figures below as a(n): *trapezoid, isosceles trapezoid, parallelogram, rectangle, rhombus, square or kite*. Write the name of the quadrilateral below the figure. There is only one correct answer for each figure.
- Give a reason for your answer.

 <p>6. <u>Square</u></p> <ul style="list-style-type: none"> <li>• 4 <math>\cong</math> sides</li> <li>• 4 right <math>\angle</math>s.</li> </ul>	 <p>7. <u>Kite</u></p> <p>2 pairs adjacent <math>\cong</math> sides</p>	 <p>8. <u>parallelogram</u></p> <p>2 pairs <math>\parallel</math> sides</p>
 <p>9. <u>Rectangle</u></p> <p>4 right <math>\angle</math>s.</p>	 <p>10. <u>trapezoid</u></p> <p>1 pair <math>\parallel</math> sides</p>	 <p>11. <u>quadrilateral</u></p> <p>4 sides</p>

12. Use  $\square ABCD$  to find  $x$  and  $y$ . Give a reason for your setups.

$x = \underline{1; 4}$

$y = \underline{-2; 6}$



Opp. Sides  $\cong$

$AB = DC$

$$\begin{aligned} x^2 + 3x &= 8x - 4 \\ x^2 + 3x - 8x + 4 &= 0 \\ x^2 - 5x + 4 &= 0 \\ (x - 1)(x - 4) &= 0 \end{aligned}$$

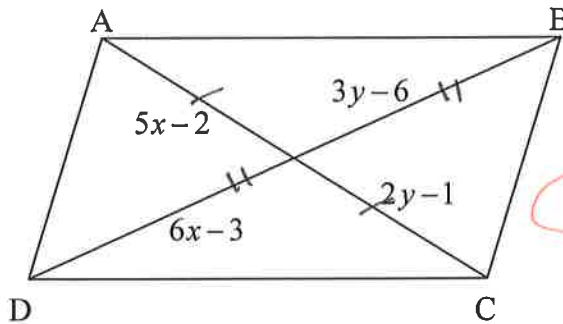
$AD = BC$

$$\begin{aligned} y^2 - 3y + 1 &= y + 13 \\ y^2 - 3y - y + 1 - 13 &= 0 \\ y^2 - 4y - 12 &= 0 \\ (y + 2)(y - 6) &= 0 \end{aligned}$$

13. Use  $\square ABCD$  to find  $x$  and  $y$ . Give a reason for your setups.

$x = \underline{5; 3}$

$y = \underline{1; 6; 7}$



$5x - 2 = 2y - 1$   
 $5x - 2y = 1$

$6x - 3 = 3y - 6$   
 $6x - 3y = -3$

Diagonals bisect each other

$5x - 2 = 2y + 1$   
 $6x - 3 = 3y - 6$

$-3(5x - 2y = 3)$   
 $2(6x - 3y = -3)$

~~$-15x + 6y = 9$   
 $12x - 6y = -6$   
 $-3x = -15$   
 $x = 5$~~

~~$5x - 2 = 2y + 1$   
 $5(5) - 2 = 2y + 1$   
 $25 - 2 - 1 = 2y$   
 $22 = 2y$   
 $11 = y$~~

$-3(5x - 2y) = -3(1)$   
 $2(6x - 3y) = 2(-3)$

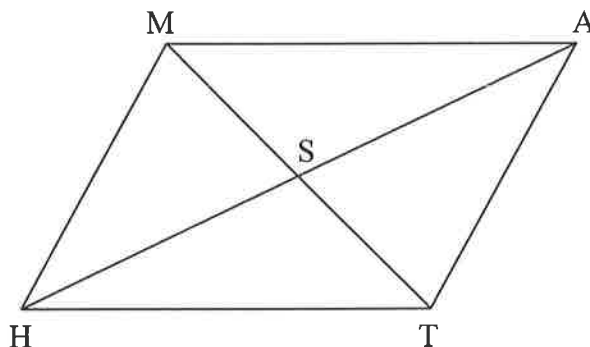
$-15x + 6y = -3$   
 $12x - 6y = -6$   
 $-3x = -9$   
 $x = 3$

$5x - 2 = 2y + 1$   
 $5(3) - 2 = 2y + 1$   
 $13 = 2y + 1$   
 $12 = 2y$   
 $y = 6$

For problems 14-15, complete each statement about  $\square$  MATH. Then justify your answer!!! (Explain why your answer is true.)

14.  $\overline{MA} \cong \overline{HT}$

opposite sides are  $\cong$



15.  $\angle MAT$  is supplementary to  $\angle ATH \cong \angle AMH$

consecutive  $\angle$ s of a  $\square$  are supplementary.

Use rectangle STUV and the given information for problems 16-17. Show your steps and give reasons.

16.  $m\angle 7 = 36$ , find  $m\angle 2$

$m\angle 2 = 54^\circ$

$m\angle 7 + m\angle TSV + m\angle 2 = 180$

$m\angle TSV = 90$

$36 + 90 + m\angle 2 = 180$

$126 + m\angle 2 = 180$

$m\angle 2 = 54$

17.  $m\angle 1 = x + 41$ ,  $m\angle 2 = 3x + 15$ ,

Find  $x$  and  $m\angle 6$ .

$x = 13$

$m\angle 1 = m\angle 2$

$x + 41 = 3x + 15$

$26 = 2x$

$13 = x$

$m\angle 6 = m\angle 1$

$m\angle 6 = x + 41$

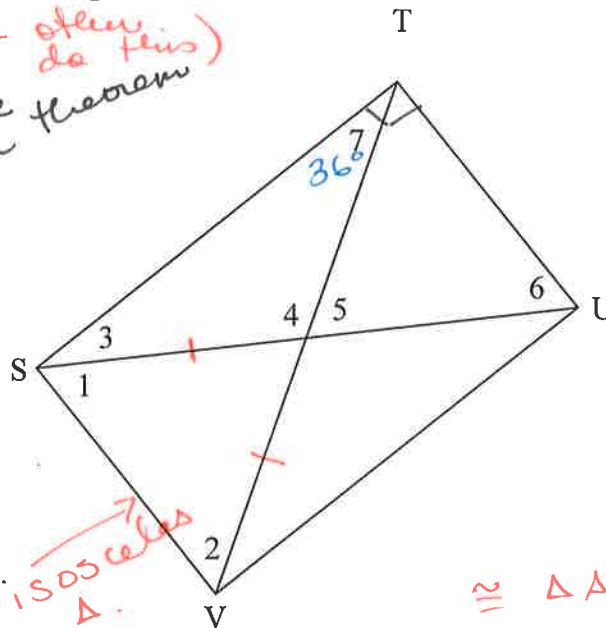
$m\angle 6 = 13 + 41$

$m\angle 6 = 54$

$m\angle 6 = 54$

(there are other ways to do this)

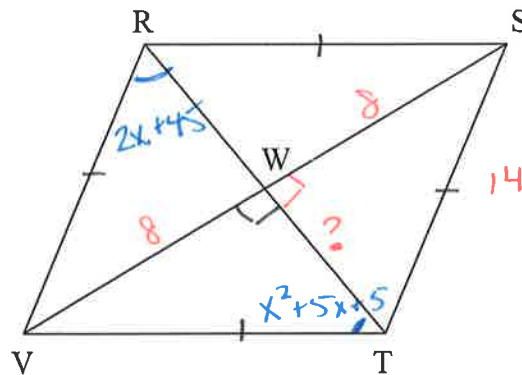
angle sum theorem



isosceles  $\Delta$

$\cong \Delta A$

Quadrilateral RSTV is a rhombus. Use the figure and information for problems 18-19. Give reasons for your setups.



18.  $SV = 16$ ,  $ST = 14$ , Find  $WT$ . (Leave your answer in simplified square root form)

$$WT = \underline{2\sqrt{33}}$$

Right  $\Delta$ , Pythagorean theorem.

$$SW^2 + WT^2 = ST^2$$

$$8^2 + WT^2 = 14^2$$

$$64 + WT^2 = 196$$

$$WT^2 = 132$$

$$WT = \sqrt{132}$$

$$= 2\sqrt{33}$$

19.  $m\angle VRT = 2x + 45$ ,  $m\angle RTV = x^2 + 5x + 5$ , Find  $x$ .

$$x = \underline{5; -8}$$

isosceles  $\Delta$  b/c all 4 sides  $\cong$ .

$$m\angle VRT = m\angle RTV$$

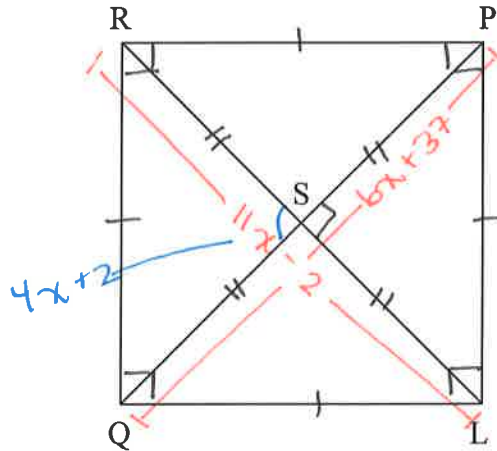
$$2x + 45 = x^2 + 5x + 5$$

$$0 = x^2 + 5x - 2x + 5 - 45$$

$$0 = x^2 + 3x - 40$$

$$0 = (x + 8)(x - 5)$$

Use square QRPL for problems 20-21 to find  $x$ . Give reasons for your setups.



20.  $RL = 11x + 2$   
 $QP = 6x + 37$

$x = \underline{7}$

diagonals are  $\cong$ .

$$RL = QP$$

$$11x + 2 = 6x + 37$$

$$5x = 35$$

$$x = 7$$

21.  $m\angle RSQ = 4x + 2$

$x = \underline{22}$

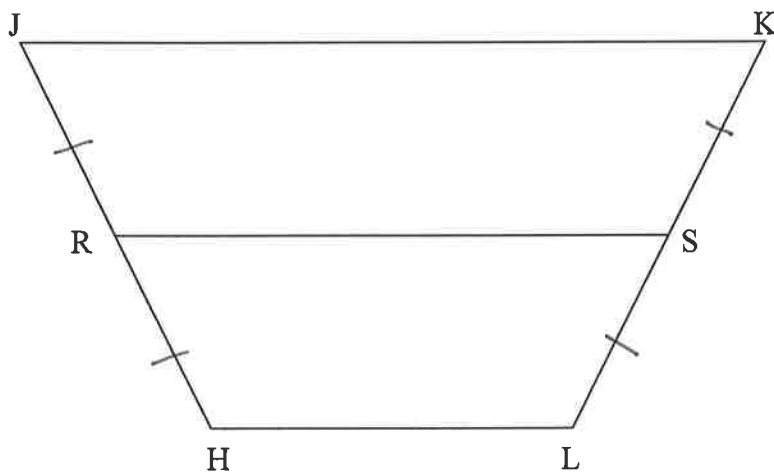
$m\angle RSQ = 90$  diagonals are  $\perp$

$$4x + 2 = 90$$

$$4x = 88$$

$$x = 22$$

Use isosceles trapezoid  $HJKL$  with median  $\overline{RS}$  for problems 22-23. Give reasons for your setups.



Reason enough!

$$m = \frac{1}{2}(a + b)$$

22. If  $HL = 9$  and  $JK = 27$ , Find  $RS$ .

$RS = \underline{18}$

$$RS = \frac{1}{2}(JK + HL)$$

$$RS = \frac{1}{2}(27 + 9)$$

$$RS = \frac{1}{2}(36)$$

$$RS = 18$$

23. If  $JK = 7x - 7$ ,  $RS = 11$ , and  $HL = x + 5$ , Find  $x$ .

$x = \underline{3}$

$$RS = \frac{1}{2}(JK + HL)$$

$$11 = \frac{1}{2}(7x - 7 + x + 5)$$

$$22 = 8x - 2$$

$$24 = 8x$$

$$3 = x$$

For problems 24-28, fill in the blank for each statement with ALWAYS, SOMETIMES, or NEVER.  
(Each of these is worth 1 point each.)

24. A rectangle is Sometimes a rhombus. (if it's a square)

25. Diagonals of a parallelogram are Sometimes congruent. (if it's a rectangle)

26. A square's diagonals are perpendicular but are not congruent. never

27. Diagonals of a rectangle always bisect each other.

28. Diagonals of a parallelogram Sometimes bisect the opposite angles. (if it's a rhombus.)