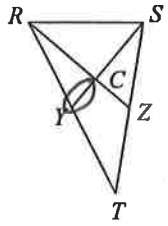


Medians and a centroid

Each figure shows a triangle with one or more of its medians.

1) Find  $CY$  if  $SY = 33$

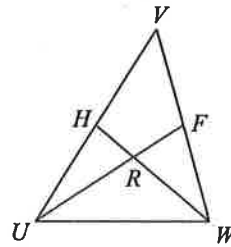


$$CY = \frac{1}{3}(SY)$$

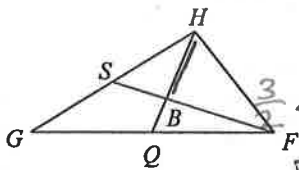
$$CY = \frac{1}{3}(33)$$

$$\boxed{CY = 11}$$

2) Find  $WR$  if  $RH = 2$



3) Find  $HQ$  if  $HB = 4.8$

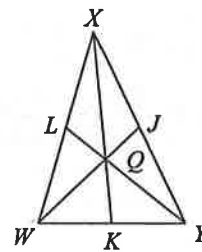


$$HB = \frac{2}{3}(HQ)$$

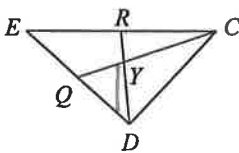
$$4.8 = \frac{2}{3}(HQ) \cdot \frac{3}{2}$$

$$\boxed{7.2 = HQ}$$

4) Find  $QJ$  if  $WQ = 5$



5) Find  $DY$  if  $DR = 16.5$

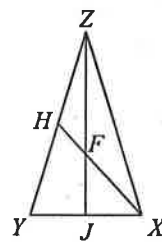


$$DY = \frac{2}{3}(DR)$$

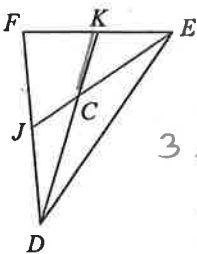
$$DY = \frac{2}{3}(16.5)$$

$$\boxed{DY = 11}$$

6) Find  $FJ$  if  $ZF = 6$



7) Find  $DK$  if  $CK = 12$

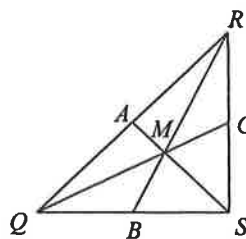


$$CK = \frac{1}{3}(DK)$$

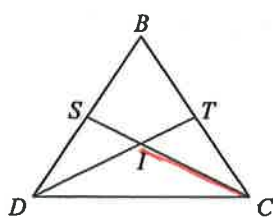
$$3 \cdot 12 = \frac{1}{3}(DK) \cdot 3$$

$$\boxed{36 = DK}$$

8) Find  $QM$  if  $MC = 7$



9) Find  $CI$  if  $CS = 6$



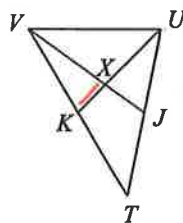
$$CI = \frac{2}{3}(CS)$$

$$CI = \frac{2}{3}(6)$$

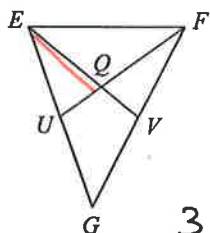
$$\boxed{CI = 4}$$

10) Find  $XK$  if  $UX = 8$

where  $Y$  not counted.



11) Find  $x$  if  $EQ = x + \frac{4}{5}$  and  $EV = \frac{8}{5}x + \frac{1}{10}$



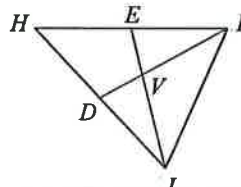
$$EQ = \frac{2}{3}(EV)$$

$$x + \frac{4}{5} = \frac{2}{3}\left(\frac{8}{5}x + \frac{1}{10}\right)$$

$$3x + \frac{12}{5} = 2\left(\frac{8}{5}x + \frac{1}{10}\right)$$

$$3x + \frac{12}{5} = \frac{16}{5}x + \frac{2}{10}$$

12) Find  $x$  if  $JV = 3x - 6$  and  $VE = 2x - 7$

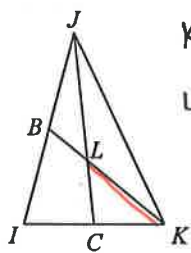


$$\frac{15}{5}x + \frac{12}{5} = \frac{16}{5}x + \frac{1}{5}$$

$$15x + 12 = 16x + 1$$

$$\boxed{11 = x}$$

13) Find  $x$  if  $KL = 4x - 8$  and  $KB = 3x + 12$



$$KL = \frac{2}{3}(KB)$$

$$4x - 8 = \frac{2}{3}(3x + 12)$$

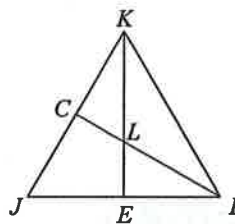
$$4x - 8 = 2(x + 4)$$

$$4x - 8 = 2x + 8$$

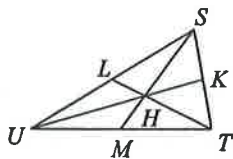
$$2x = 16$$

$$\boxed{x = 8}$$

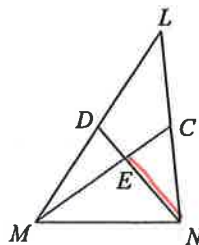
14) Find  $x$  if  $KL = 7x + 1$  and  $LE = 2x + 5$



15) Find  $x$  if  $SM = 2x + 2$  and  $HM = 2x - 2$



16) Find  $x$  if  $NE = x + 4$  and  $ND = 2x$



$$NE = \frac{2}{3}(ND)$$

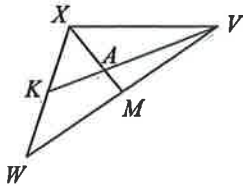
$$x + 4 = \frac{2}{3}(2x)$$

$$3(x + 4) = 2(2x)$$

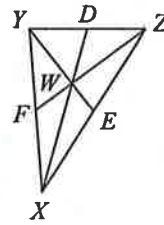
$$3x + 12 = 4x$$

$$\boxed{12 = x}$$

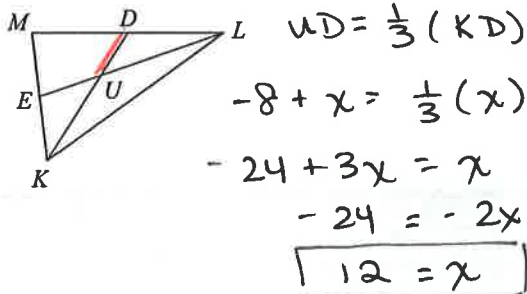
17) Find  $x$  if  $VA = x + 4$  and  $AK = x - 1$



18) Find  $x$  if  $ZW = -6 + 2x$  and  $WF = 2x - 9$

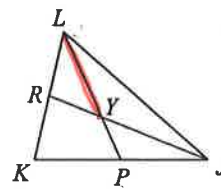


19) Find  $x$  if  $KD = x$  and  $UD = -8 + x$



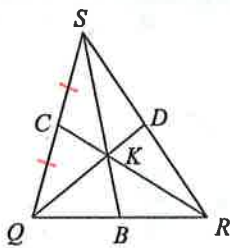
$$\begin{aligned}
 UD &= \frac{1}{3}(KD) \\
 -8 + x &= \frac{1}{3}(x) \\
 -24 + 3x &= x \\
 -24 &= -2x \\
 \boxed{12} &= x
 \end{aligned}$$

20) Find  $x$  if  $LY = 4x$  and  $LP = 5x + 1$



$$\begin{aligned}
 LY &= \frac{2}{3}(LP) \\
 4x &= \frac{2}{3}(5x + 1) \\
 12x &= 2(5x + 1) \\
 12x &= 10x + 2 \\
 2x &= 2 \\
 \boxed{x} &= 1
 \end{aligned}$$

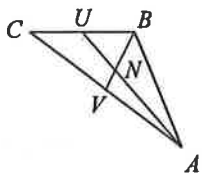
21) Find  $CS$  if  $CQ = \frac{2x-9}{2}$  and  $CS = \frac{1+x}{2}$



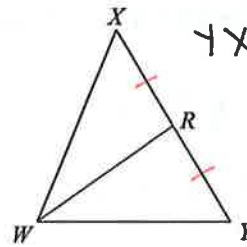
$$\begin{aligned}
 CQ &= CS \\
 \frac{2x-9}{2} &= \frac{1+x}{2} \\
 2x-9 &= 1+x \\
 x &= 10
 \end{aligned}$$

$$\begin{aligned}
 CS &= \frac{1+x}{2} \\
 &= \frac{1+10}{2} \\
 \boxed{CS} &= \frac{11}{2}
 \end{aligned}$$

23) Find  $AN$  if  $AN = x + 4$  and  $NU = \frac{2x-1}{2}$



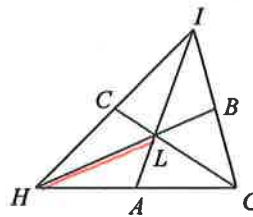
22) Find  $RY$  if  $YX = x - 2$  and  $RX = x - 7$



$$\begin{aligned}
 YX &= 2(RX) \\
 x-2 &= 2(x-7) \\
 x-2 &= 2x-14 \\
 12 &= x
 \end{aligned}$$

$$\begin{aligned}
 RY &= RX \\
 RY &= x-7 \\
 RY &= 12-7 \\
 \boxed{RY} &= 5
 \end{aligned}$$

24) Find  $HL$  if  $HL = 3x + 1$  and  $HB = 7x - 1$

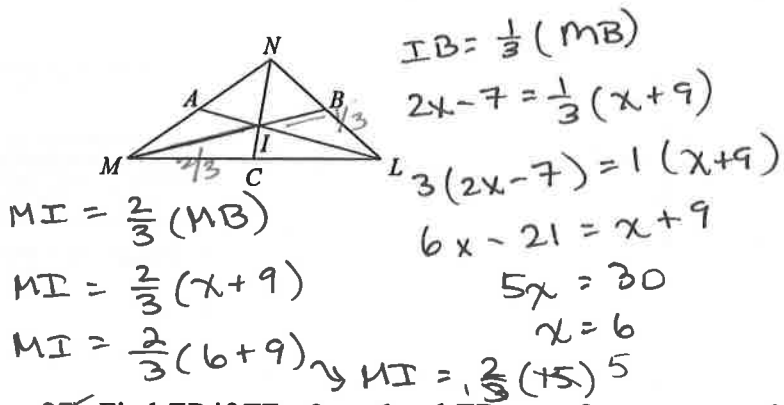


$$\begin{aligned}
 HL &= \frac{2}{3}(HB) \\
 3x+1 &= \frac{2}{3}(7x-1) \\
 3(3x+1) &= 2(7x-1) \\
 9x+3 &= 14x-2
 \end{aligned}$$

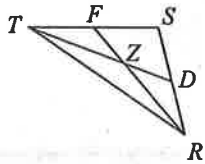
$$\begin{aligned}
 HL &= 3x+1 \\
 HL &= 3(1)+1 \\
 \boxed{HL} &= 4
 \end{aligned}$$

$$\begin{aligned}
 5 &= 5x \\
 1 &= x
 \end{aligned}$$

- 25) Find  $MI$  if  $MB = x + 9$  and  $IB = 2x - 7$

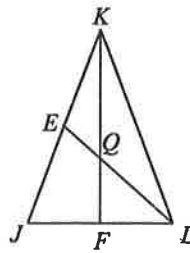


- 27) Find  $ZD$  if  $TZ = 2x - 6$  and  $TD = x + 9$

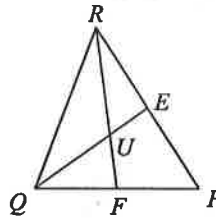


$MI = 10$

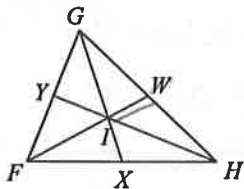
- 26) Find  $LQ$  if  $LQ = x - 6$  and  $QE = x - 8$



- 28) Find  $QE$  if  $QU = x - 4$  and  $UE = x - 8$



- 29) Find  $IW$  if  $FW = 10x$  and  $IW = 2x + 4$



$IW = \frac{1}{3}(FW)$   
 $2x + 4 = \frac{1}{3}(10x)$   
 $3(2x + 4) = 10x$   
 $6x + 12 = 10x$   
 $12 = 4x$   
 $3 = x$

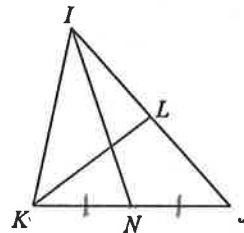
$IW = 2x + 4$

$IW = 2(3) + 4$

$IW = 6 + 4$

$IW = 10$

- 30) Find  $NK$  if  $NJ = \frac{2x - 3}{4}$  and  $NK = \frac{x}{4}$



$NJ = NK$   
 $\frac{2x - 3}{4} = \frac{x}{4}$

$2x - 3 = x$

$x = 3$

$NK = \frac{x}{4}$

$NK = \frac{3}{4}$