

ODDS

Write and Graph Inequalities

Example 1 Write an inequality for the sentence.

Fewer than 70 students attended the last dance.

Words	Fewer than 70 students attended the last dance.
Variable	Let s = the number of students.
Inequality	$s < 70$

Example 2 Graph each inequality on a number line.

a. $x > 8$



The **open dot** means 8 does *not* make the sentence true. The graph to the right means that numbers greater than 8 make the sentence true.

b. $x \leq 8$



The **closed dot** means 8 *does* make the sentence true. The graph to the left means that numbers less than 8 make the sentence true.

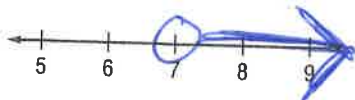
Exercises

Write an inequality for each sentence.

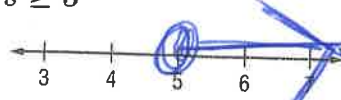
- The maximum height h is 45 feet.
- The weight m of all adult male elephants is over 12,000 pounds.
- The maximum fee f for any student is \$15.
- You must be at least 38 inches tall to ride the roller coaster.

Graph each inequality on the number line.

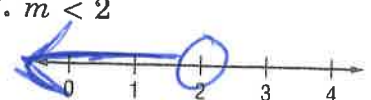
5. $x > 7$



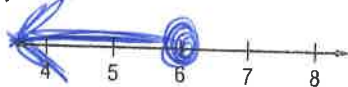
6. $s \geq 5$



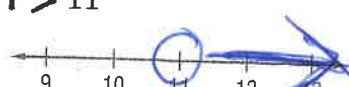
7. $m < 2$



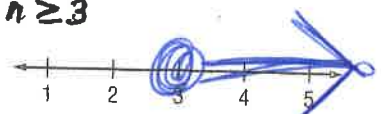
8. $f \leq 6$



9. $r > 11$



10. $n \geq 3$



Skills Practice

Write and Graph Inequalities

Write an inequality for each sentence.

1. More than 40,000 fans attended the opening football game at the University of Florida.

$$x > 40,000$$

2. Her earnings were no more than \$86.

$$x \leq 86$$

3. A savings account balance is now less than \$550.

$$x < 550$$

4. The number of club members is at least 25.

$$x \geq 25$$

5. The spring calf class at the cattle show is for calves that weigh 825 pounds or less.

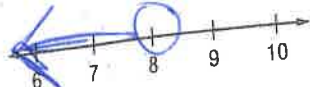
$$x \leq 825$$

6. The minimum deposit for a new checking account is \$75.

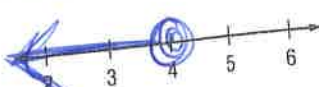
$$x \geq 75$$

Graph each inequality on the number line.

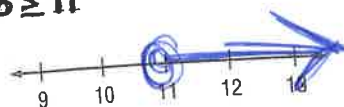
7. $a < 8$



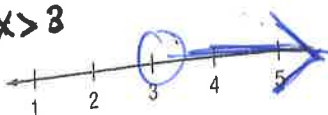
8. $d \leq 4$



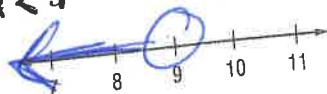
9. $b \geq 11$



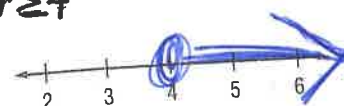
10. $x > 3$



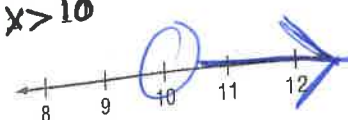
11. $x < 9$



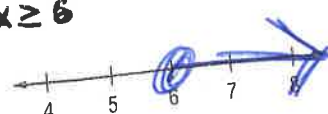
12. $r \geq 4$



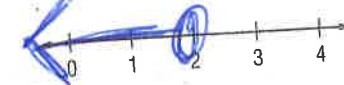
13. $x > 10$



14. $x \geq 6$



15. $x \leq 2$

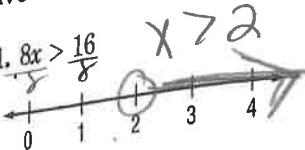


Skills Practice

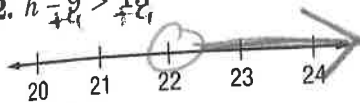
Solve One-Step Inequalities

Solve each inequality. Graph the solution on a number line.

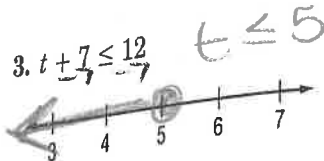
$$1. 8x > \frac{16}{8}$$



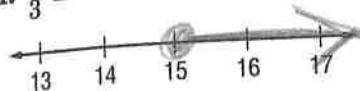
$$2. h - 9 > \frac{13}{1}$$



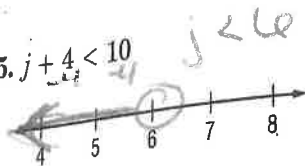
$$3. t + 7 \leq \frac{12}{1}$$



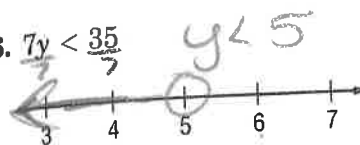
$$4. \frac{r}{3} \geq 5.3$$



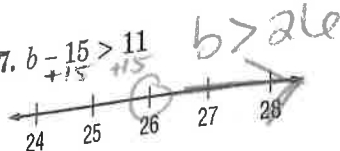
$$5. j + 4 < \frac{10}{1}$$



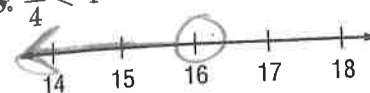
$$6. 7y < \frac{35}{7}$$



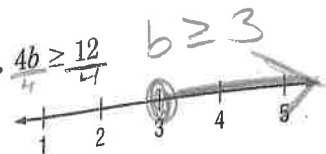
$$7. b - 15 > \frac{11}{1}$$



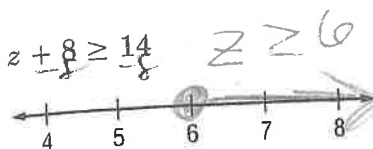
$$8. \frac{n}{4} < 4.4$$



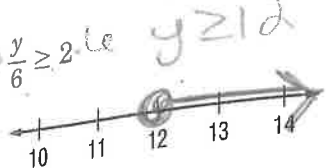
$$9. 4b \geq \frac{12}{4}$$



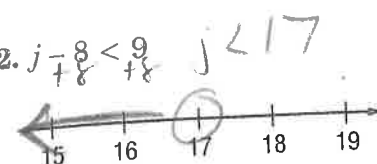
$$10. z + 8 \geq \frac{14}{1}$$



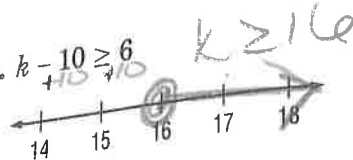
$$11. \frac{y}{6} \geq 2$$



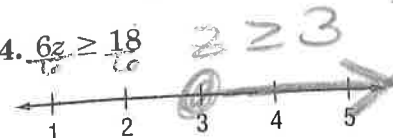
$$12. j - 8 < \frac{9}{1}$$



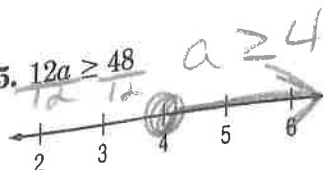
$$13. k - 10 \geq \frac{6}{1}$$



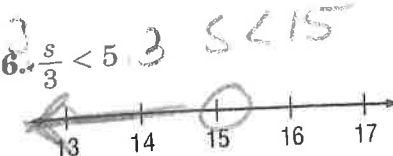
$$14. 6z \geq \frac{18}{6}$$



$$15. 12a \geq \frac{48}{12}$$



$$16. \frac{s}{3} < 5.3$$



17. **SHOPPING** Chantal would like to buy a new pair of running shoes. The shoes she likes start at \$85. If she has already saved \$62, write an inequality to show how much more money Chantal must save.

$$x + 62 \geq 85$$

$$-62 \quad -62$$

$$x \geq 23$$

She must save
at least \$23

Reteach**Two-Step Inequalities**

Example Four more than 3 times a number is less than 28. Write, solve, and graph an inequality to represent this situation.

Words	<i>Four more than 3 times a number is less than 28.</i>
Variable	Let n = the number.
Inequality	$3n + 4 < 28$

$$3n + 4 < 28$$

Write the inequality.

$$\begin{array}{r} 3n + 4 < 28 \\ -4 \quad -4 \end{array}$$

Subtract 4 from each side.

$$3n < 24$$

Simplify.

$$\frac{3n}{3} < \frac{24}{3}$$

Divide each side by 3.

$$n < 8$$

Simplify.

The solution is $n < 8$. To graph it, draw an open circle at 8 and draw an arrow to the left on the number line.

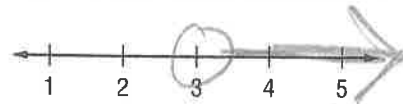
**Exercises**

Write, solve, and graph an inequality to represent each sentence.

1. 25 is less than 10 more than 5 times a number.

$$25 < 5n + 10$$

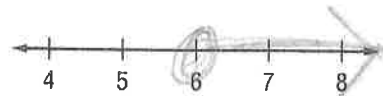
$$n > 3$$



2. Eight less than 3 times a number is greater than or equal to 10.

$$3x - 8 \geq 10$$

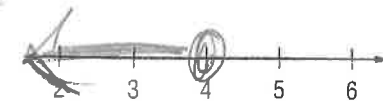
$$x \geq 6$$



3. Five more than 6 times a number is less than or equal to 29.

$$6n + 5 \leq 29$$

$$n \leq 4$$



4. **PEDAL BOATS** It costs \$25 plus \$6 per hour to rent a pedal boat at the lake. The minimum fee is \$43. What is the minimum number of hours for which you can rent the pedal boat?

$$25 + 6x \geq 43$$



Skills Practice

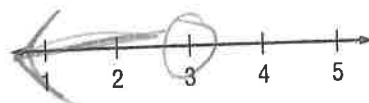
Two-Step Inequalities

Solve and graph each inequality.

1. $12 > 6 + 2n$

$$\begin{array}{r} -6 \quad -6 \\ \hline 6 > 2n \\ \frac{6}{2} > \frac{2n}{2} \\ 3 > n \end{array}$$

$$n < 3$$



2. $4n - 7 \geq 21$

$$\begin{array}{r} +7 \quad +7 \\ \hline 4n \geq 28 \\ \frac{4n}{4} \geq \frac{28}{4} \end{array}$$

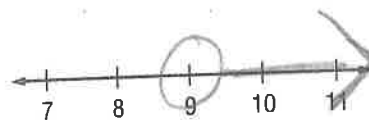
$$n \geq 7$$



3. $5n - 16 > 29$

$$\begin{array}{r} +16 \quad +16 \\ \hline 5n > 45 \\ \frac{5n}{5} > \frac{45}{5} \end{array}$$

$$n > 9$$



4. $24 \leq 12 + 3n$

$$\begin{array}{r} -12 \quad -12 \\ \hline 12 \leq 3n \\ \frac{12}{3} \leq \frac{3n}{3} \end{array}$$

$$n \geq 4$$



5. $2n - 9 \geq 17$

$$\begin{array}{r} +9 \quad +9 \\ \hline 2n \geq 26 \\ \frac{2n}{2} \geq \frac{26}{2} \end{array}$$

$$n \geq 13$$



6. $56 > 6 + 10n$

$$\begin{array}{r} -6 \quad -6 \\ \hline 50 > 10n \\ \frac{50}{10} > \frac{10n}{10} \end{array}$$

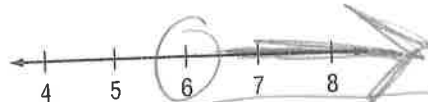
$$n < 5$$



7. **SALES** Eric gets paid \$7 for each hour he works at the electronics store, plus an extra \$2 for every store membership card he sells. How many memberships does he have to sell if he wants to make more than \$40 for working 4 hours?

$$\begin{array}{l} 7(4) + 2x > 40 \\ 28 + 2x > 40 \end{array}$$

$x > 6$ more than 6 memberships.



8. **CONTEST** In a class contest, students get 8 points for each book they read plus an extra 5 points for each book report they write. If a student reads 3 books and wants at least 34 points, how many reports does she have to write?

$$\begin{array}{l} 8(3) + 5r \geq 34 \\ 24 + 5r \geq 34 \\ r \geq 2 \end{array}$$



at least 2 reports

Name _____ Class _____ Date _____

Practice 2-3

Simplifying Algebraic Expressions

Simplify each expression.

1. $4a + 7 + 2a$

$$6a + 7$$

2. $8(k - 9)$

$$8k - 72$$

3. $5n + 6n - 2n$

$$9n$$

4. $(w + 3)7$

$$7w + 21$$

5. $5(b - 6) + 9$

$$5b - 30 + 9$$

$$5b - 21$$

6. $-4 + 8(2 + t)$

$$-4 + 16 + 8t$$

$$12 + 8t$$

7. $-4 + 3(6 + k)$

$$-4 + 18 + 3k$$

$$14 + 3k$$

8. $12j - 9j$

$$3j$$

9. $6(d - 8)$

$$6d - 48$$

10. $-9 + 8(x + 6)$

$$-9 + 8x + 48$$

$$8x + 39$$

11. $4(m + 6) - 3$

$$4m + 24 - 3$$

$$4m + 21$$

12. $27 + 2(f - 19)$

$$27 + 2f - 38$$

$$2f - 11$$

13. $4v - 7 + 8v + 4 - 5$

$$12v - 8$$

14. $5(g + 8) + 7 + 4g$

$$5g + 40 + 7 + 4g$$

$$9g + 47$$

15. $12h - 17 - h + 16 - 2h$

$$9h - 1$$

16. $7(e - 8) + 12 - 2e$

$$7e - 56 + 12 - 2e$$

$$5e - 44$$

17. $-3y + 7 + y + 6y$

$$4y + 7$$

18. $(3.2m + 1.8) - 1.07m$

$$2.13m + 1.8$$

$$4a - 28b$$

$$4(a - 7b)$$

$$9a - 3g$$

$$3(3a - g)$$

$$7a - 42z$$

$$7(a - 6z)$$

$$81a + 9p$$

$$9(9a + p)$$

$$25a - 5h$$

$$5(5a - h)$$

$$7a + 63$$

$$7(a + 9)$$

$$4a - 20m$$

$$4(a - 5m)$$

$$4a - 24$$

$$4(a - 6)$$

$$30a + 6s$$

$$6(5a + s)$$

$$3a + 24$$

$$3(a + 8)$$

Distributive Property

$$\textcircled{1} \quad 6(4d - 11)$$

$24d - 66$

$$\textcircled{2} \quad 3(6d + 8)$$

$18d + 24$

$$\textcircled{3} \quad 2(9y + 11)$$

$18y + 22$

$$\textcircled{4} \quad -5(4p + 7)$$

$-20p - 35$

$$\textcircled{5} \quad -4(5x - 8)$$

$-20x + 32$

$$\textcircled{6} \quad 7(3 + 2x)$$

$21 + 14x$

$$\textcircled{7} \quad -(x + 5)$$

$-x - 5$

$$\textcircled{8} \quad -(-x - 5)$$

$x + 5$

$$\textcircled{9} \quad 4(3r + 5)$$

$12r + 20$

$$\textcircled{10} \quad 8(6 + 2b)$$

$48 + 16b$

$$\textcircled{11} \quad 17 + 5(7d - 8)$$

$17 + 35d - 40$
 $35d - 23$

$$\textcircled{12} \quad 3(4z - 7) + 15z$$

$12z - 21 + 15z$
 $27z - 21$

Review Combining
Like Terms:

$$\textcircled{13} \quad -13 + 12r + 6$$

$12r - 7$

$$\textcircled{14} \quad 13 - 16d - 9d$$

$13 - 25d$

$$\textcircled{15} \quad -x + 4 + 5x - 2$$

$4x + 2$

$$\textcircled{16} \quad 16y + 8 - 4y - 3$$

$12y + 5$

$$\textcircled{17} \quad x + y + 2x + 3y$$

$3x + 4y$

$$\textcircled{18} \quad z + z + 8 - 10$$

$2z - 2$

Factoring Expressions

① $2x + 4$
 $2(x+2)$

② $6t + 12$
 $6(t+2)$

③ $-4x + 8$
 $-4(x-2)$

④ $24 + 6z$
 $6(4+z)$

⑤ $3x + 9x$
 $3x(1+3)$

⑥ $-5t + 15$
 $-5(t-3)$

⑦ $-7x - 49$
 $-7(x+7)$

⑧ $36y + 6$
 $6(y+1)$

⑨ $81 - 9v$
 $9(9-v)$

⑩ $25x + 15 + 10y$
 $5(5x+3+2y)$

Review Distributive Property:

⑪ $5(x+3) = 5x+15$

⑫ $-2(x+10) = -2x-20$

⑬ $4(-x-2) = -4x-8$

Review Combining Like Terms:

⑭ $3x - 8 + 7x - 2$
 $10x - 10$

⑮ $-x + 5x + 10 + 12$
 $4x + 22$