

Solve:

1) What is the derivative of $v(x) = \log_4(\cos x)$?

$$\begin{aligned}v(x) &= \log_4 u & u &= \cos x \\v'(x) &= \frac{1}{u \cdot \ln 4} \cdot u' & u' &= -\sin x \\&= \frac{-\sin x}{\cos x \cdot \ln 4} \text{ or } \boxed{\frac{-\tan x}{\ln 4}}\end{aligned}$$

3) What is $\frac{d}{dx} \log_3 x$?

$$= \frac{1}{x \ln 3}$$

2) Given $p(x) = \log_8 x$.

$$\text{What is } \frac{dp}{dx} ? = \frac{1}{x \ln 8} \text{ or } \frac{1}{3x \ln 2}$$

4) Given $d(x) = \log_9 x$.

$$\text{What is } \frac{dd}{dx} ? = \frac{1}{x \ln 9} \text{ or } \frac{1}{2x \ln 3}$$

5) What is the derivative of $w(x) = e^{x^2+x-1}$?

$$\begin{aligned}w(x) &= e^u & u &= x^2 + x - 1 \\w'(x) &= e^u \cdot u' & u' &= 2x + 1 \\&= \boxed{(2x+1)e^{x^2+x-1}}\end{aligned}$$

6) Given $n(x) = 7^{x-2}$. What is $n'(x)$?

$$= \ln 7 \cdot 7^{x-2}$$

7) Given $w(x) = 4^{\sin x}$.

$$\begin{aligned}\text{What is } \frac{dw}{dx} ? & & u &= \sin x \\& & u' &= \cos x \\w(x) &= 4^u \\w'(x) &= \ln 4 \cdot 4^u \cdot u' \\&= \boxed{\ln 4 \cdot \cos x \cdot 4^{\sin x}}\end{aligned}$$

8) Given $n(x) = e^{3x^2+5x+4}$.

$$\begin{aligned}\text{What is } \frac{dn}{dx} ? & & u &= 3x^2 + 5x + 4 \\& & u' &= 6x + 5 \\n(x) &= e^u \\n'(x) &= e^u \cdot u' \\&= \boxed{(6x+5)e^{3x^2+5x+4}}\end{aligned}$$